



# Signatures of collective behavior in small collision systems

Igor Kozlov

I. K, M. Luzum, G. Denicol, S. Jeon, C. Gale (**1405.3976**)

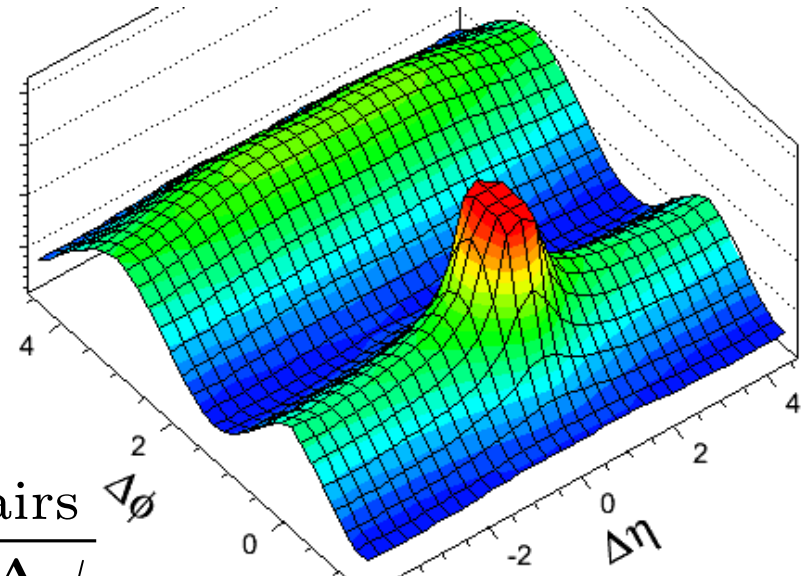
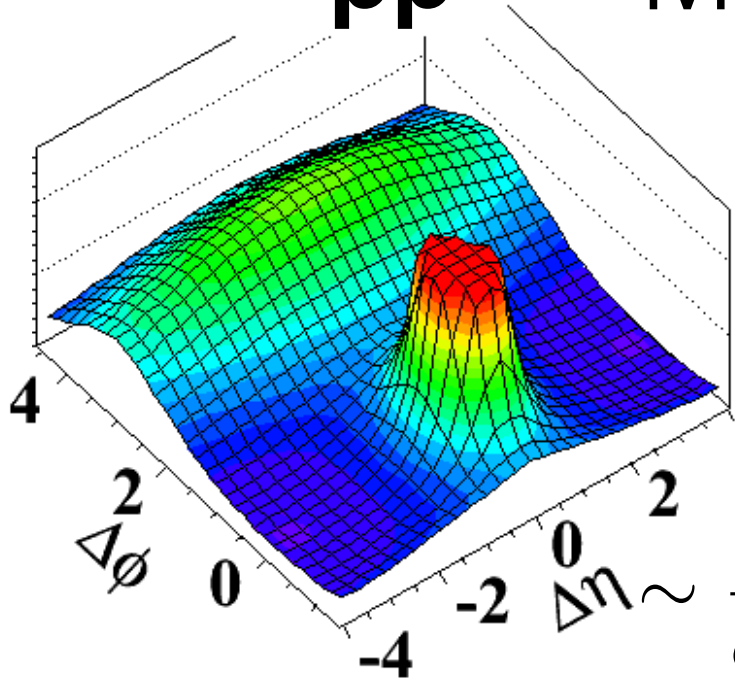
JET Summer School (Davis, CA), June 21, 2014

**pp**

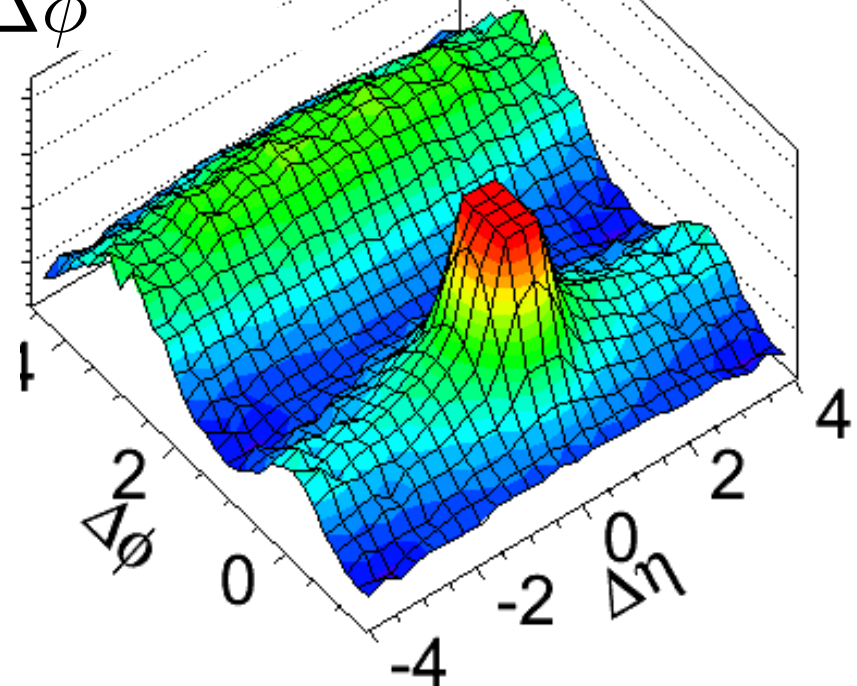
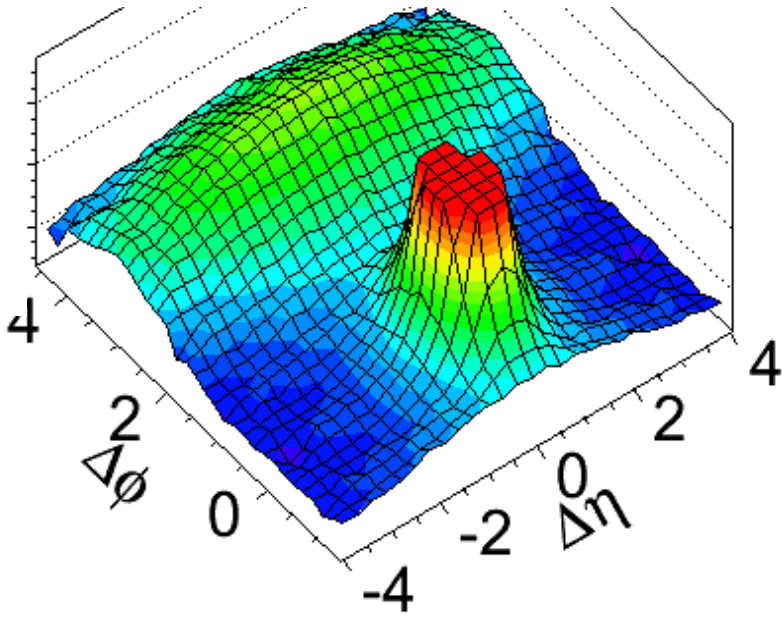
Motivation

**PbPb**

CMS 1305.0609



$$\frac{d^2 N_{\text{pairs}}}{d\Delta\eta d\Delta\phi}$$



**pPb low multiplicity**

**pPb high multiplicity**

# Are particle azimuthal anisotropies due to hydro?

- Check whether experimental data can be described with hydrodynamics
- Introduce a more stringent test on hydrodynamics (observable  $r_n$ ), which gives another handle to explore HIC
- Use MUSIC: Schenke, Jeon & Gale, PRL 106 (2011)

pPb low multiplicity

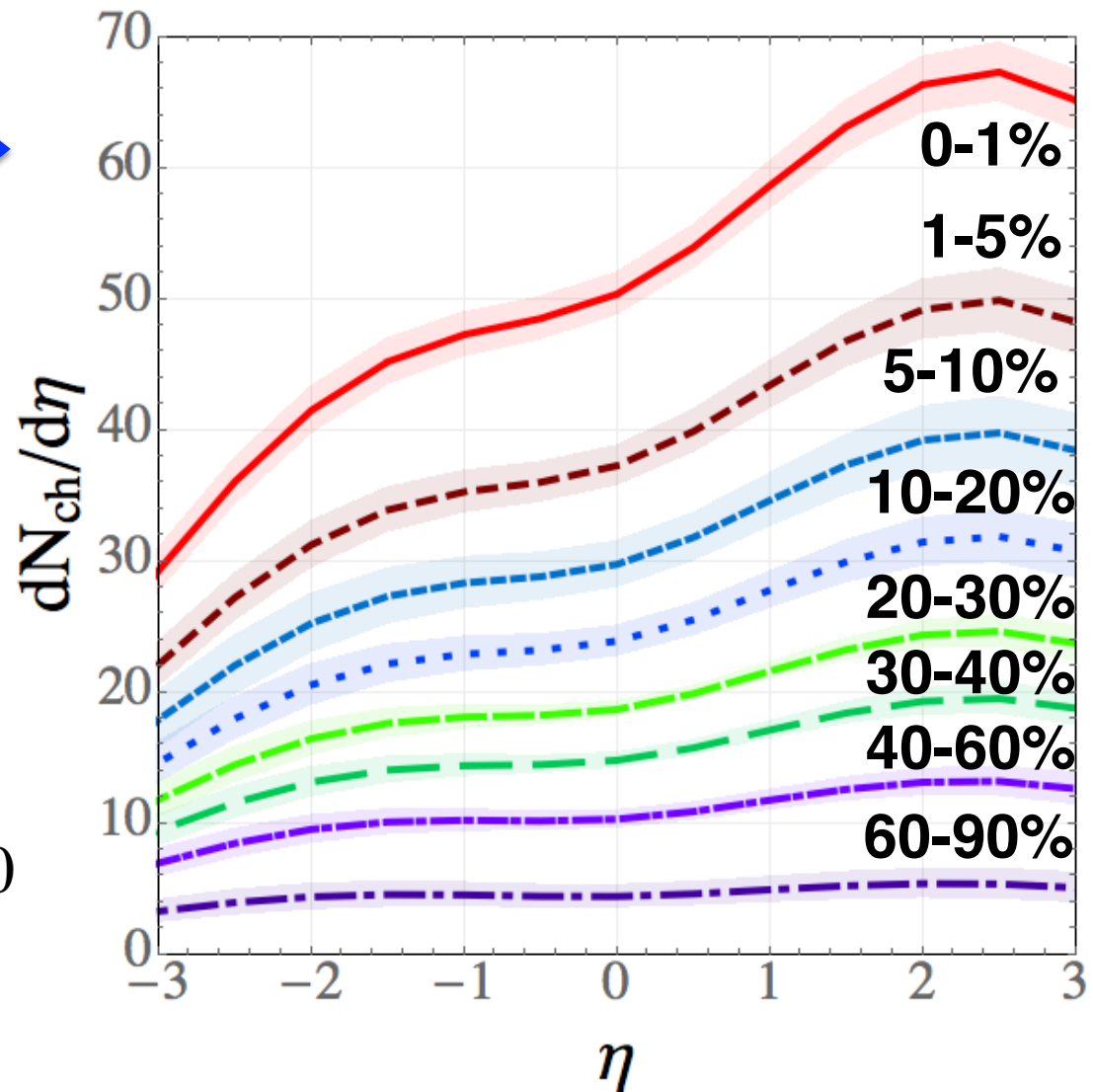
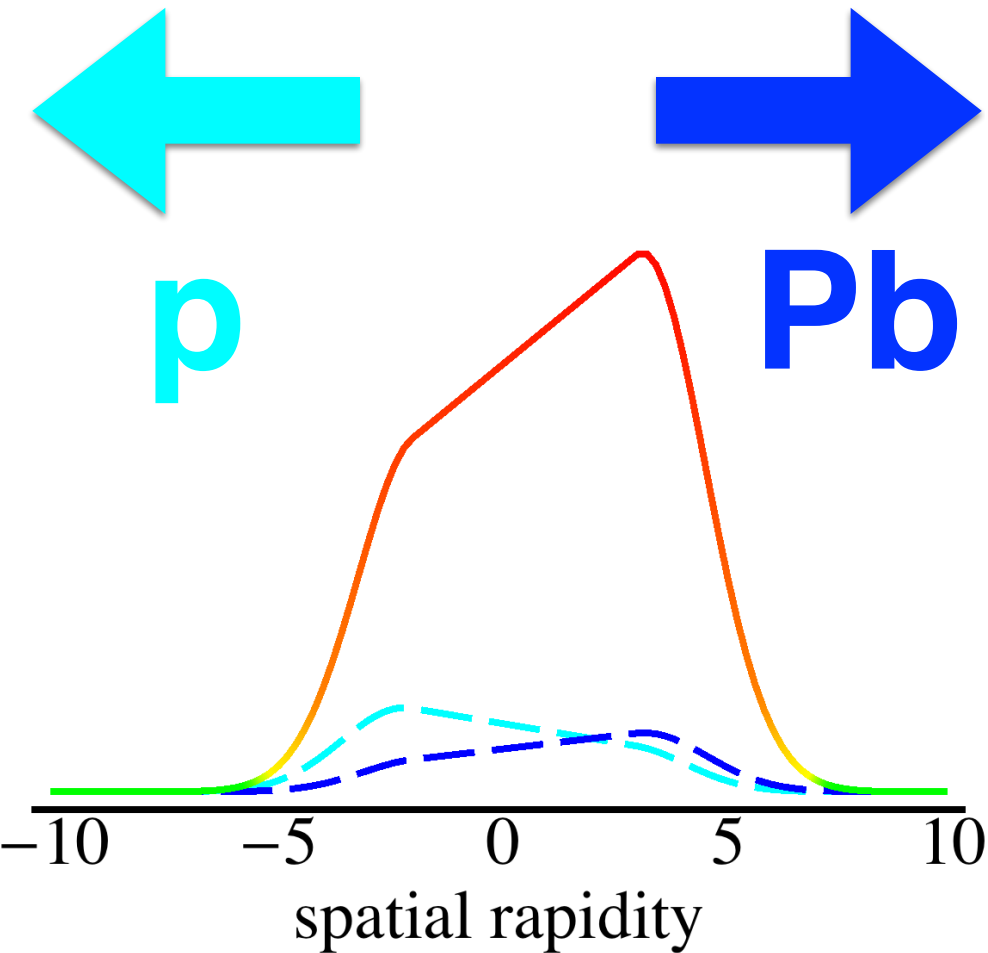
pPb high multiplicity

# Glauber + rapidity distribution

initial entropy profile



final multiplicity profile

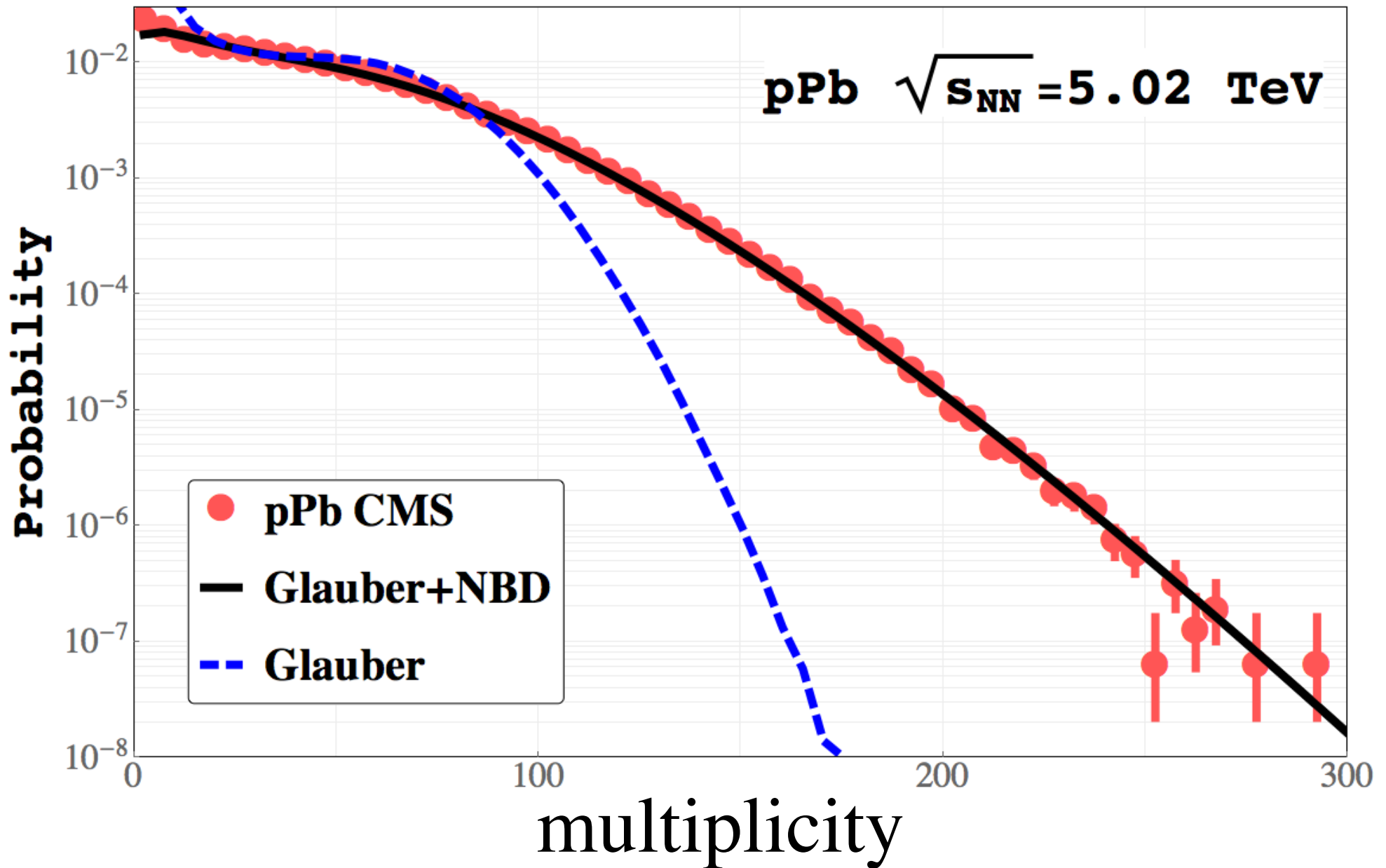


Bozek, Wyskiel 1002.4999

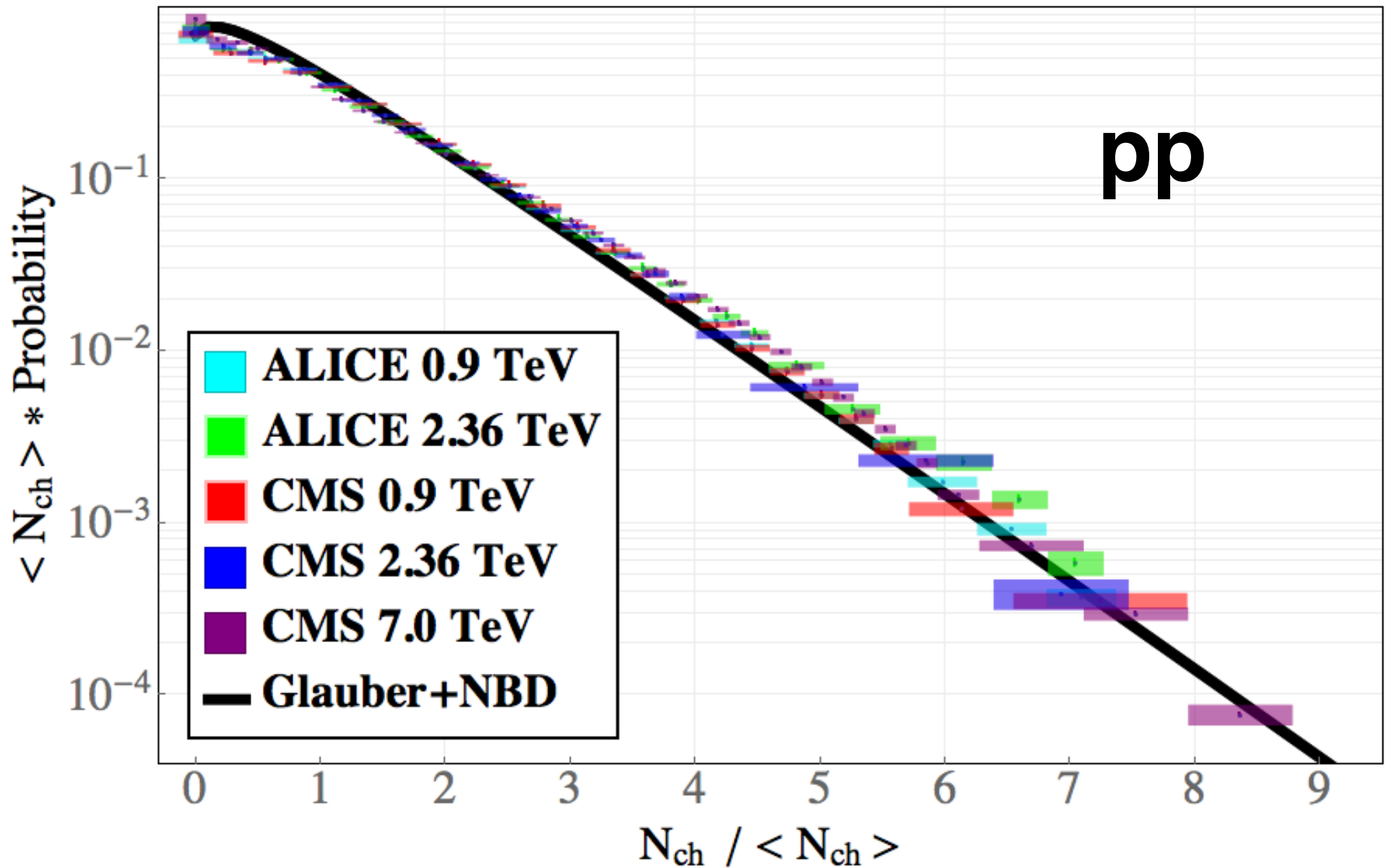
McGill, LBNL 1405.3976



# Glauber+NBD

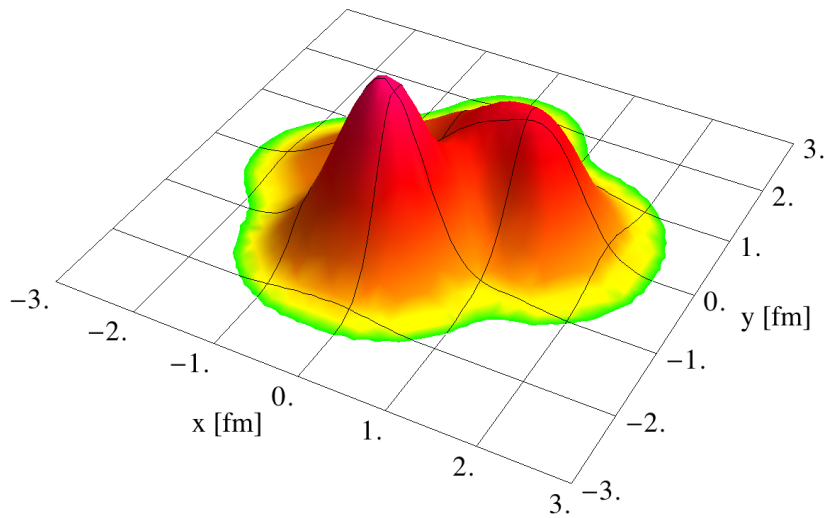


# pp multiplicity with **Glauber+NBD**

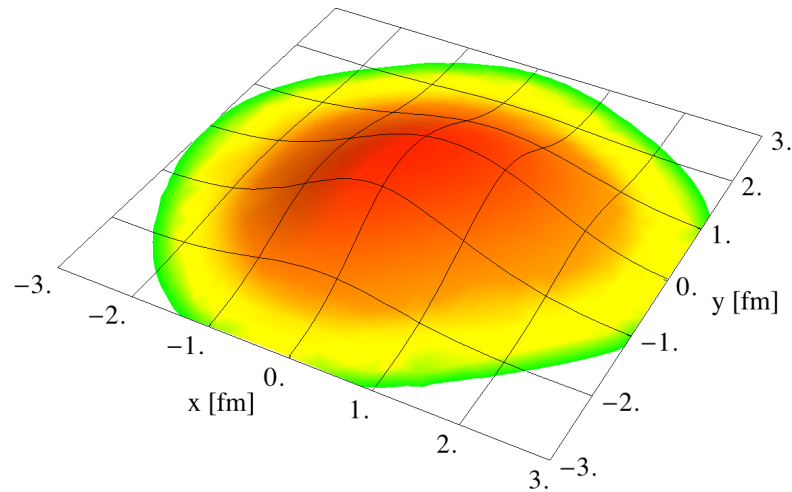


# Transverse granularity

$$\sigma = 0.40 \text{ fm}$$



$$\sigma = 0.80 \text{ fm}$$

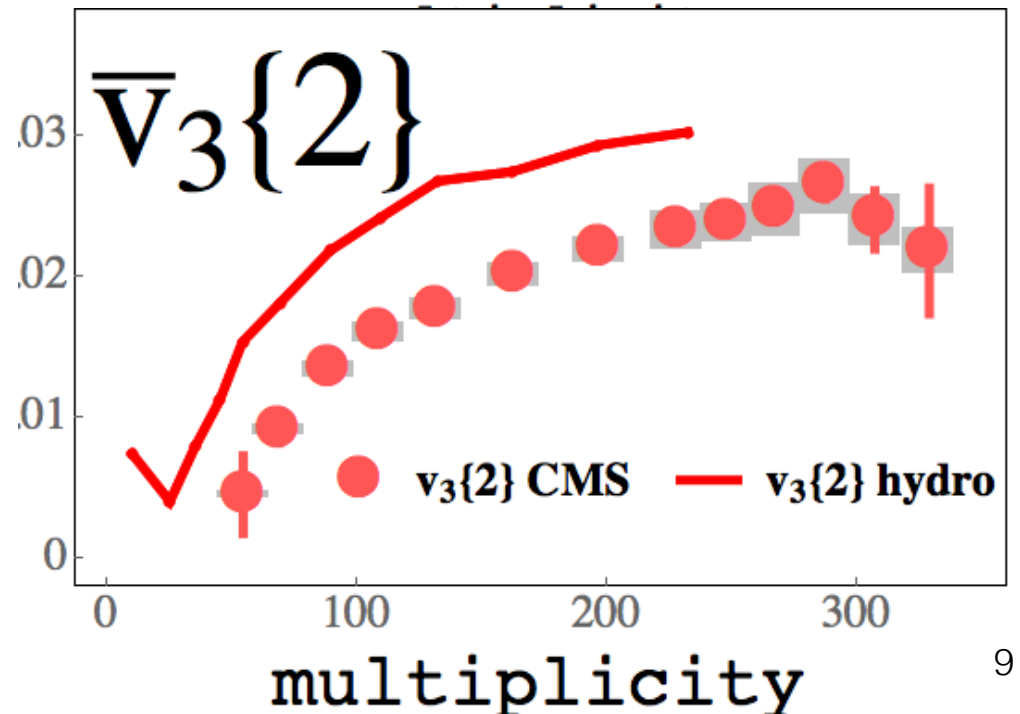
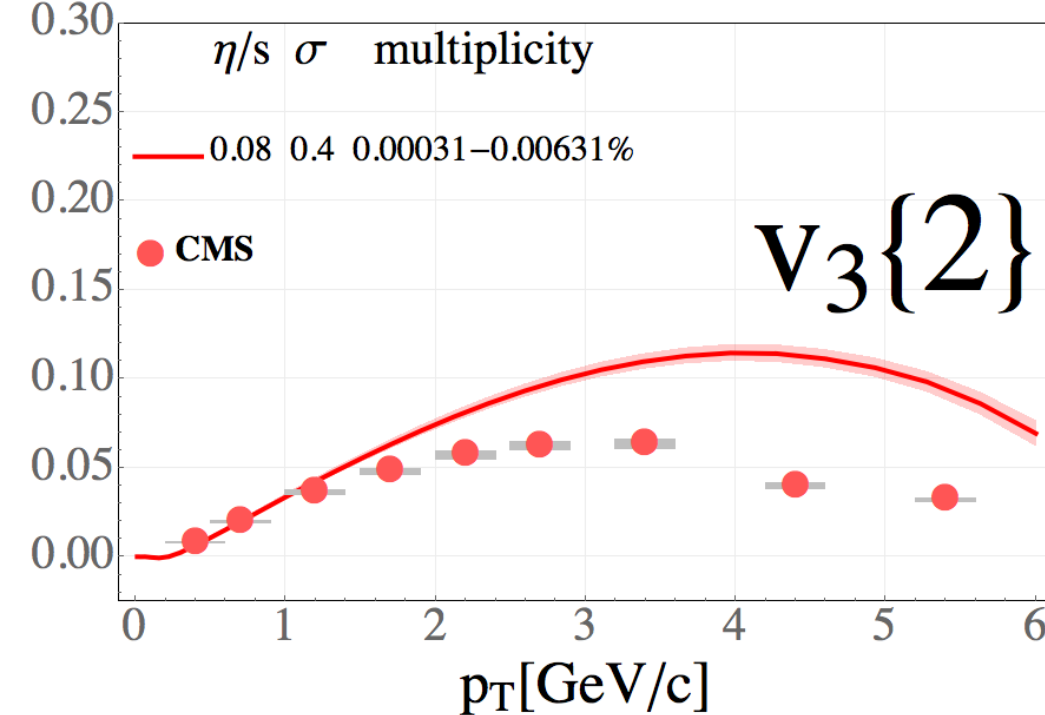
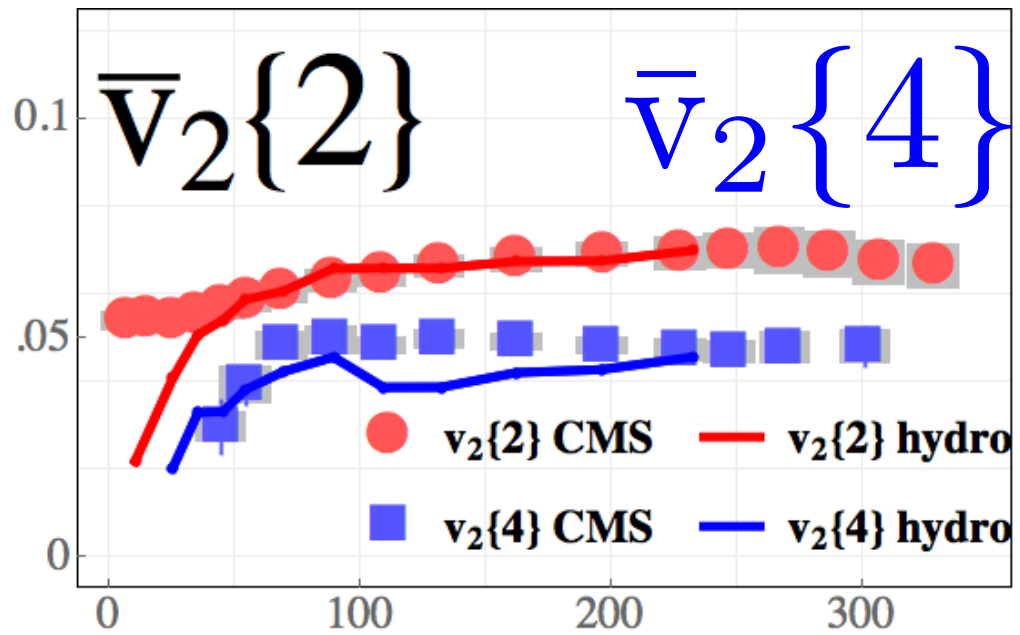
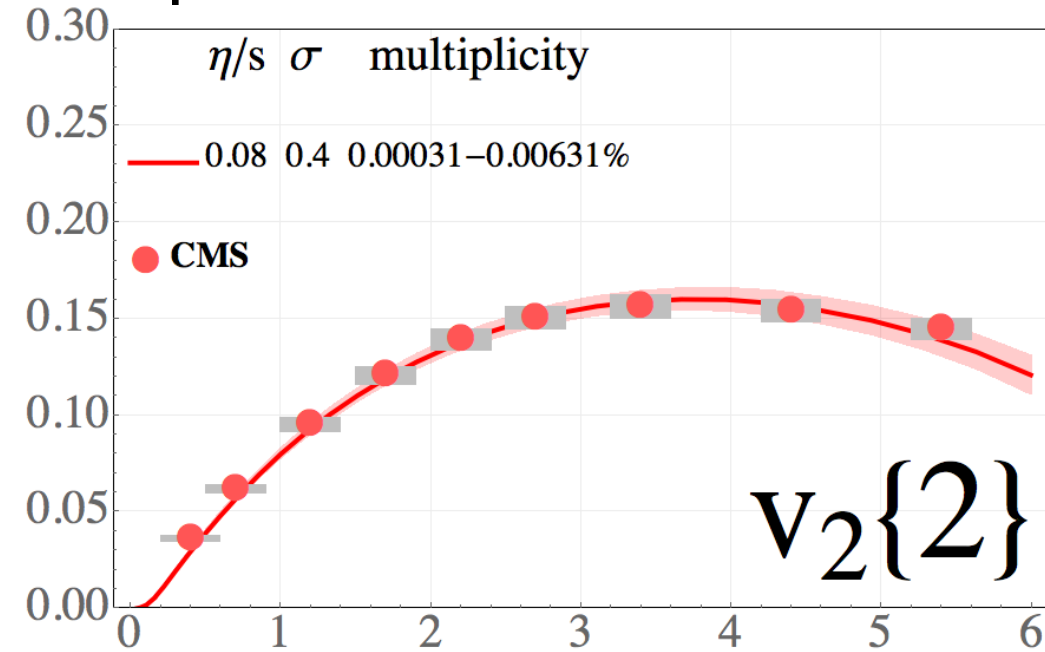


Compare with hydro; start with:

$$\sigma = 0.4 \text{ fm} \quad \eta/s = 0.08$$

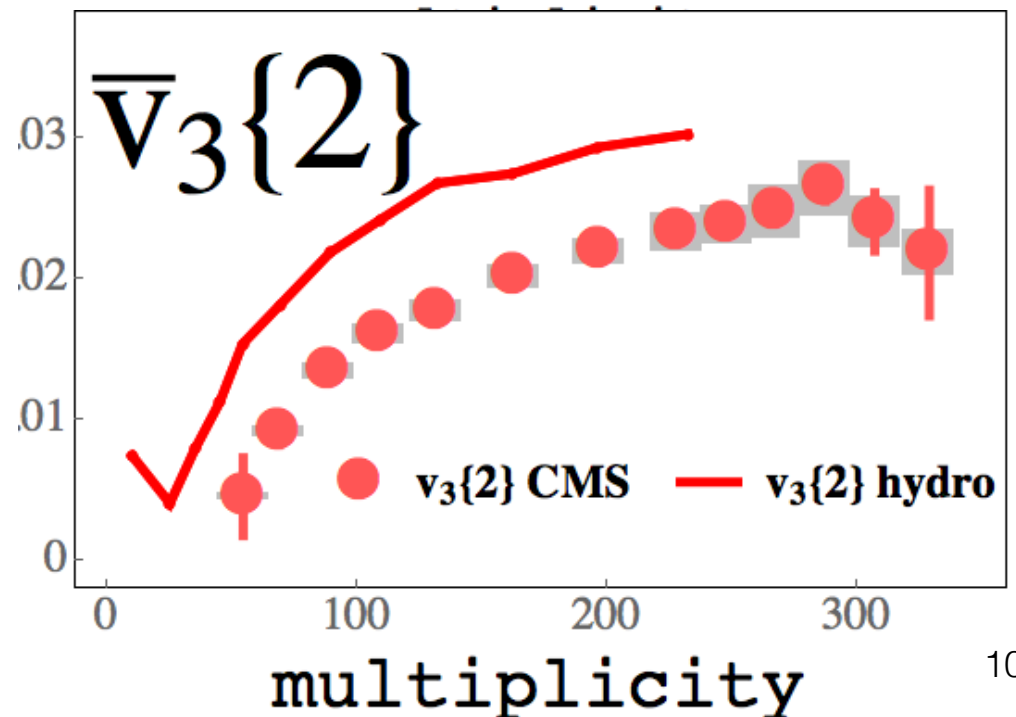
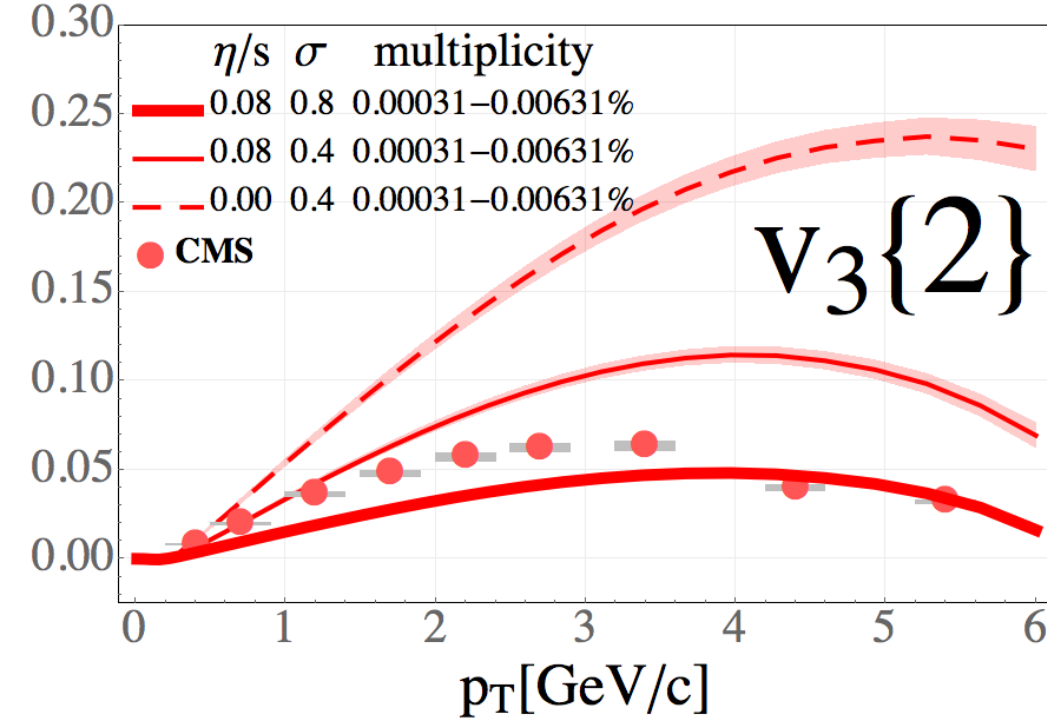
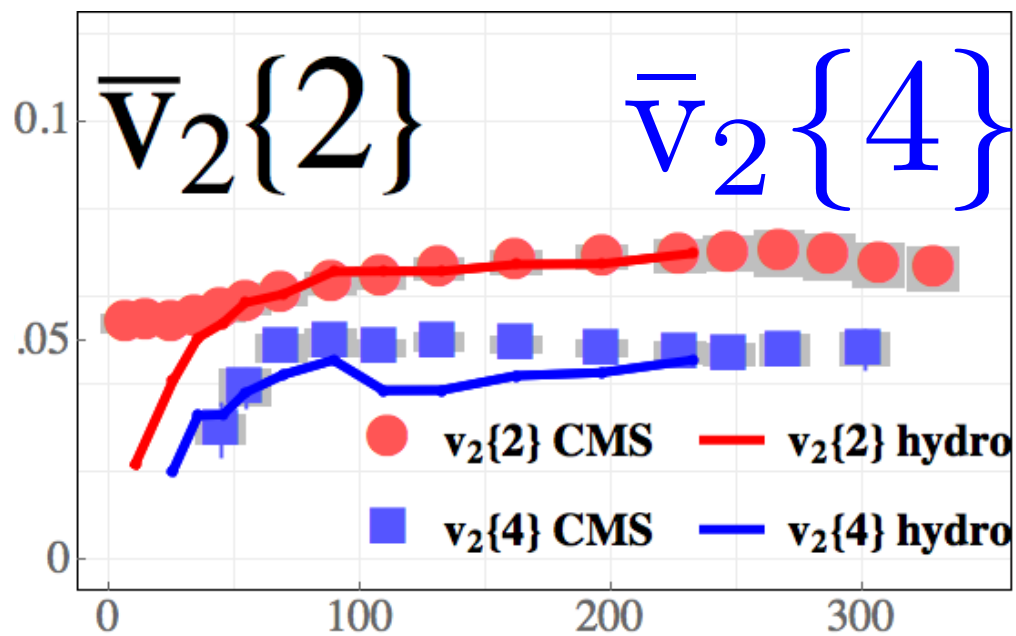
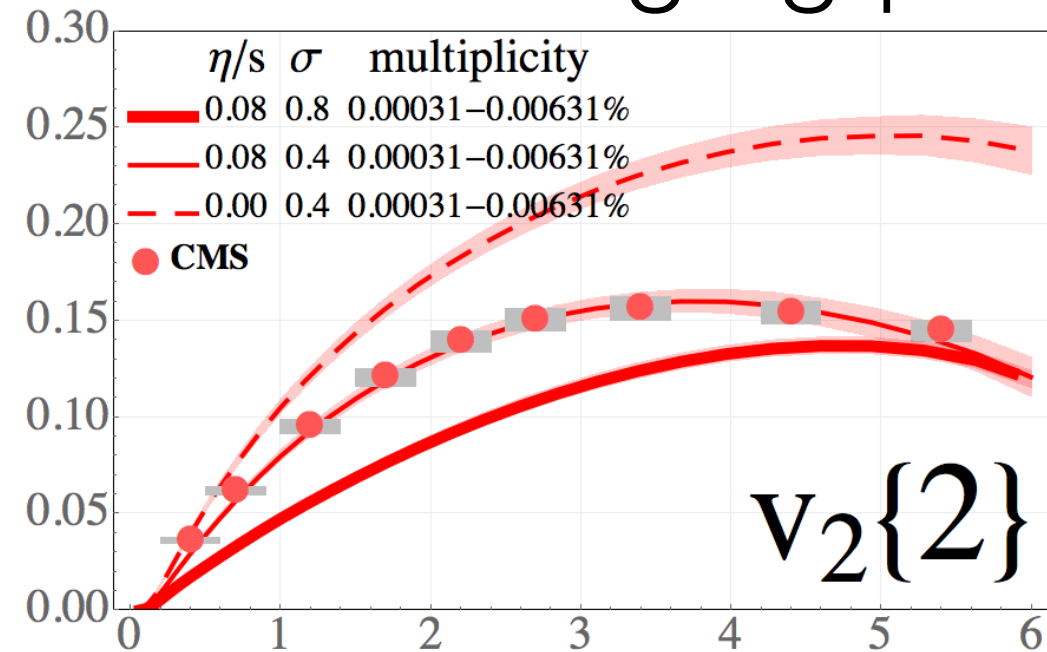
# **Comparing hydro calculations to existing pA data**

# pPb flow observables: CMS & hydro

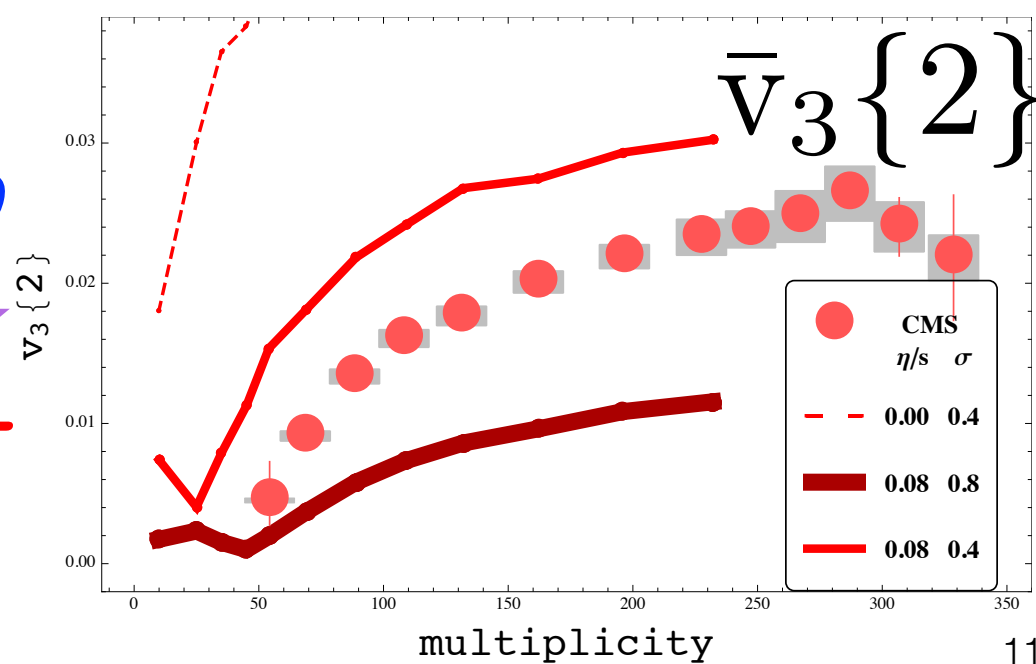
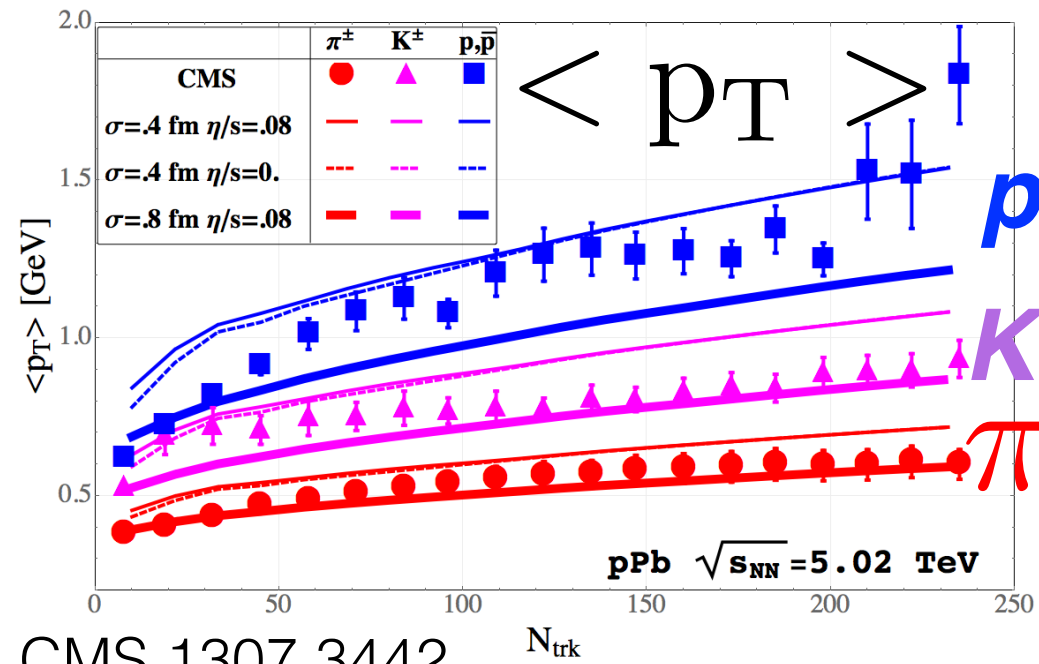
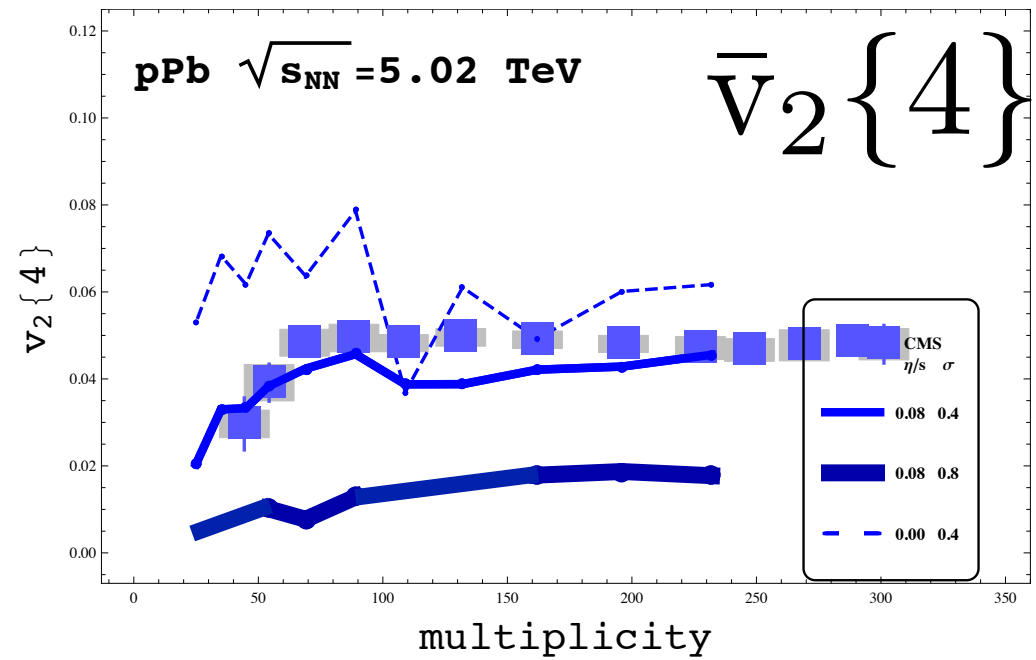
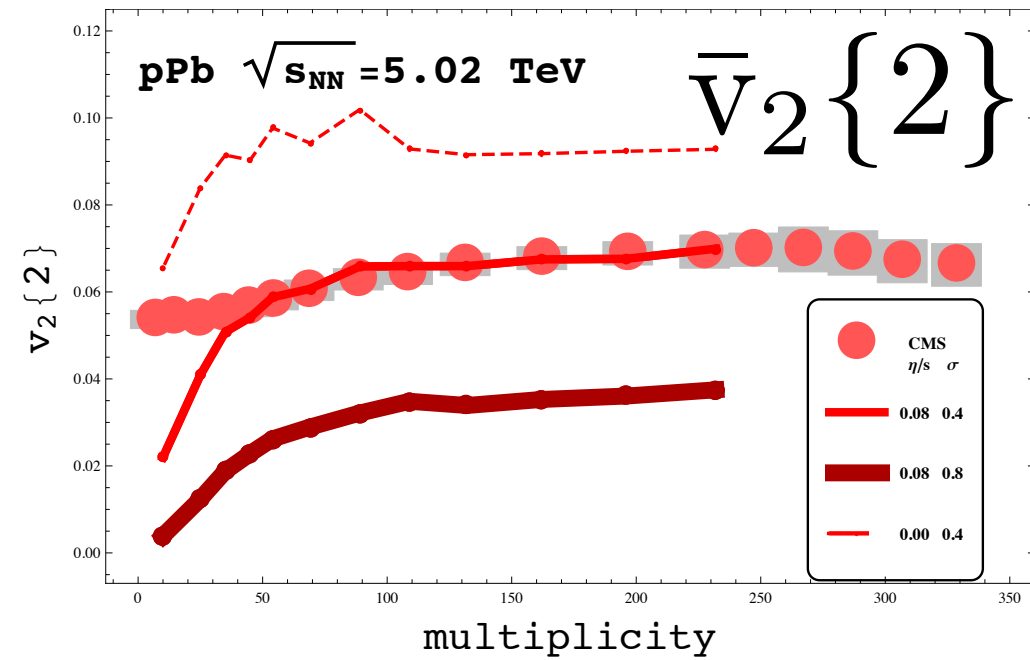




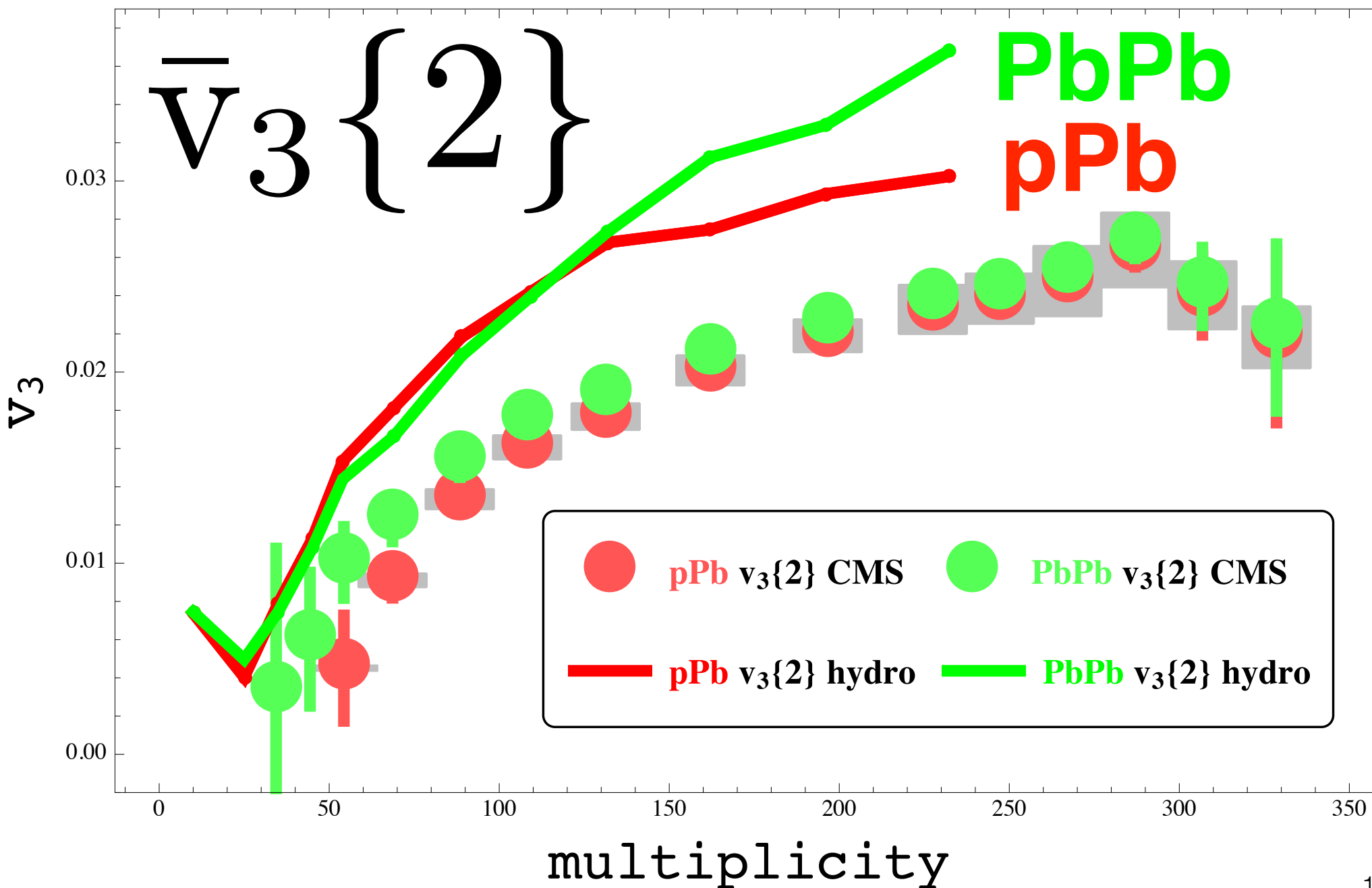
# Changing parameters $\sigma$ and $\eta/s$



# Flow observables dependence on $\sigma$ and $\eta/s$



# CMS finding in hydro



# All two-particle correlation observables

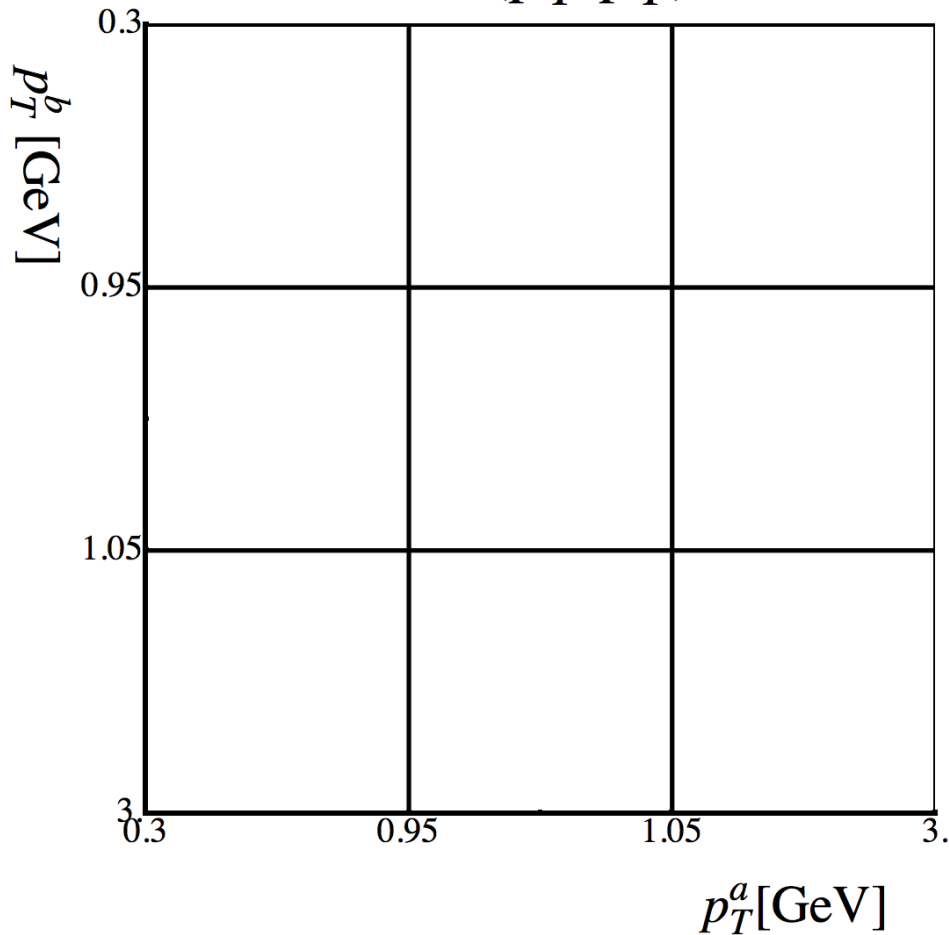
**theory:**

$$\frac{2\pi}{N} \frac{dN}{d\phi^a} = 1 + 2 \sum_{n=1}^{\infty} v_n(p_T^a) \cos n(\phi^a - \Psi_n)$$

**experiment:**

$$V_{n\Delta}(p_T^a, p_T^b) \equiv \overline{\langle \cos n(\phi^a - \phi^b) \rangle}$$

$V_{\Delta n}(p_T^a, p_T^b)$



# All two-particle correlation observables

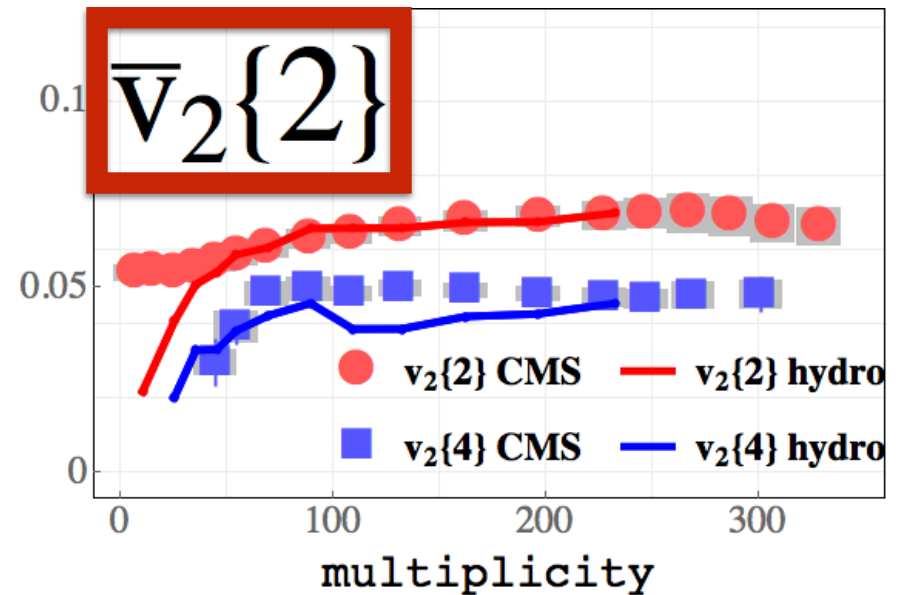
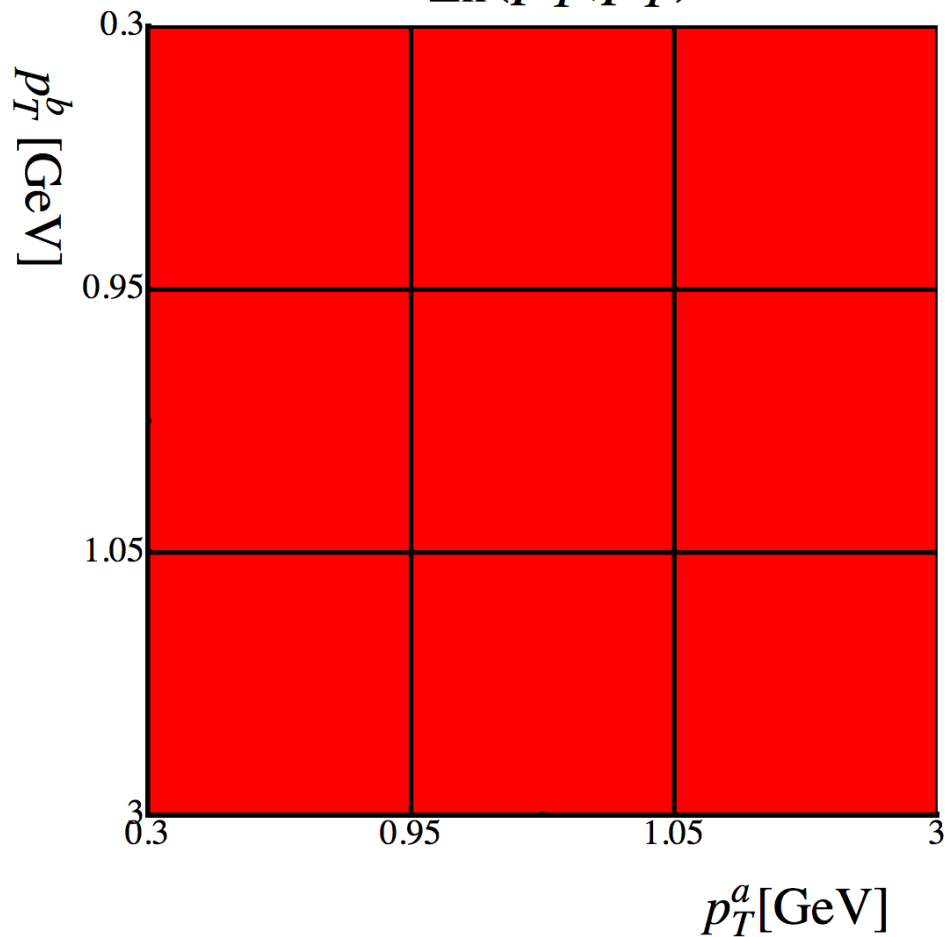
**theory:**

$$\frac{2\pi}{N} \frac{dN}{d\phi^a} = 1 + 2 \sum_{n=1}^{\infty} v_n(p_T^a) \cos n(\phi^a - \Psi_n)$$

**experiment:**

$$V_{n\Delta}(p_T^a, p_T^b) \equiv \langle \overline{\cos n(\phi^a - \phi^b)} \rangle$$

$$V_{\Delta n}(p_T^a, p_T^b)$$





# All two-particle correlation observables

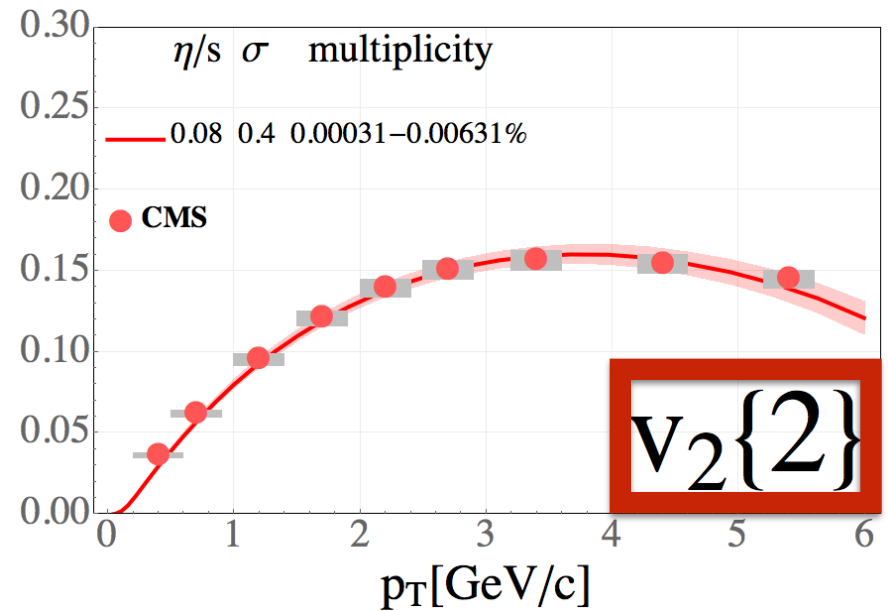
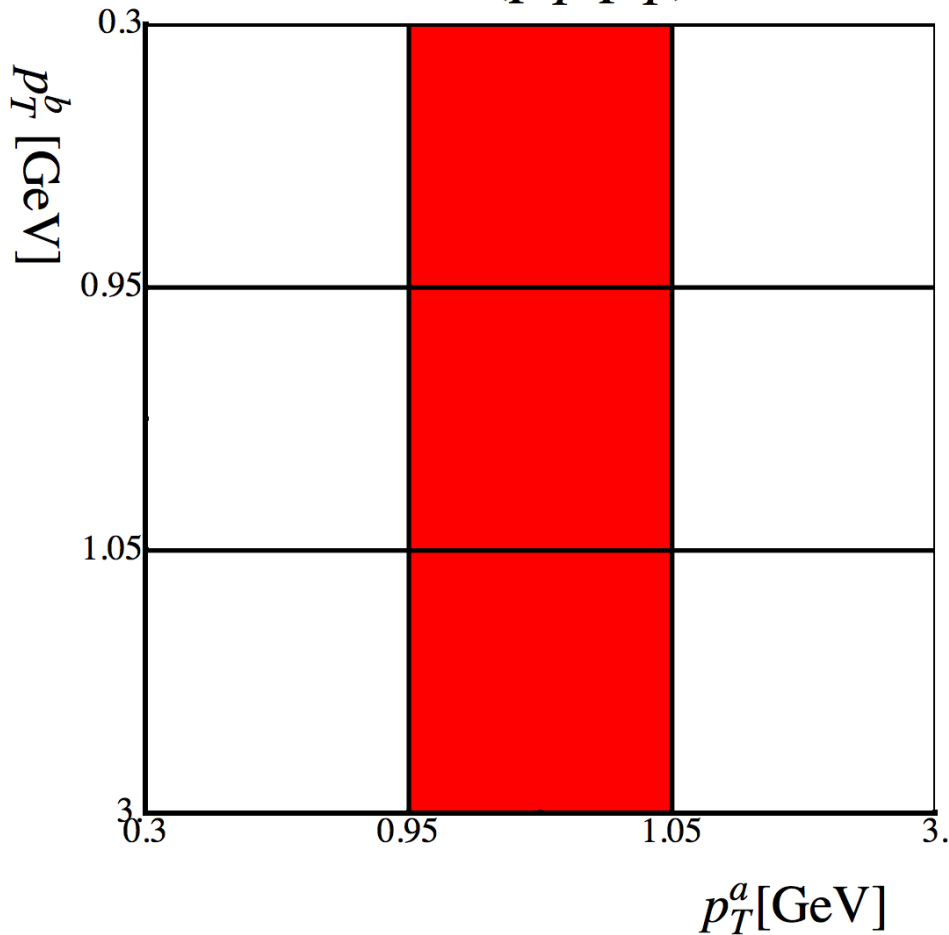
**theory:**

$$\frac{2\pi}{N} \frac{dN}{d\phi^a} = 1 + 2 \sum_{n=1}^{\infty} v_n(p_T^a) \cos n(\phi^a - \Psi_n)$$

**experiment:**

$$V_{n\Delta}(p_T^a, p_T^b) \equiv \overline{\langle \cos n(\phi^a - \phi^b) \rangle}$$

$$V_{\Delta n}(p_T^a, p_T^b)$$



# Two-particle correlation in hydro

**theory:**

$$\frac{2\pi}{N} \frac{dN}{d\phi^a} = 1 + 2 \sum_{n=1}^{\infty} v_n(p_T^a) \cos n(\phi^a - \Psi_n)$$

**experiment:**

$$V_{n\Delta}(p_T^a, p_T^b) \equiv \overline{\langle \cos n(\phi^a - \phi^b) \rangle}$$

Abs  $|r_n|$

$p_T^b$  [GeV]

= 1	$\leq 1$	$\leq 1$
$\leq 1$	= 1	$\leq 1$
$\leq 1$	$\leq 1$	= 1

$p_T^a$  [GeV]

$$r_n \equiv \frac{V_{n\Delta}(p_T^a, p_T^b)}{\sqrt{V_{n\Delta}(p_T^a, p_T^a) V_{n\Delta}(p_T^b, p_T^b)}}$$

**hydro:**

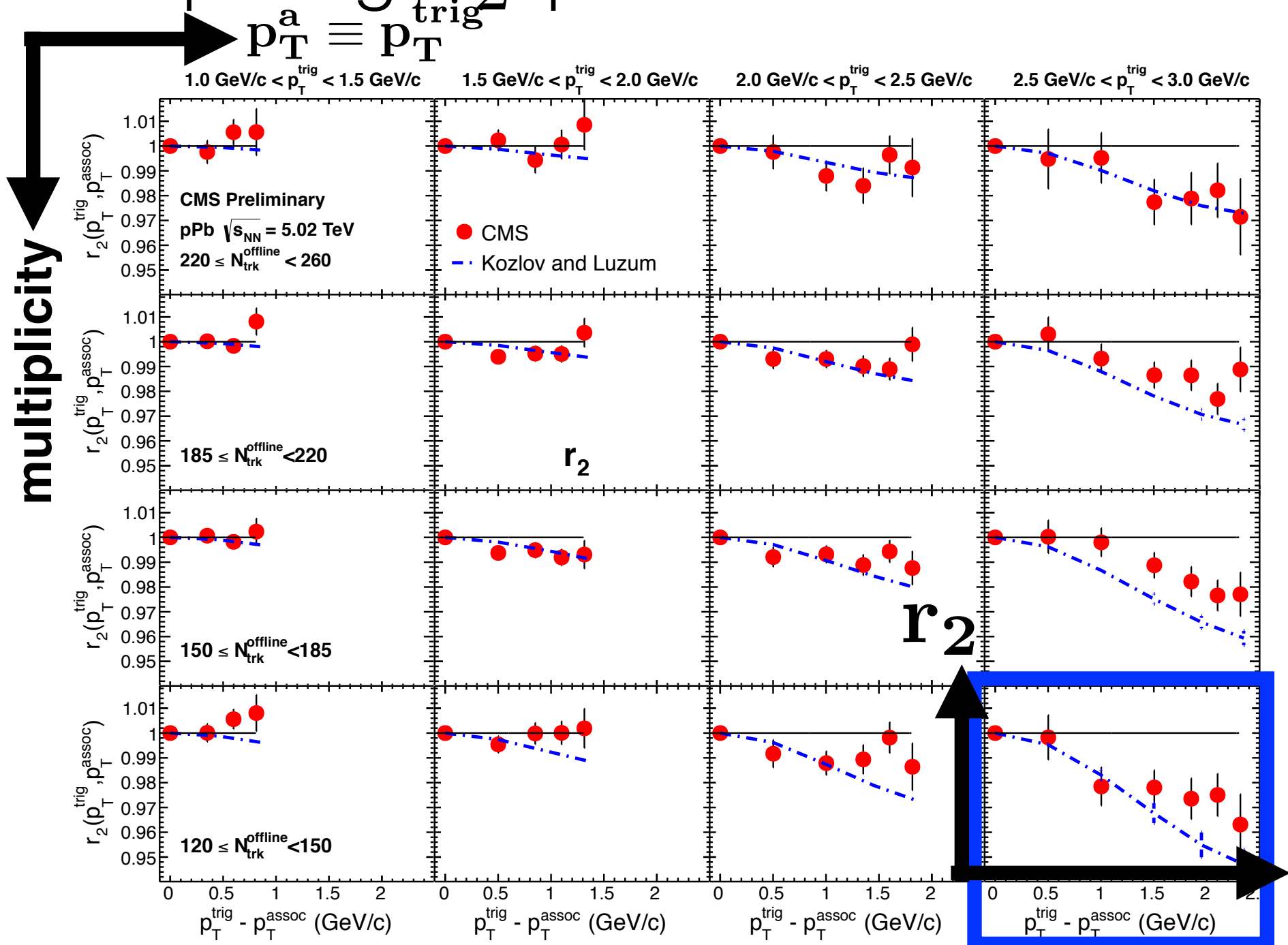
$$\frac{dN_{pairs}}{d^3p^a d^3p^b} \stackrel{\text{(flow)}}{=} \frac{dN}{d^3p^a} \times \frac{dN}{d^3p^b}$$

$$V_{n\Delta}(p_T^a, p_T^a) \geq 0$$

$$V_{n\Delta}(p_T^a, p_T^b)^2 \leq$$

$$V_{n\Delta}(p_T^a, p_T^a) V_{n\Delta}(p_T^b, p_T^b)$$

# Comparing $r_2$ predictions to CMS data



Devetak for CMS QM 2014

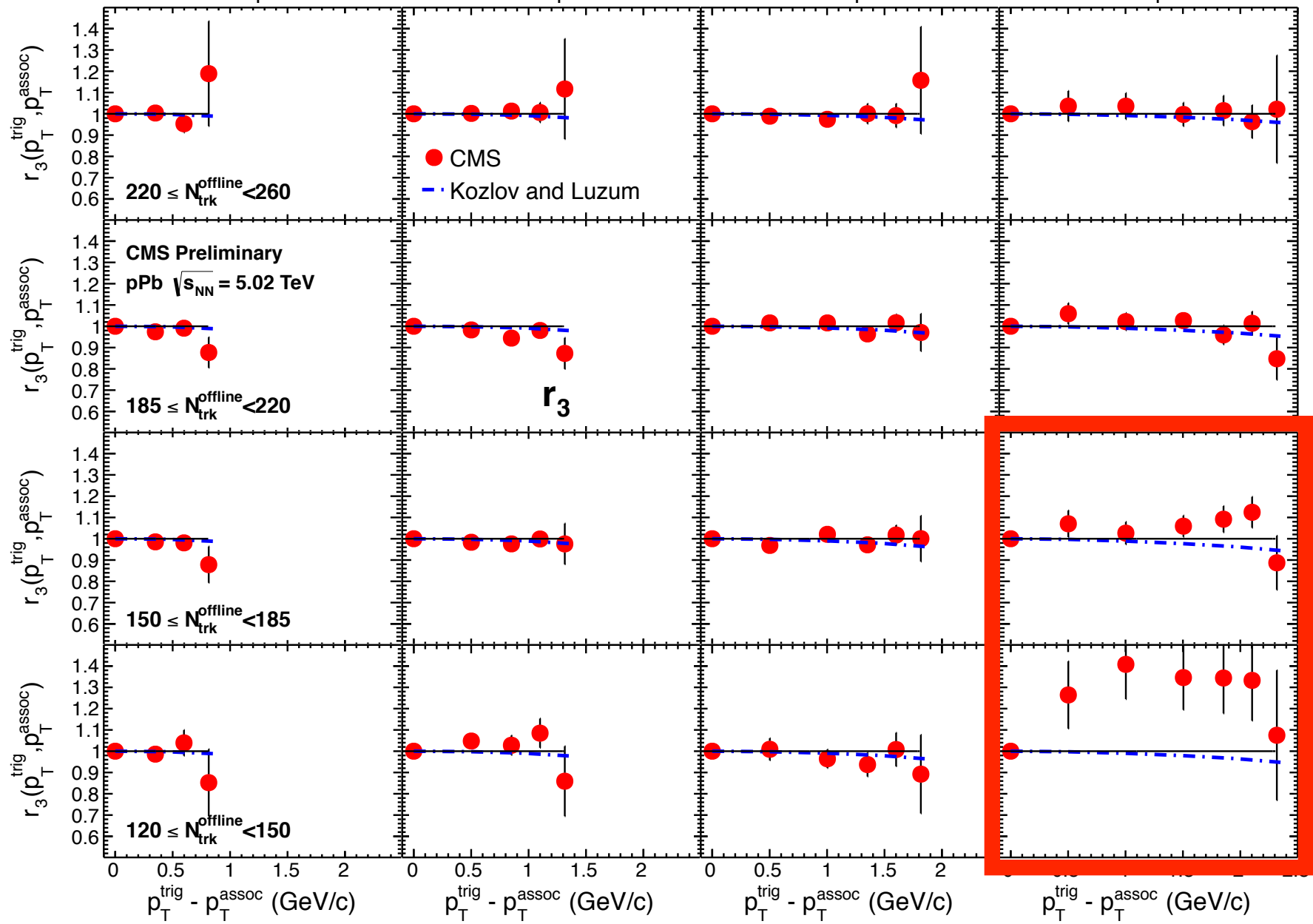
$p_T^b$

# Comparing $r_3$ predictions to CMS data

multiplicity

$p_T^a \equiv p_T^{\text{trig}}$

$1.0 \text{ GeV/c} < p_T^{\text{trig}} < 1.5 \text{ GeV/c}$    
  $1.5 \text{ GeV/c} < p_T^{\text{trig}} < 2.0 \text{ GeV/c}$    
  $2.0 \text{ GeV/c} < p_T^{\text{trig}} < 2.5 \text{ GeV/c}$    
  $2.5 \text{ GeV/c} < p_T^{\text{trig}} < 3.0 \text{ GeV/c}$



Devetak for CMS QM 2014

$p_T^b$   
 18

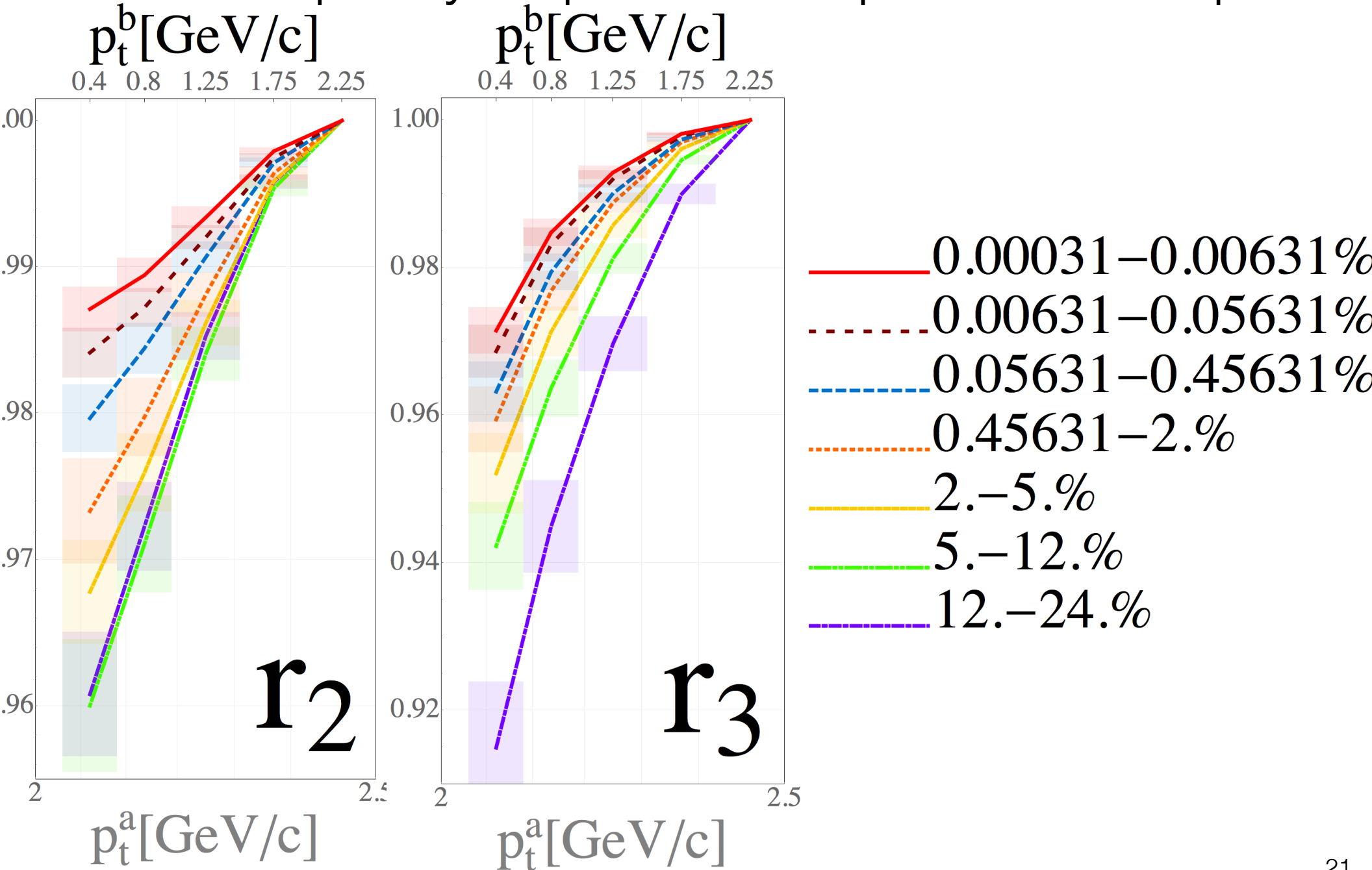
# Section conclusions

- Hydrodynamics can reasonably describe a wide range of flow observables for pPb system at high multiplicity  $v_2\{2\}$ ,  $v_3\{2\}$ ,  $v_2\{4\}$  and  $r_n$

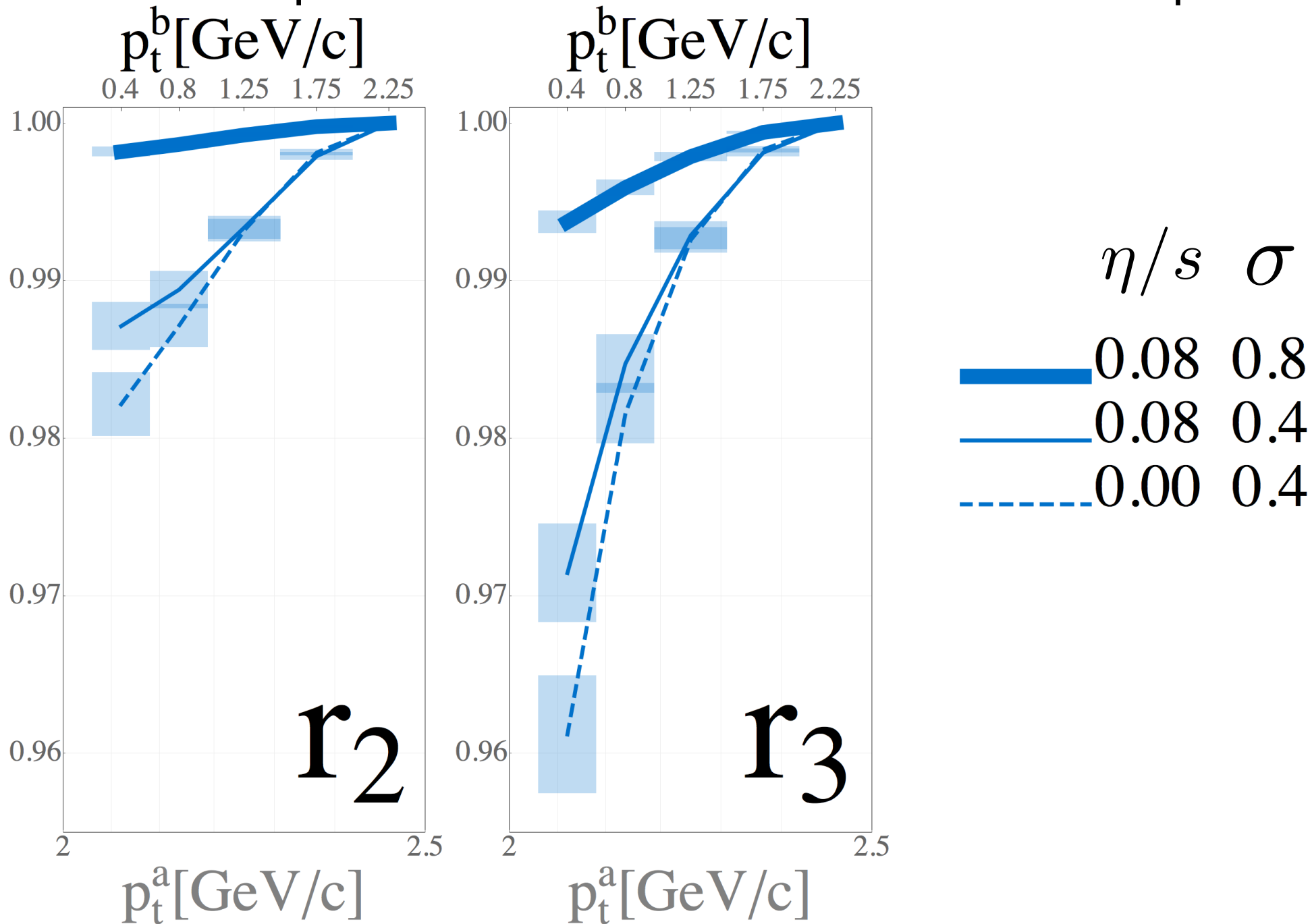


# **Another handle to study HIC**

# multiplicity dependence prediction in pPb



# $r_n$ dependence on $\sigma$ and $\eta/s$ in pPb



$r_n$  dependence on  $\sigma$  and  $\eta/s$  in pPb

$p_t^b$  [GeV/c]

0.4 0.8 1.25 1.75 2.25

$p_t^b$  [GeV/c]

0.4 0.8 1.25 1.75 2.25

$r_n$  is sensitive to  
transverse granularity

$\eta/s$   $\sigma$

0.08 0.8

0.08 0.4

0.00 0.4

$r_2$

$r_3$

2

2.5

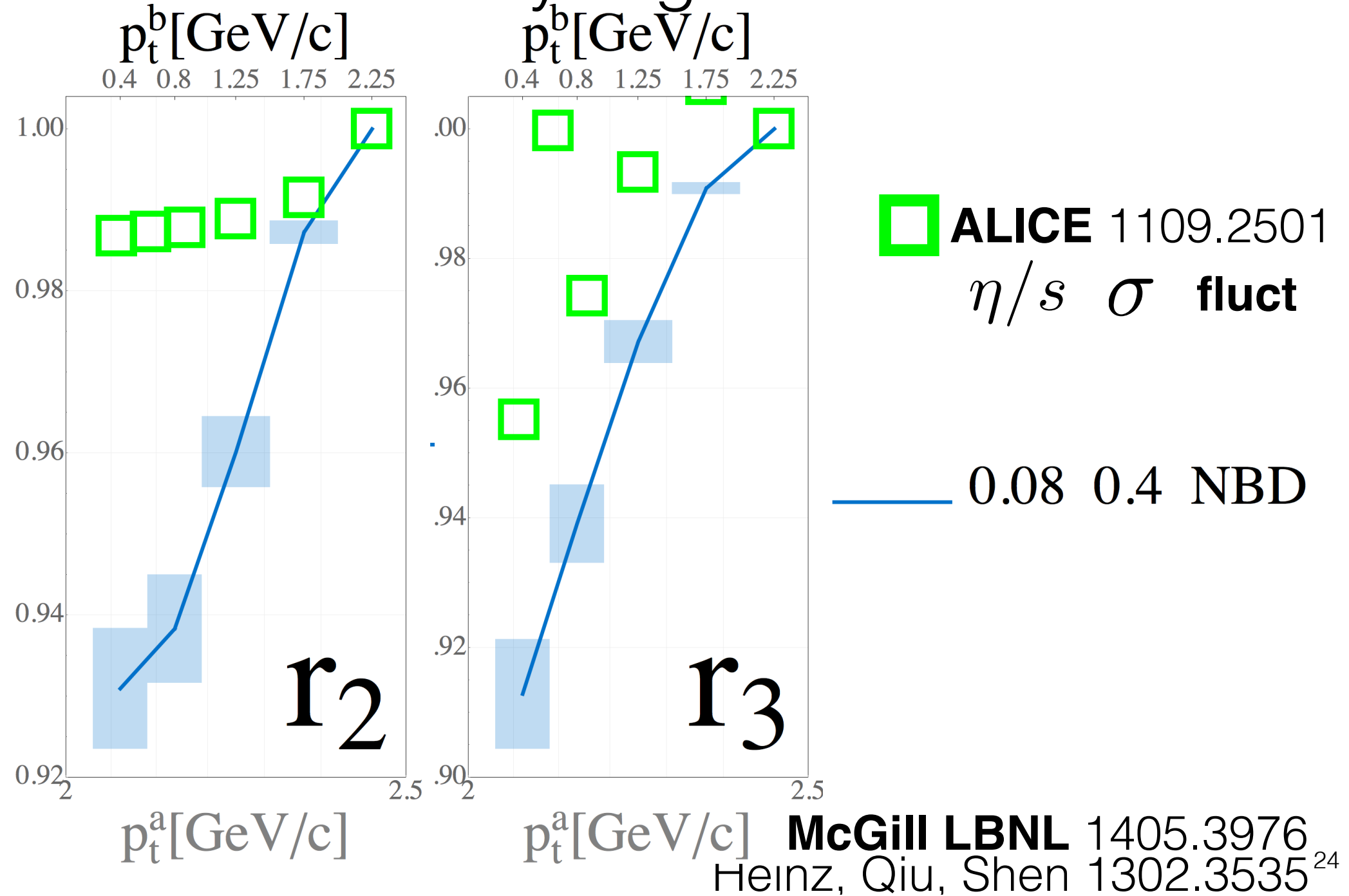
2

2.5

$p_t^a$  [GeV/c]

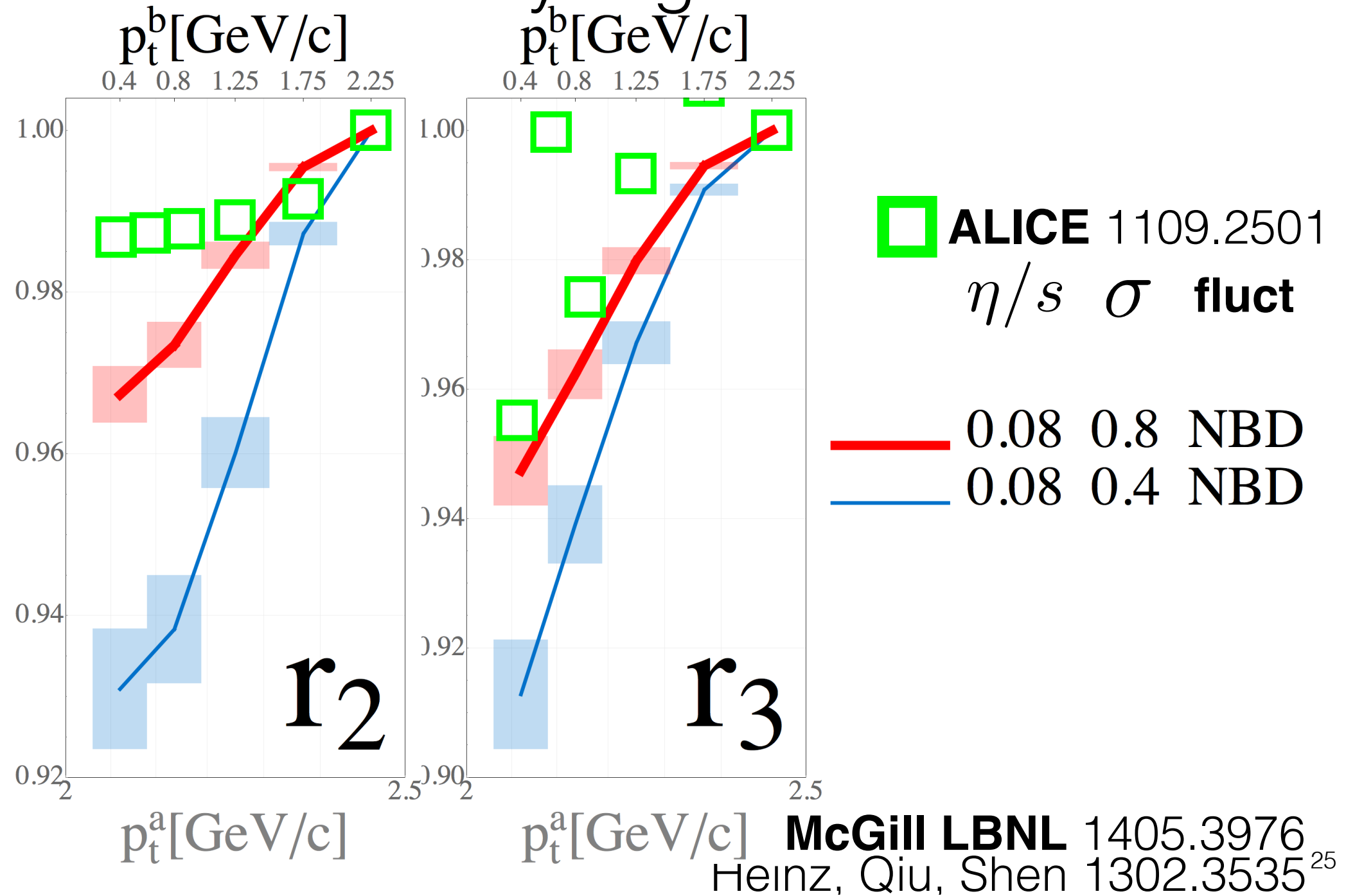
$p_t^a$  [GeV/c]

# Reanalyzing PbPb data

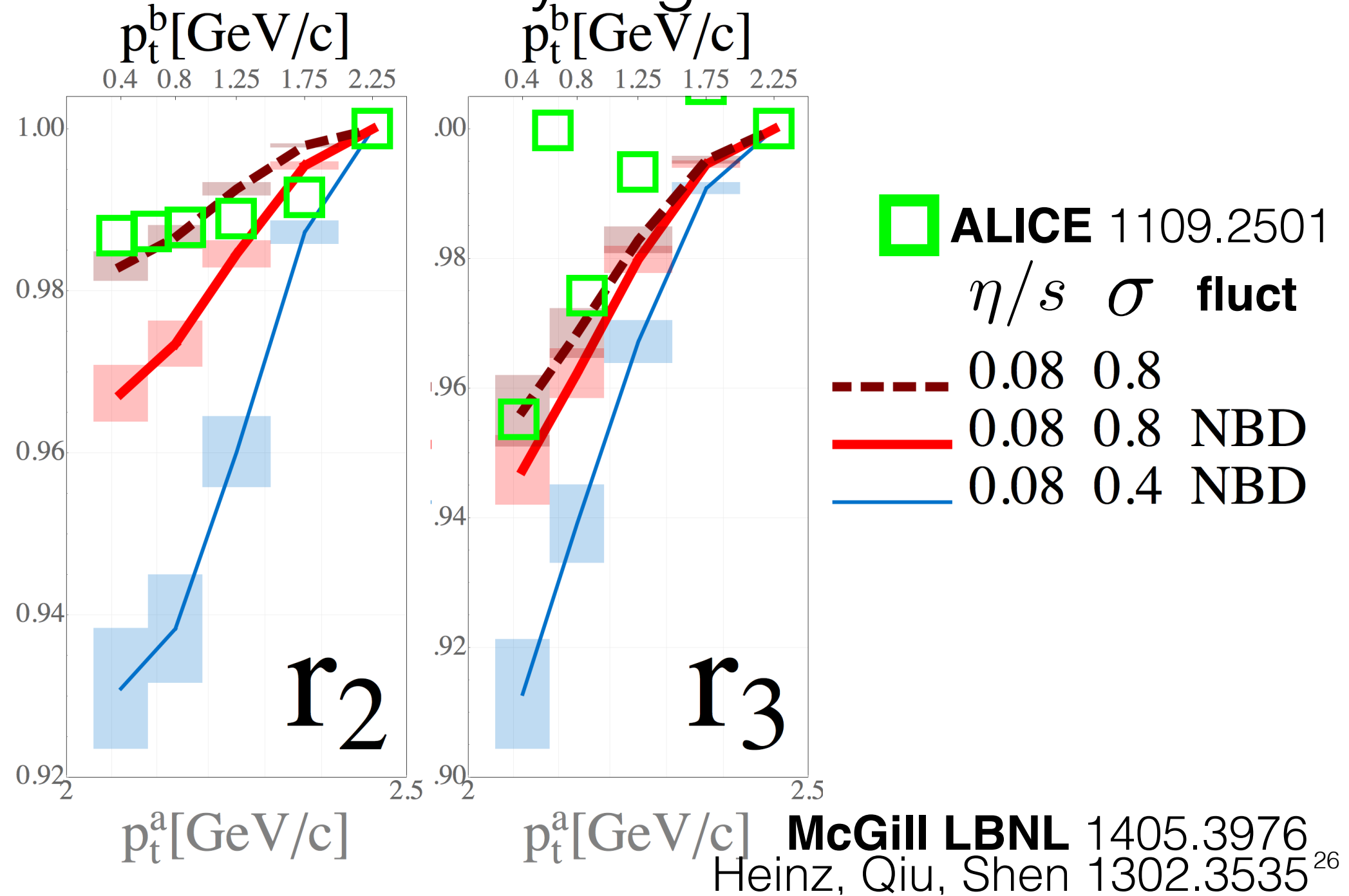




# Reanalyzing PbPb data



# Reanalyzing PbPb data

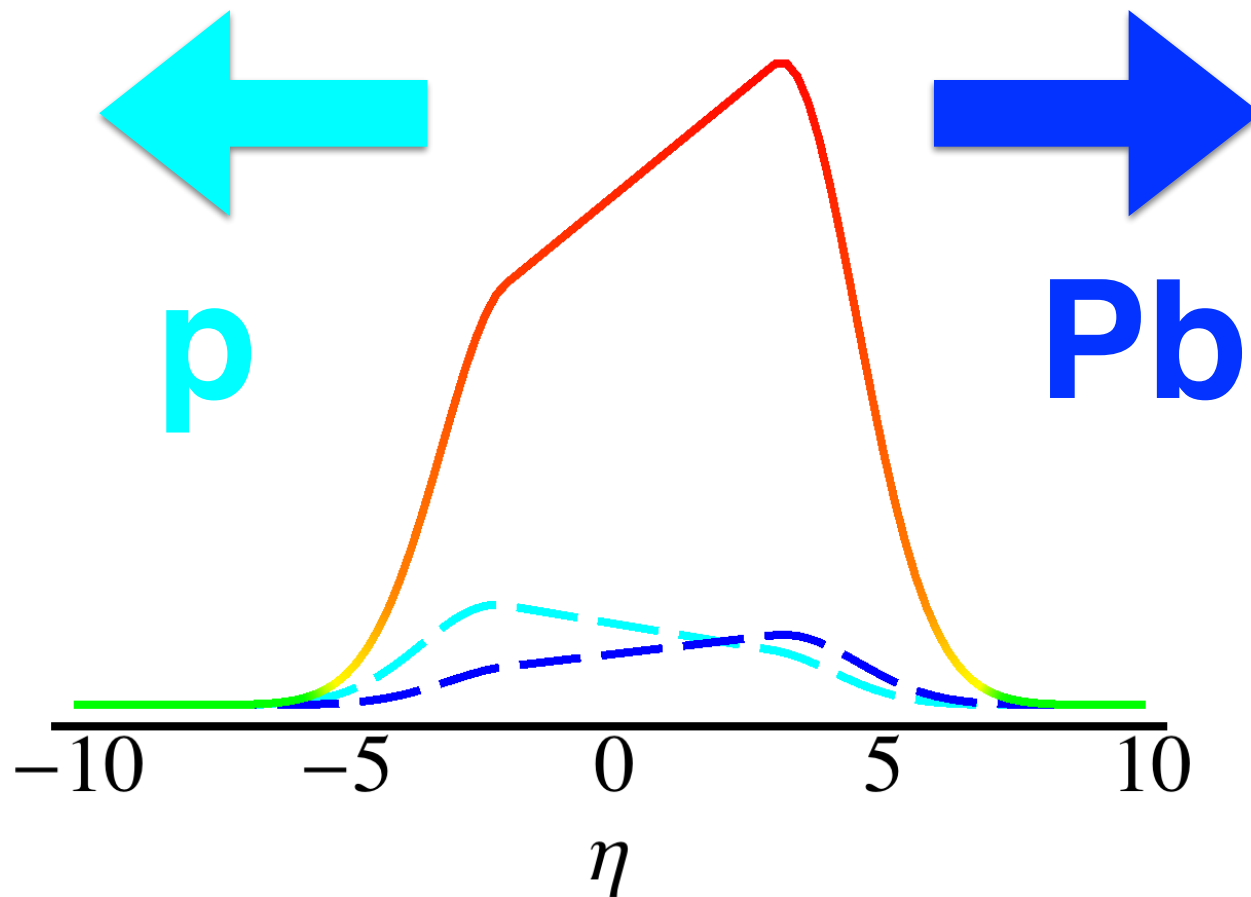


# Conclusion

- Hydrodynamics can reasonably describe a wide range of flow observables for pPb system at high multiplicity  $v_2\{2\}$ ,  $v_3\{2\}$ ,  $v_2\{4\}$  and  $r_n$
- $r_n$  predictions provide another handle to explore HIC
  - ▶ it tells us where hydro breaks down
  - ▶ a way to probe initial conditions (granularity)
  - ▶ a way to study differences between pA and AA

# Backup

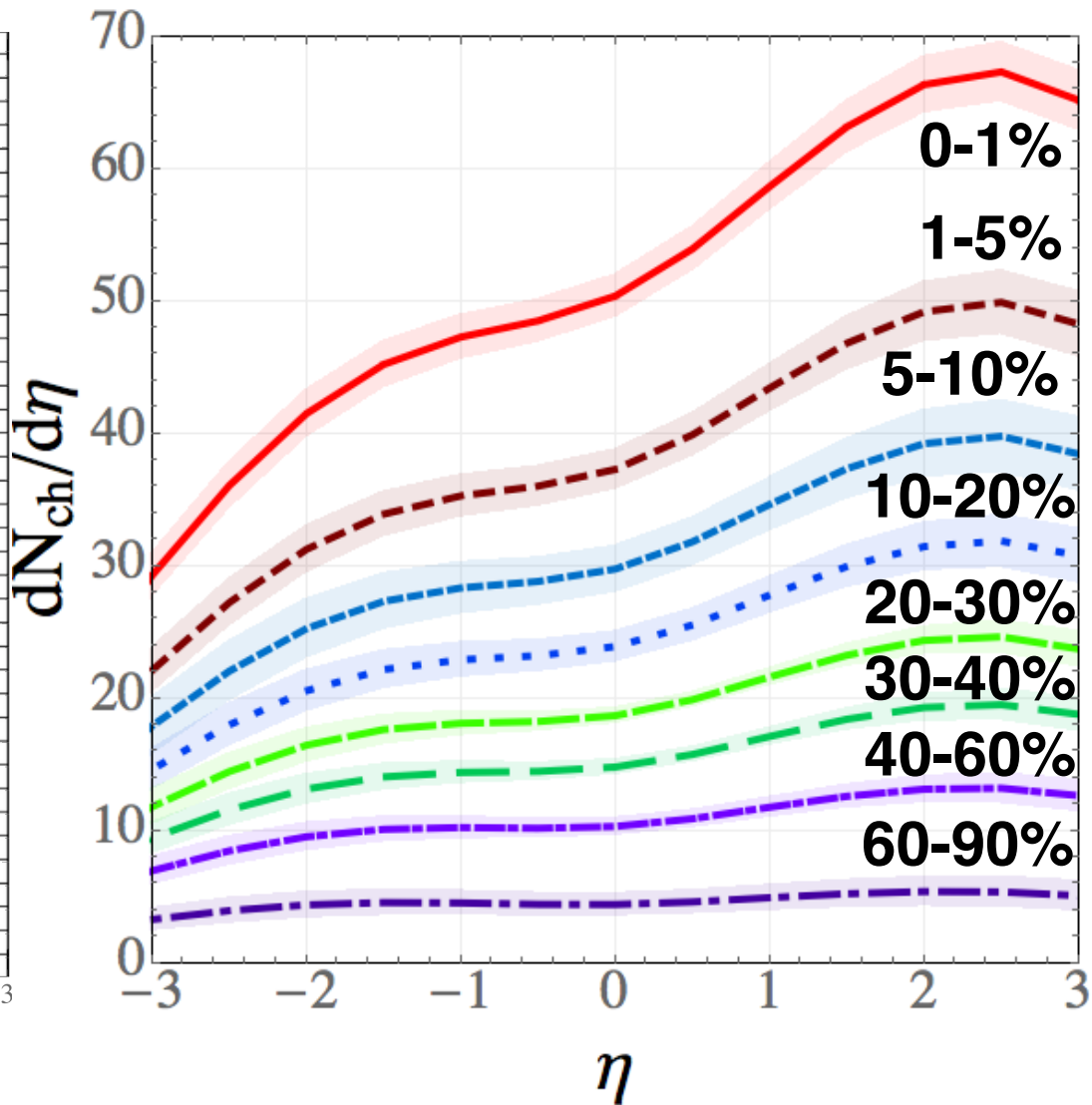
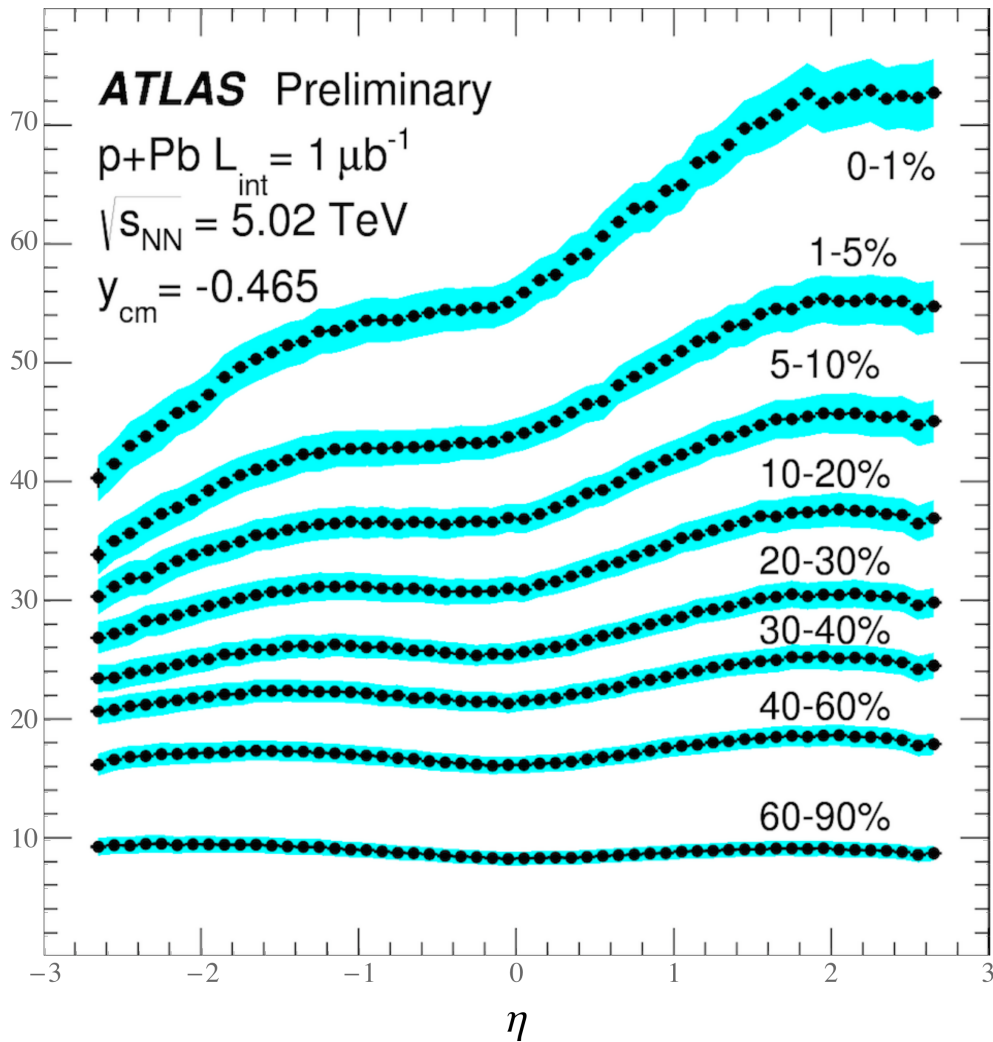
# Initial conditions: longitudinal profile



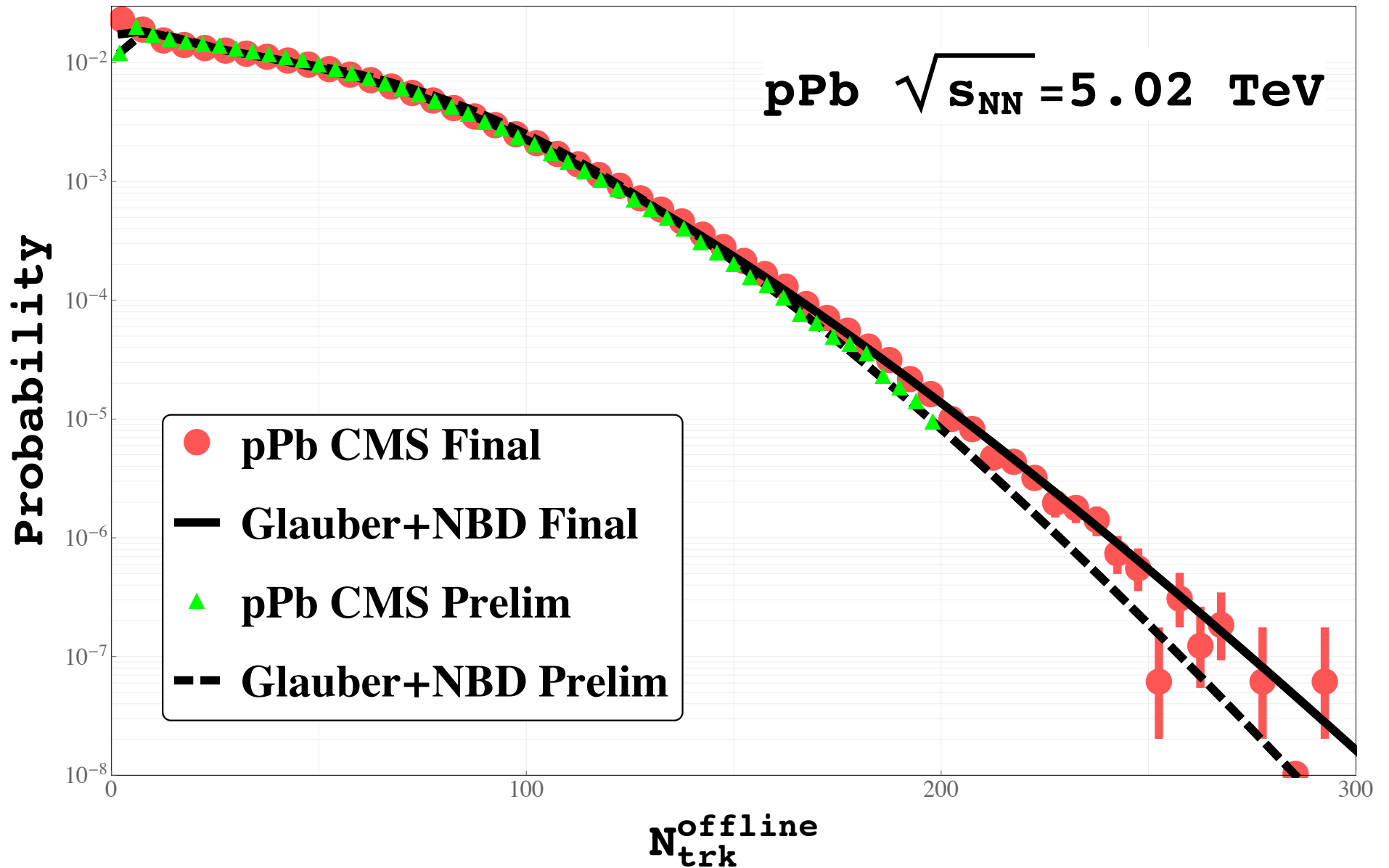
$$\left(1 + \frac{\eta}{y_{\text{beam}}}\right) \exp\left(-\frac{(|\eta| - \eta_0)^2}{2\sigma_\eta^2} \theta(|\eta| - \eta_0)\right)$$

# Pseudorapidity distribution

ATLAS arXiv/1403.5738

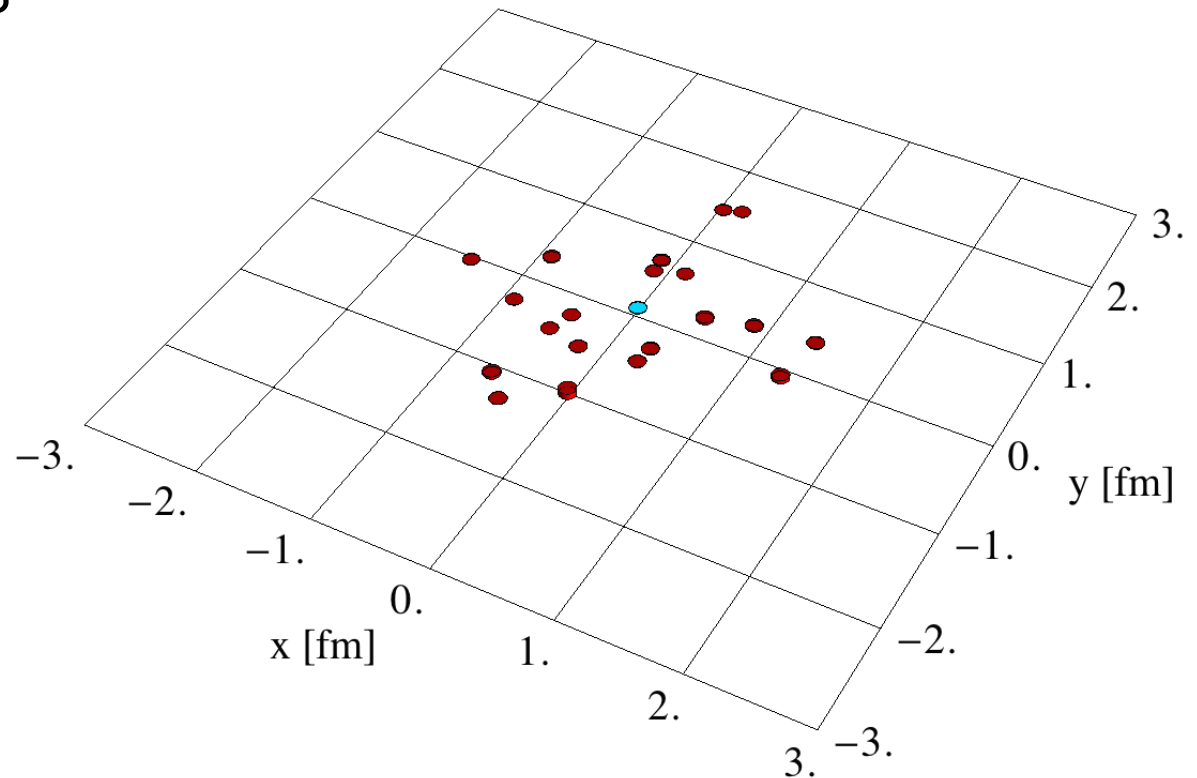


# Initial conditions: Glauber+NBD



# Initial conditions: Glauber

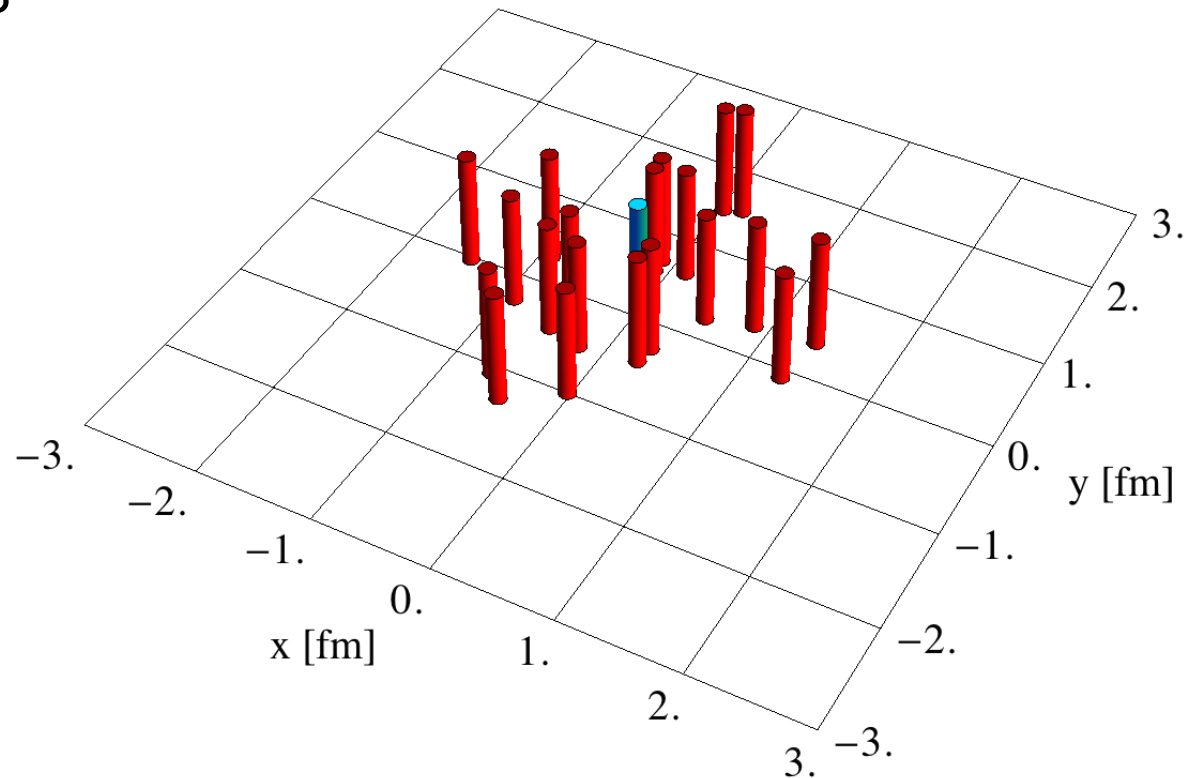
- sample participants





# Initial conditions: Glauber

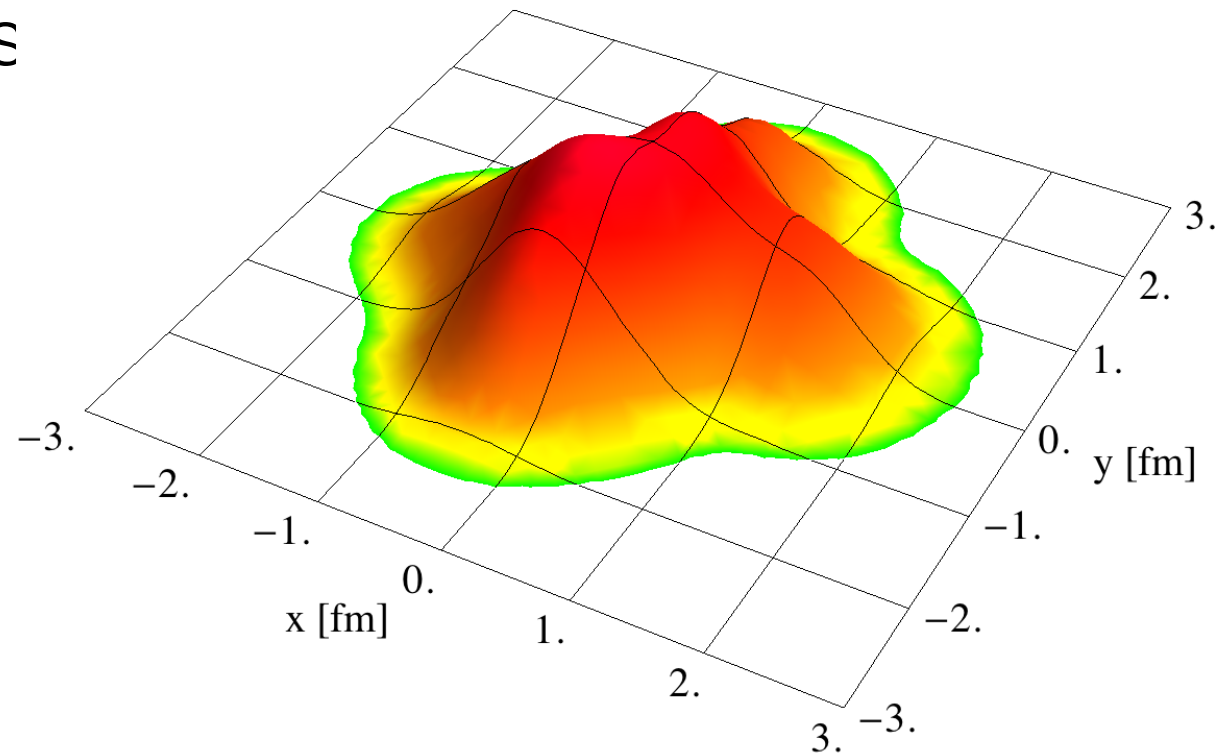
- sample participants
- add sources



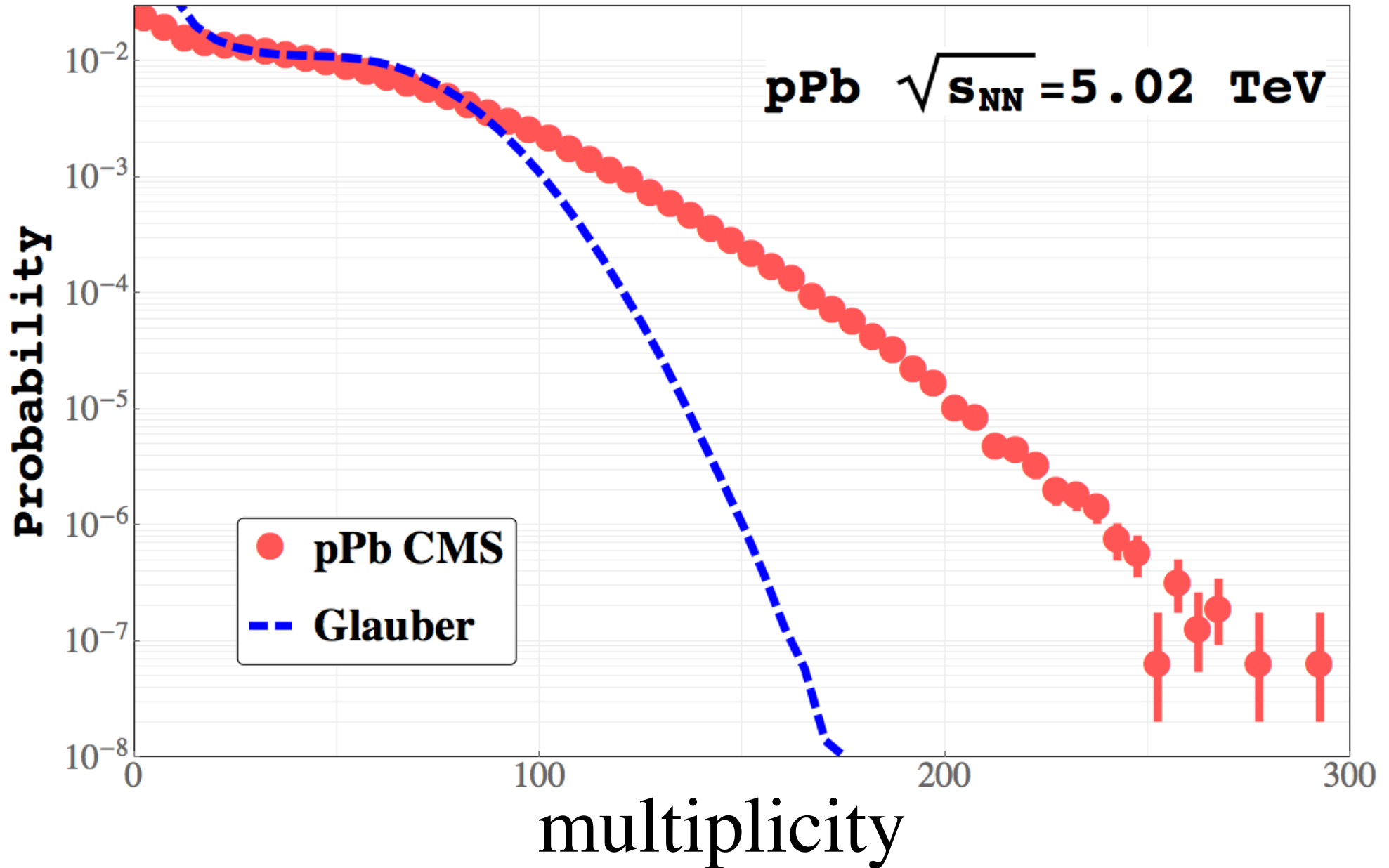
# Initial conditions: Glauber

$$\sigma = 0.40 \text{ fm}$$

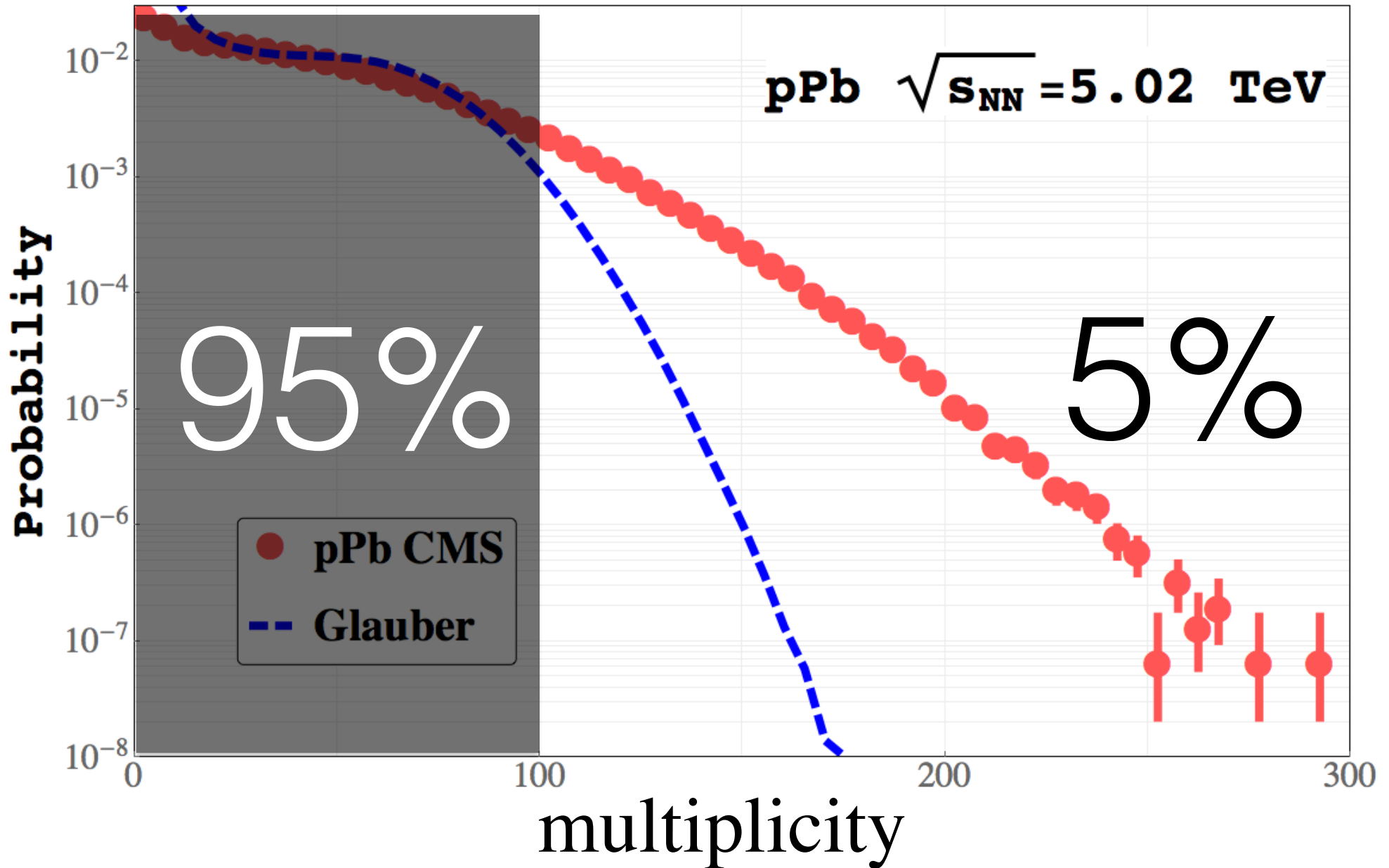
- sample participants
- add sources
- increase  $\sigma$



# Glauber+NBD

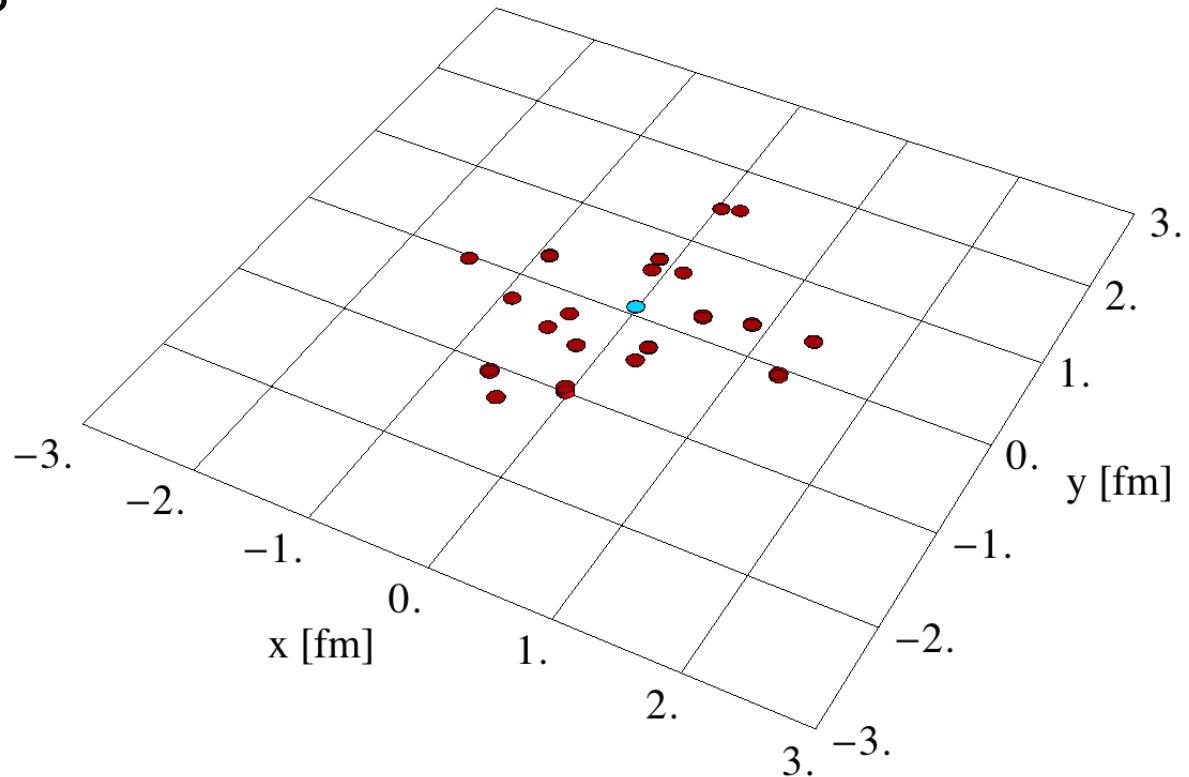


# Glauber+NBD



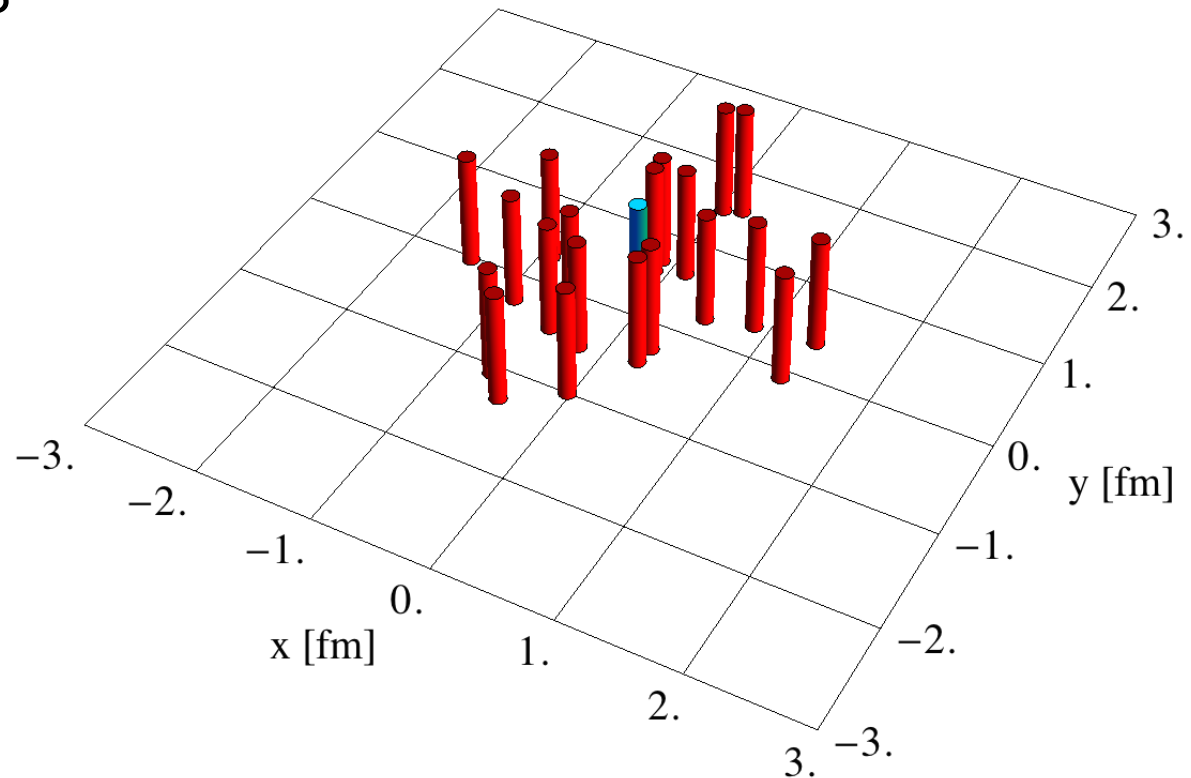
# Initial conditions: Glauber+NBD

- sample participants



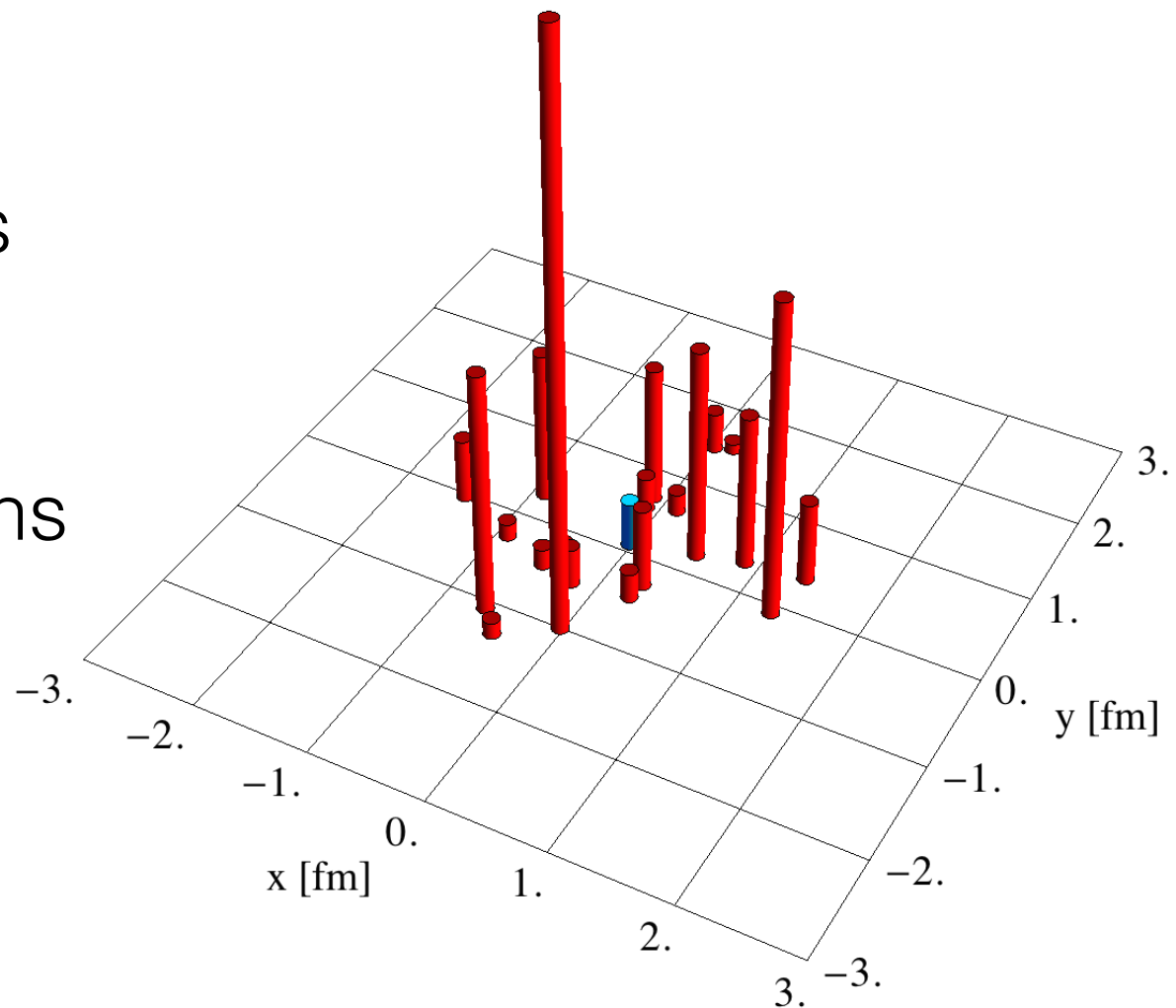
# Initial conditions: Glauber+NBD

- sample participants
- add sources



# Initial conditions: Glauber+NBD

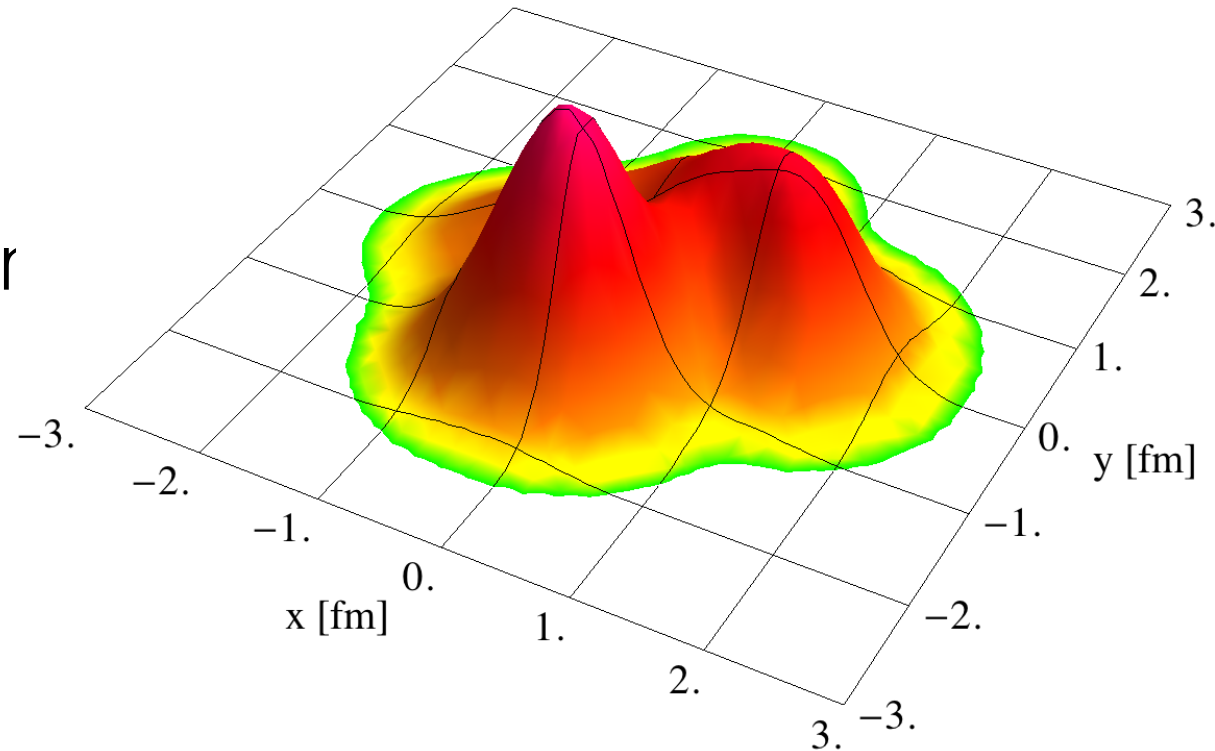
- sample participants
- add sources
- add NBD fluctuations



# Initial conditions: Glauber+NBD

$$\sigma = 0.40 \text{ fm}$$

- sample participants
- add sources
- add NBD fluctuation
- increase  $\sigma$

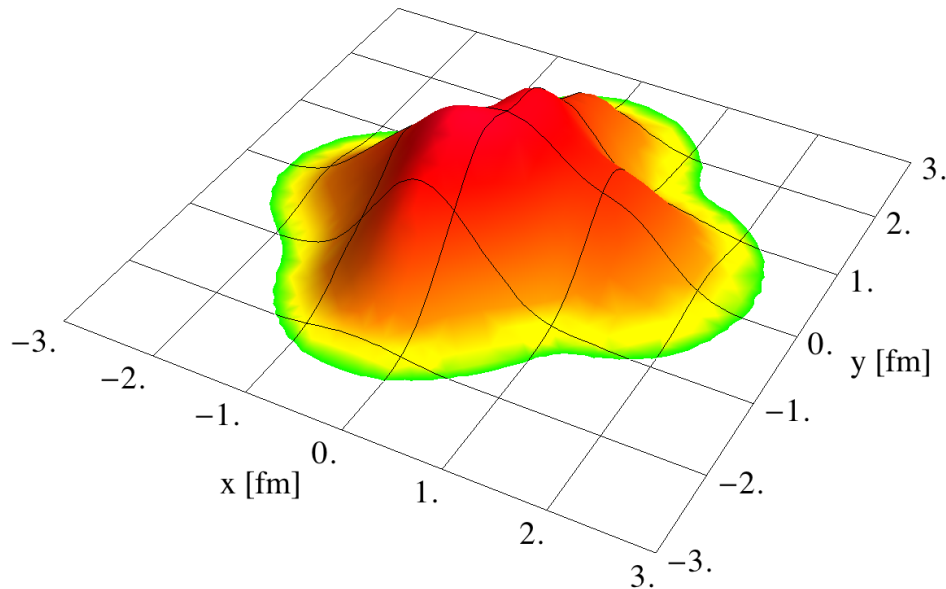




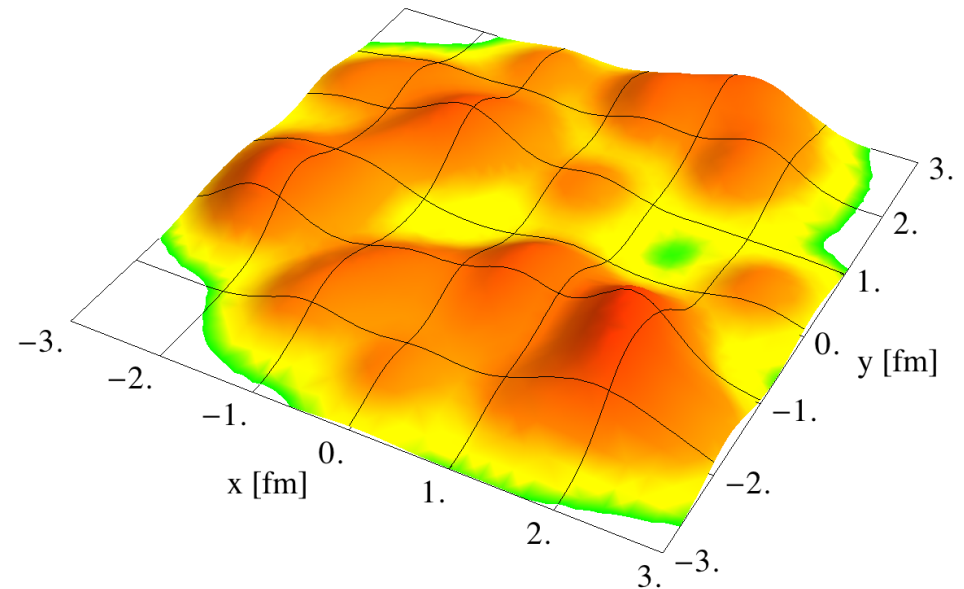
# Initial conditions: Glauber

$$\sigma = 0.40 \text{ fm}$$

$$\sigma = 0.40 \text{ fm}$$



pPb

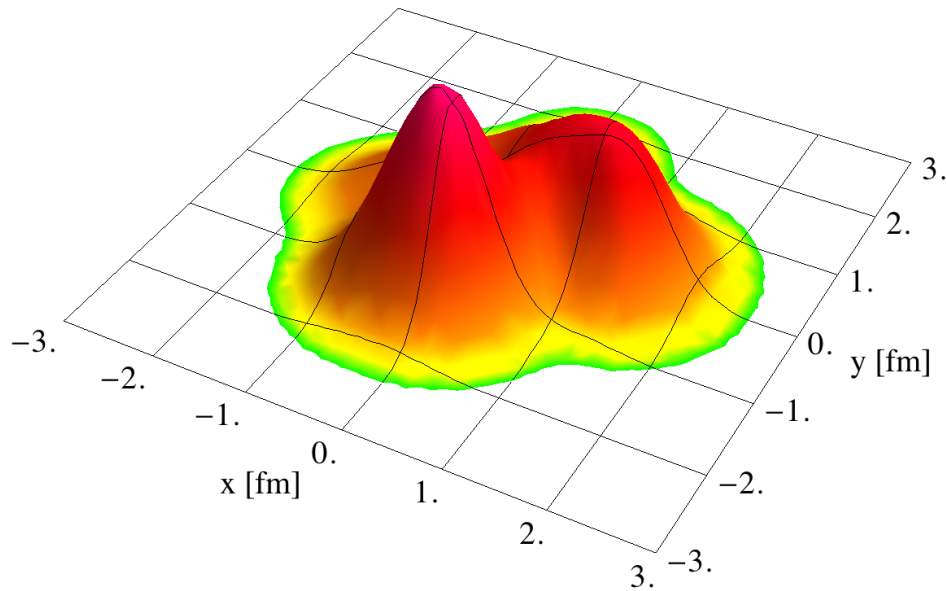


PbPb

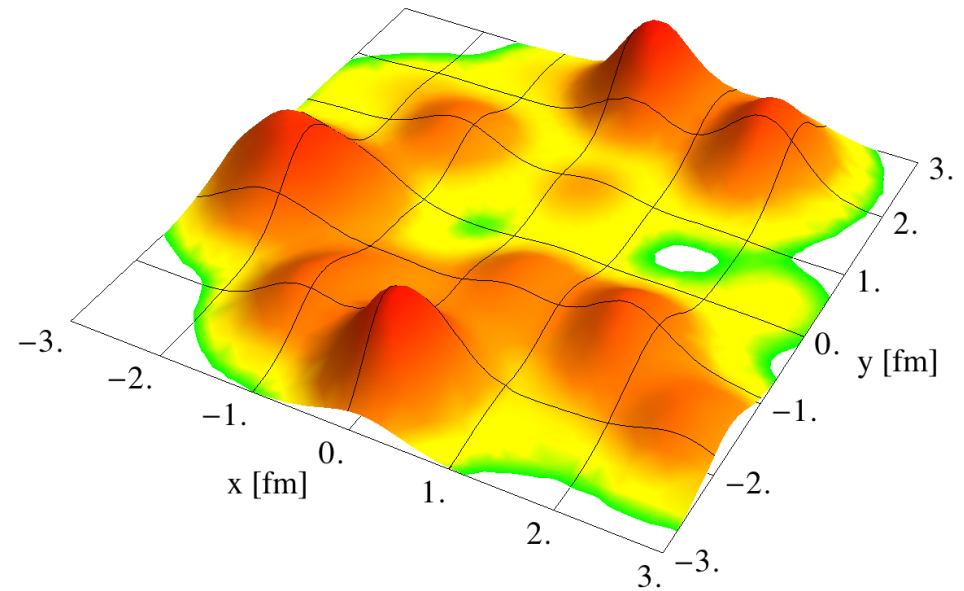
# Initial conditions: Glauber+NBD

$$\sigma = 0.40 \text{ fm}$$

$$\sigma = 0.40 \text{ fm}$$

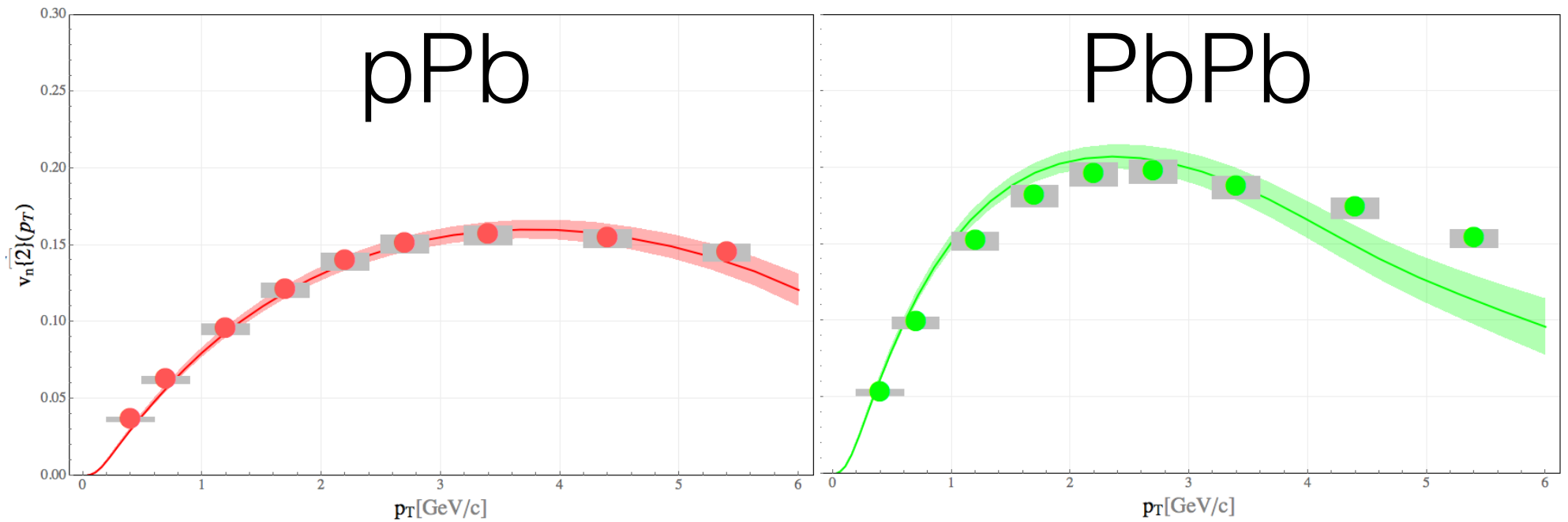


pPb

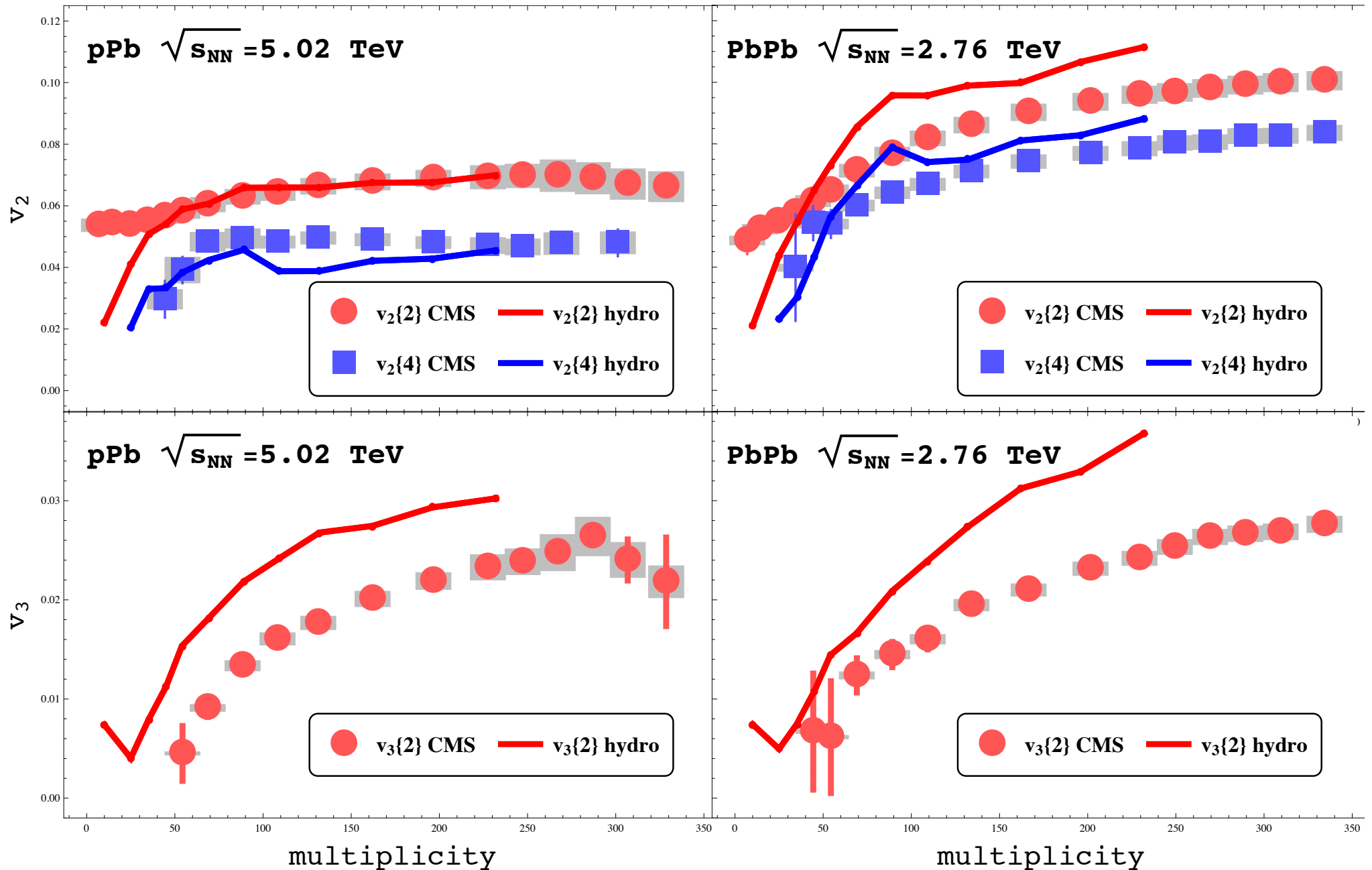


PbPb

# Flow observables for pPb and PbPb



# Flow observables for pPb and PbPb



## experiment:

$$V_{n\Delta}(p_T^a, p_T^b) \equiv \overline{\langle \cos n(\phi^a - \phi^b) \rangle}$$

$$r_n \equiv \frac{V_{n\Delta}(p_T^a, p_T^b)}{\sqrt{V_{n\Delta}(p_T^a, p_T^a)V_{n\Delta}(p_T^b, p_T^b)}}$$

$$\frac{dN_{pairs}}{d^3p^a d^3p^b} \stackrel{\text{(flow)}}{=} \frac{dN}{d^3p^a} \times \frac{dN}{d^3p^b}$$

$$\overline{\langle e^{in(\phi^a - \phi^b)} \rangle} = \overline{\langle e^{in\phi^a} \cdot e^{-in\phi^b} \rangle}$$

$$v_n^a e^{in\Psi_n^a} \equiv \overline{e^{in\phi^a}}$$

$$V_{n\Delta}^{ab}(p_T^a, p_T^b) = \langle v_n^a v_n^b e^{in(\Psi_n^a - \Psi_n^b)} \rangle$$

$$V_{n\Delta}(p_T^a, p_T^a) \geq 0$$

$$V_{n\Delta}(p_T^a, p_T^b)^2 \leq V_{n\Delta}(p_T^a, p_T^a)V_{n\Delta}(p_T^b, p_T^b)$$