

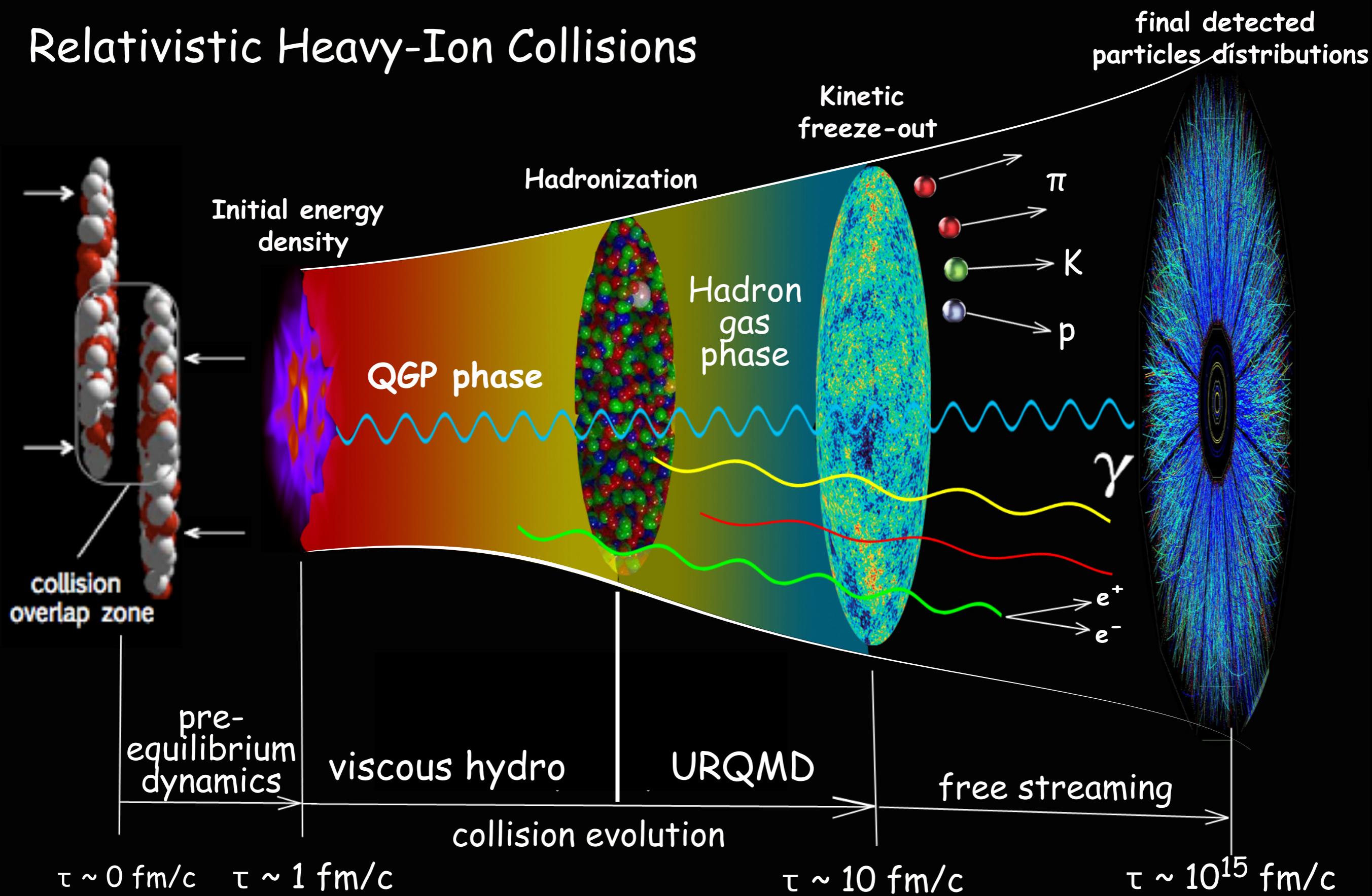
The iEBE package

Chun Shen
The Ohio State University

In collaboration with Zhi Qiu, Jia Liu, Chris
Plumberg, Jean-Francios Paquet, Jonah Bernhard,
Ulrich Heinz, Steffen Bass, and Charles Gale

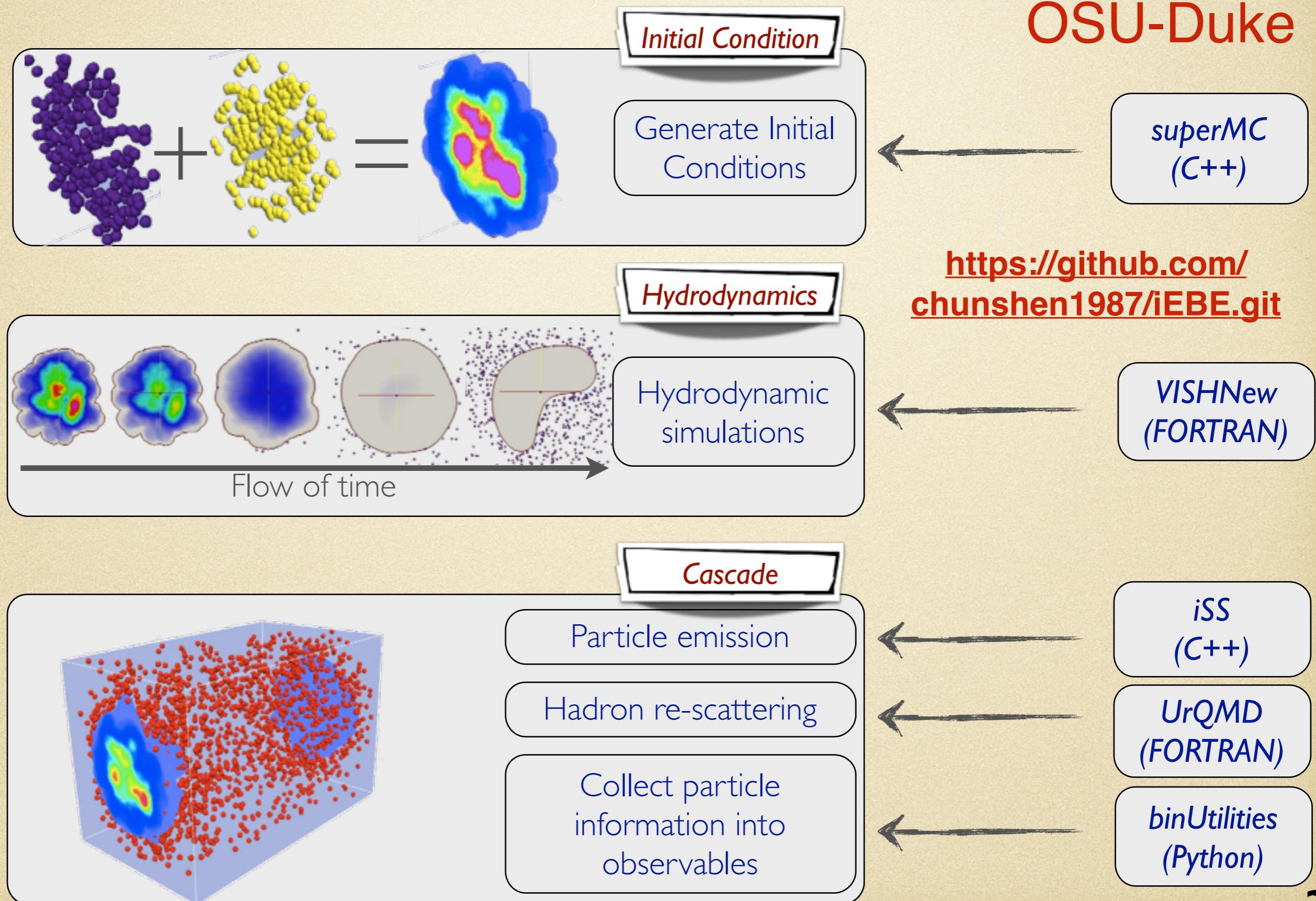
Little Bang

Relativistic Heavy-Ion Collisions



IEBE simulation work flow

OSU-Duke

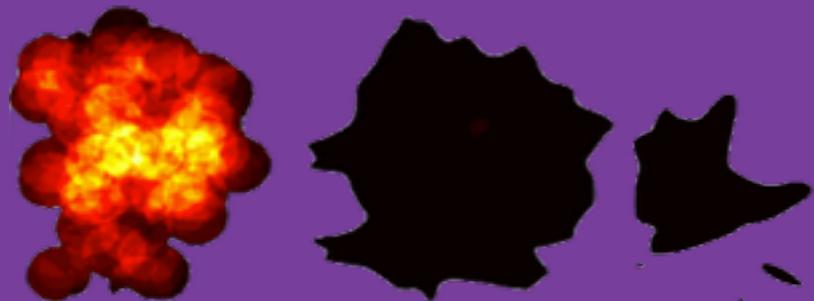


State-of-the-art hydrodynamic modeling

Initial Condition
Generators

(MC-KLN, MC-Glauber)

Hydrodynamic
Simulations
(VISH2+1)



UrQMD

Hadrons spectra &
 v_n

[https://github.com/
chunshen1987/iEBE.git](https://github.com/chunshen1987/iEBE.git)



HydroInfo
Package

e-b-e
VI SHNU

$u^\mu, \pi^{\mu\nu}$

OSU-Duke
Thermal Photon
Emission Rates

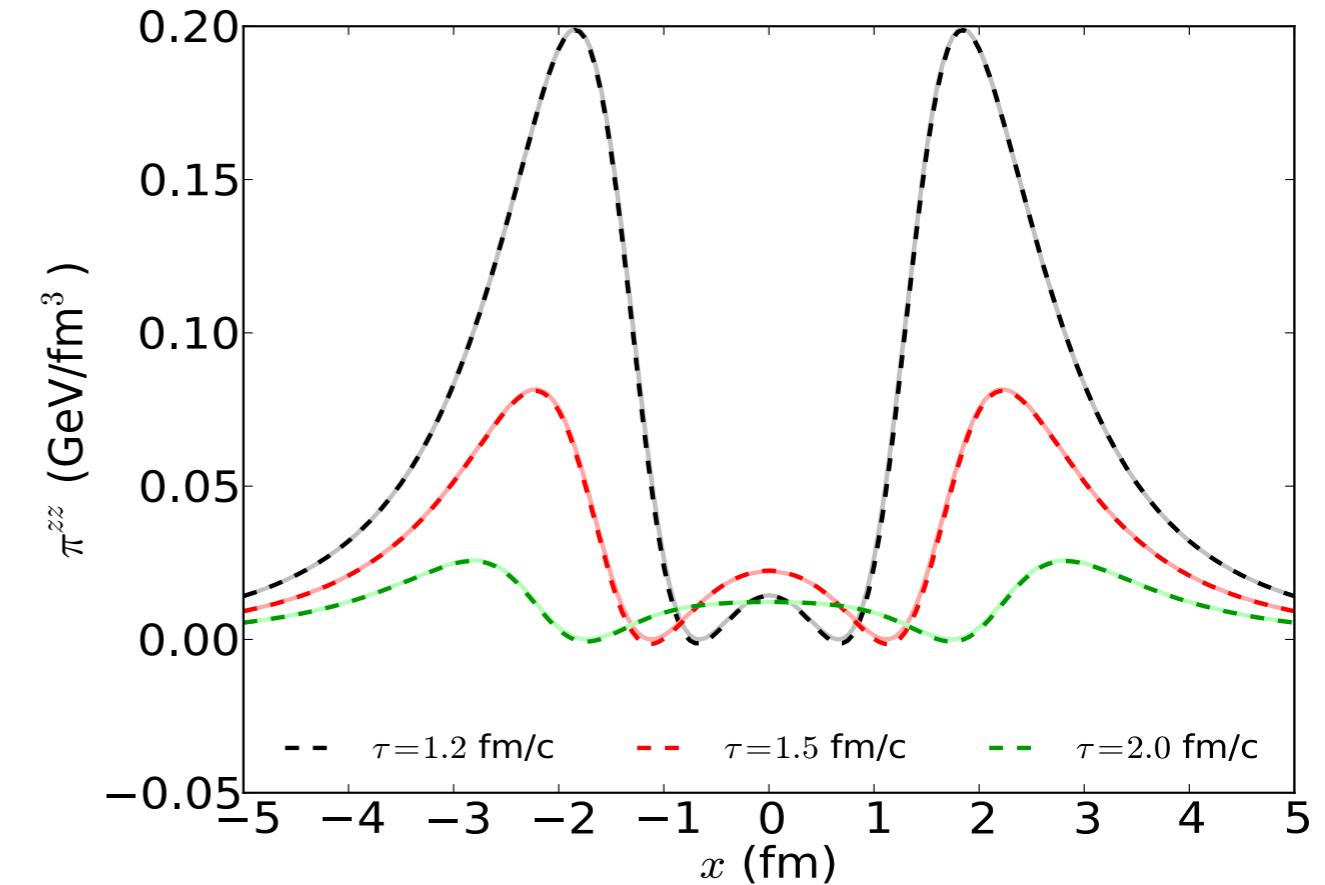
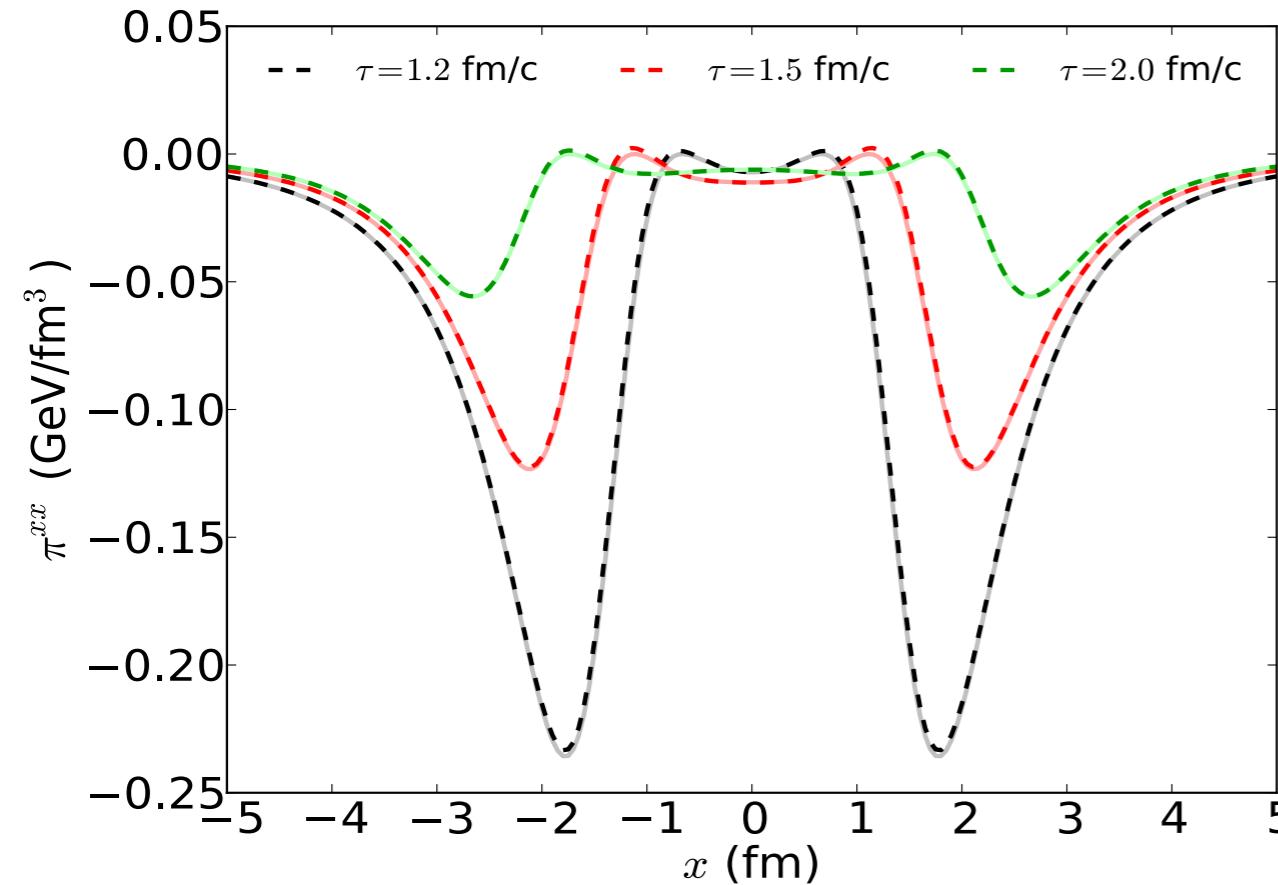
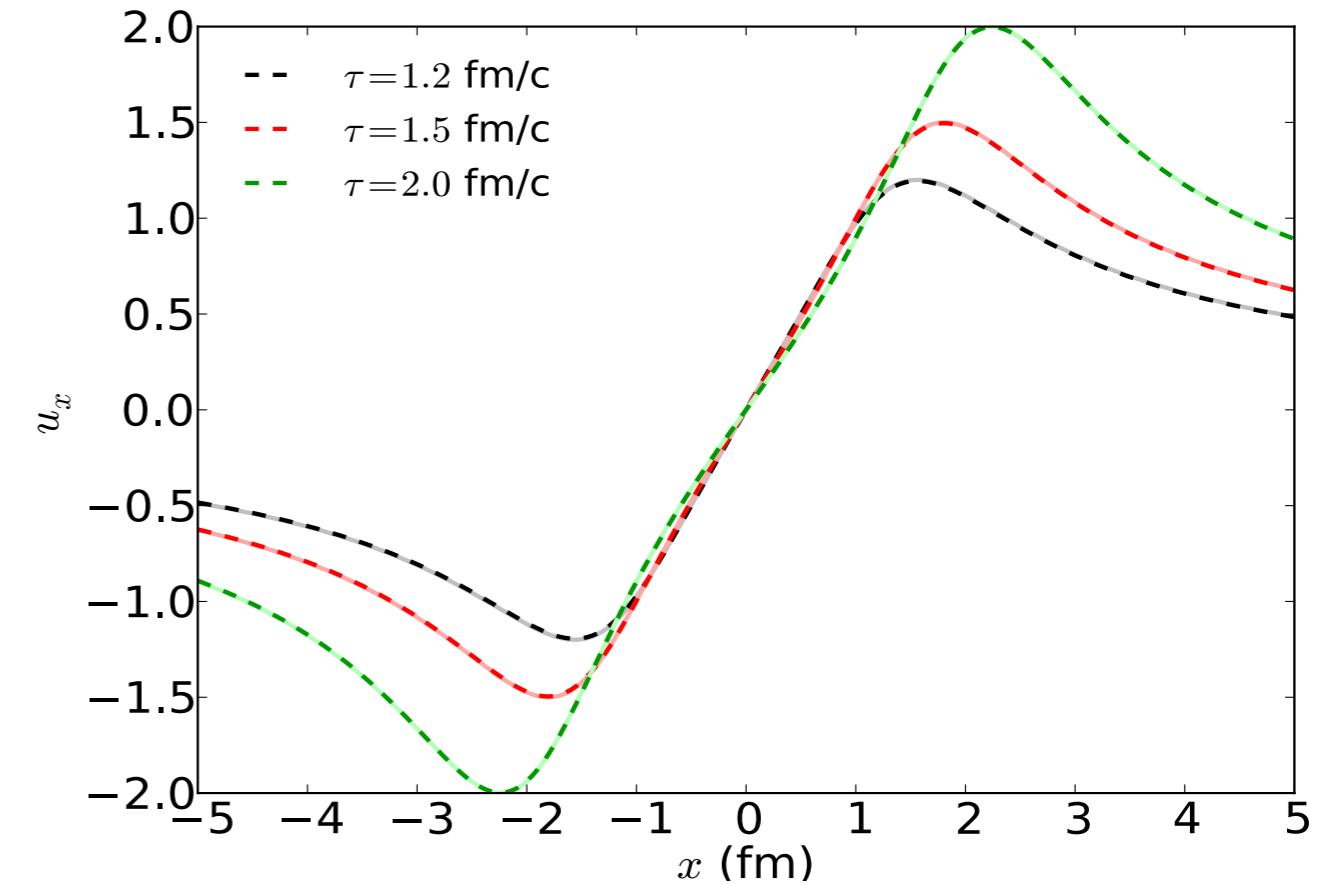
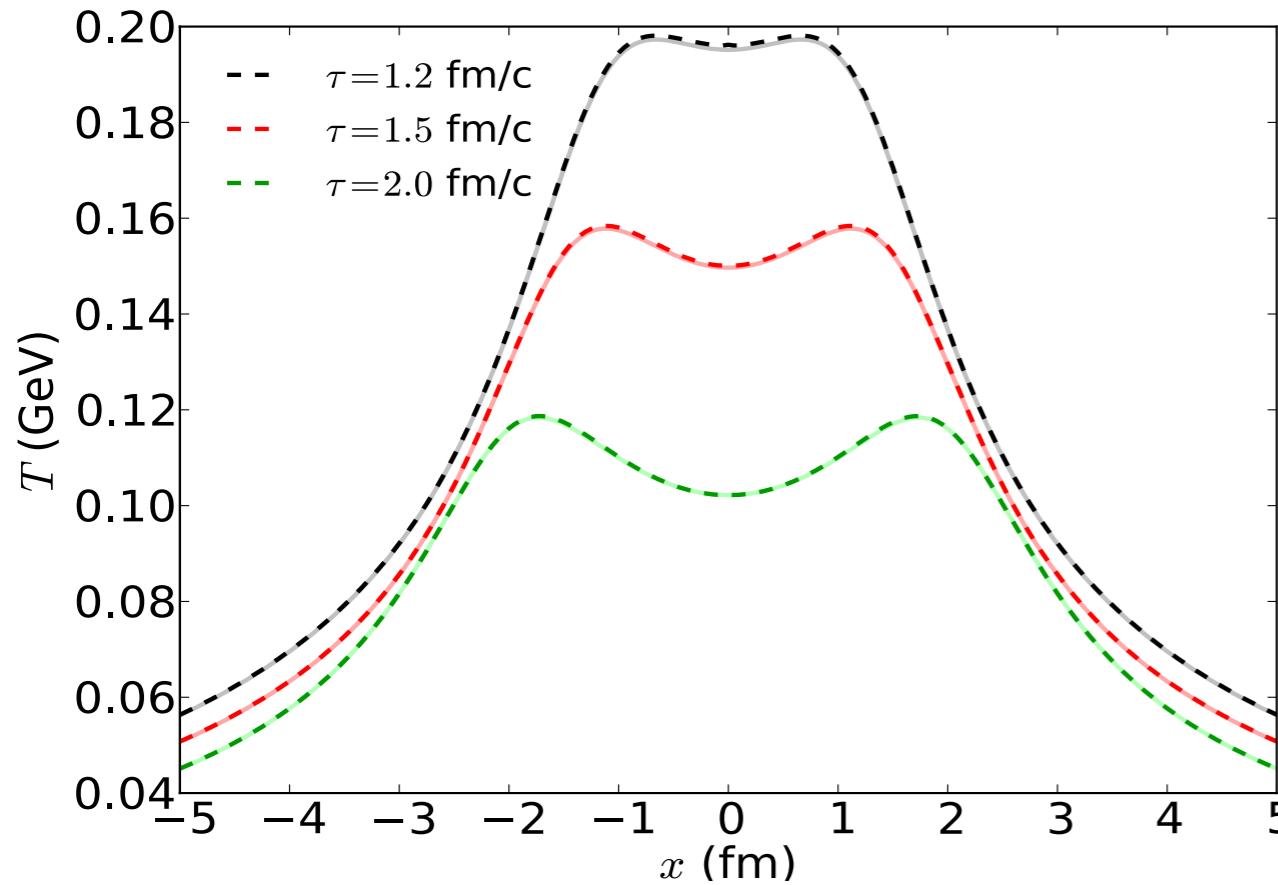
Thermal Photon
Interface
[https://github.com/
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$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\pi^{\mu\nu} q_\mu q_\nu}{2(e+p)} a_{\alpha\beta} \Gamma^{\alpha\beta}$$

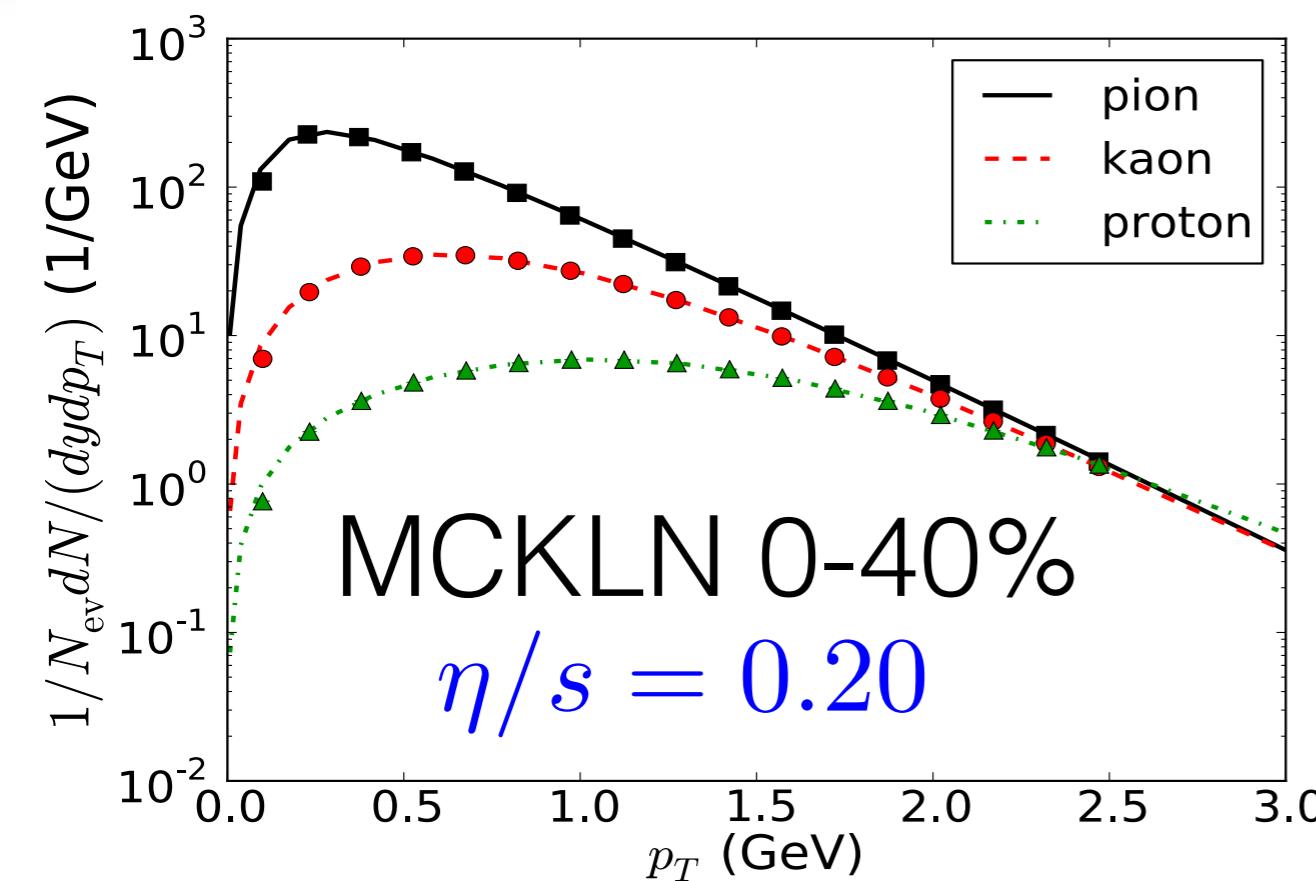
$$E \frac{dN^\gamma}{d^3p} = \int d^4x q \frac{dR}{d^3q}$$

Photon spectrum &
 v_n

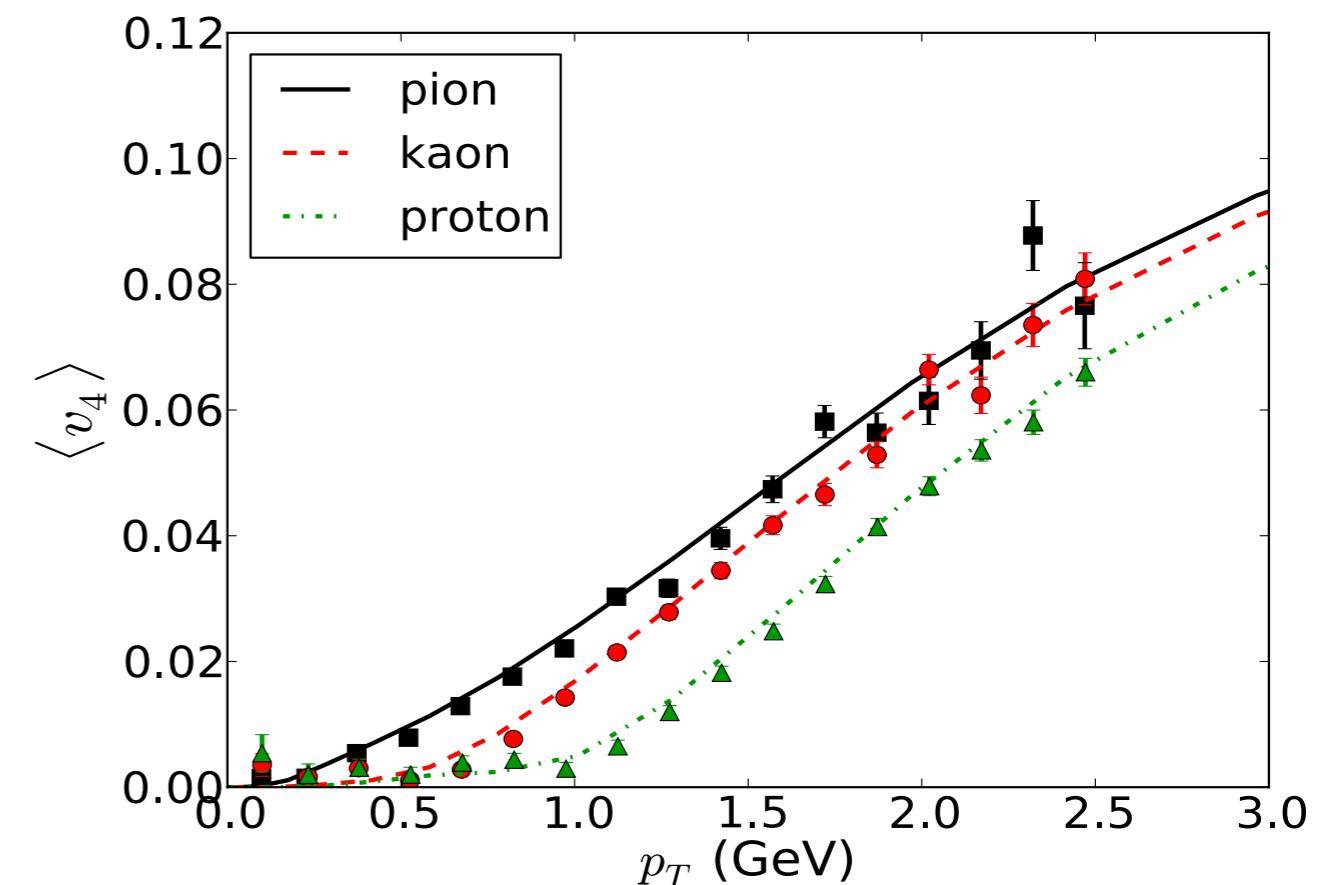
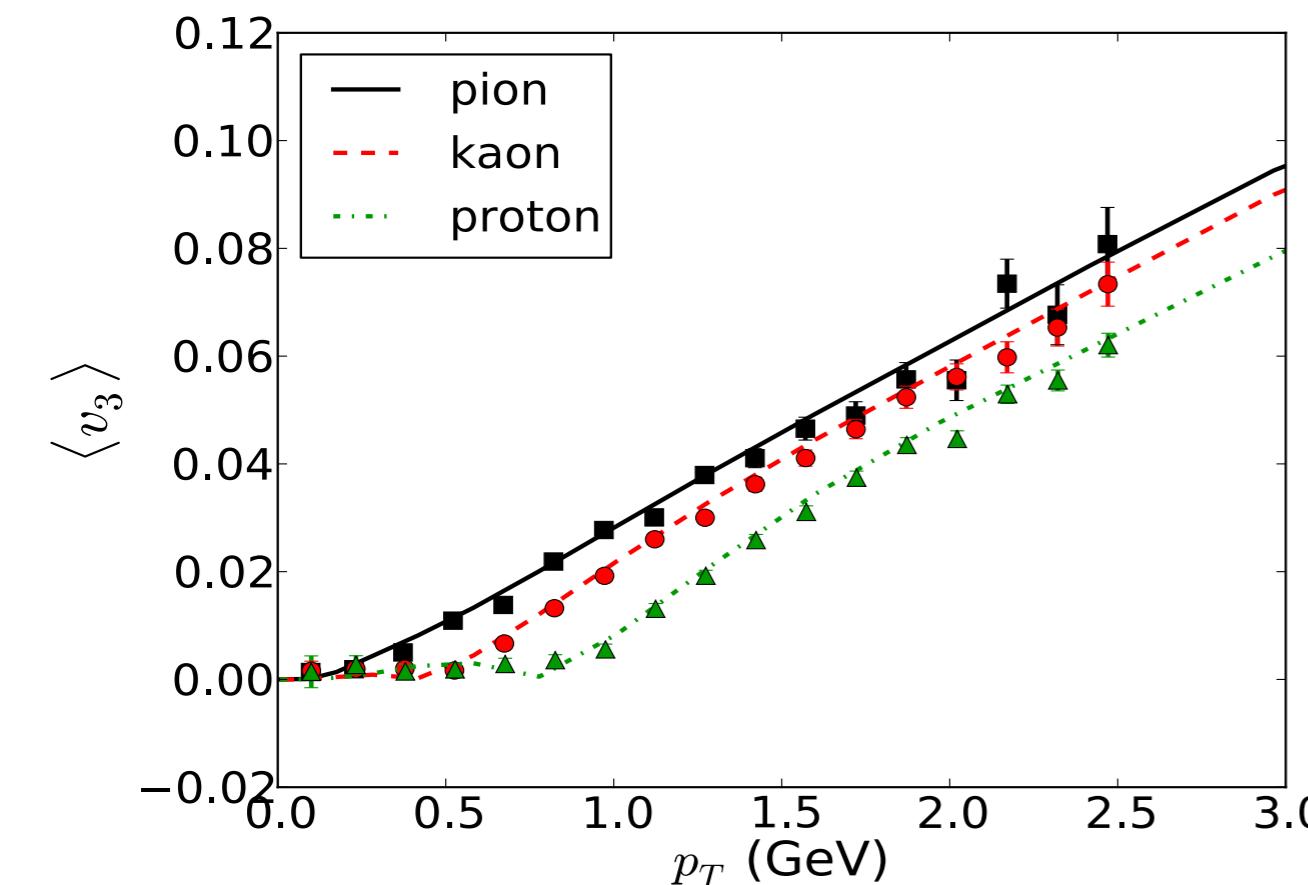
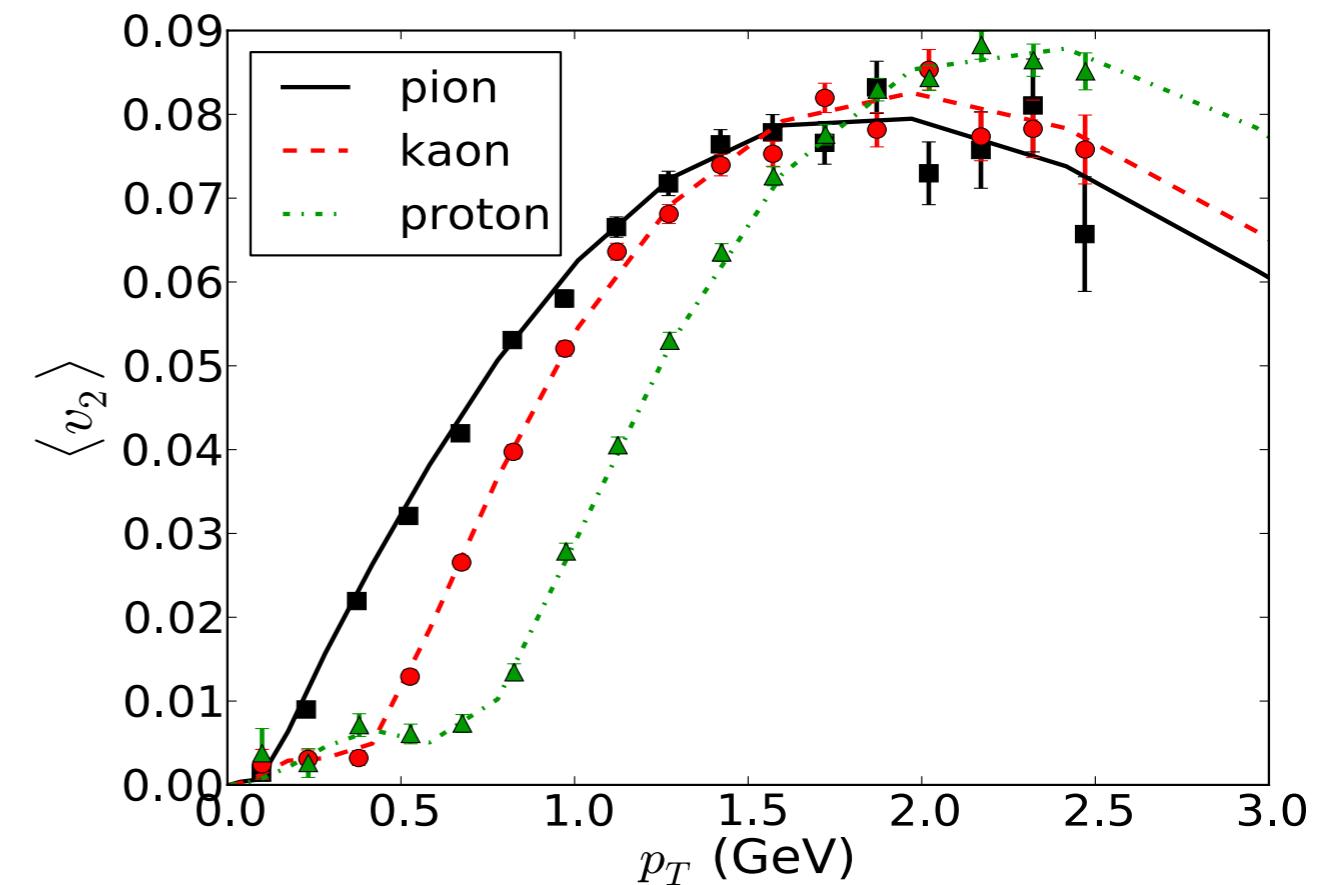
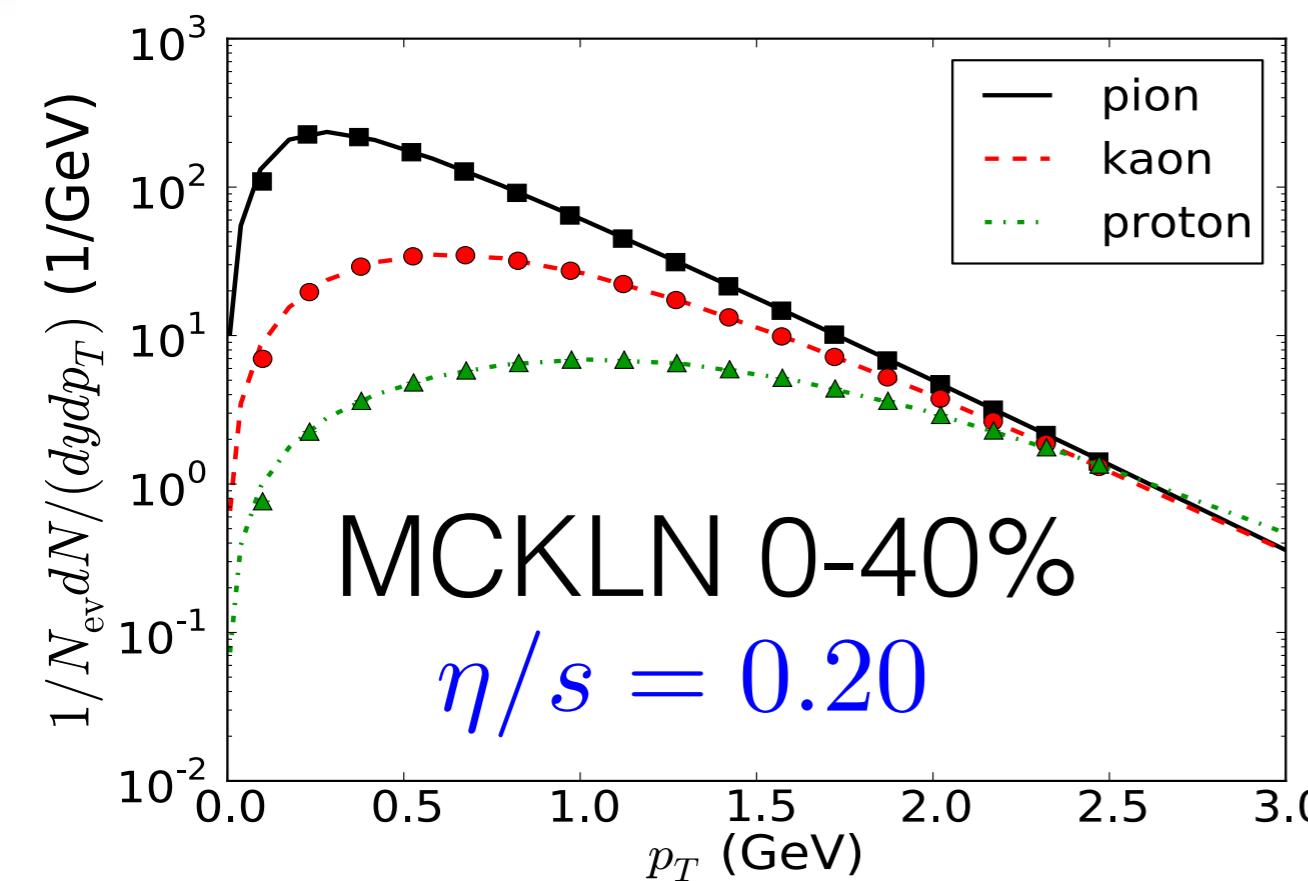
Code test VISH2+1 with Gubser's flow



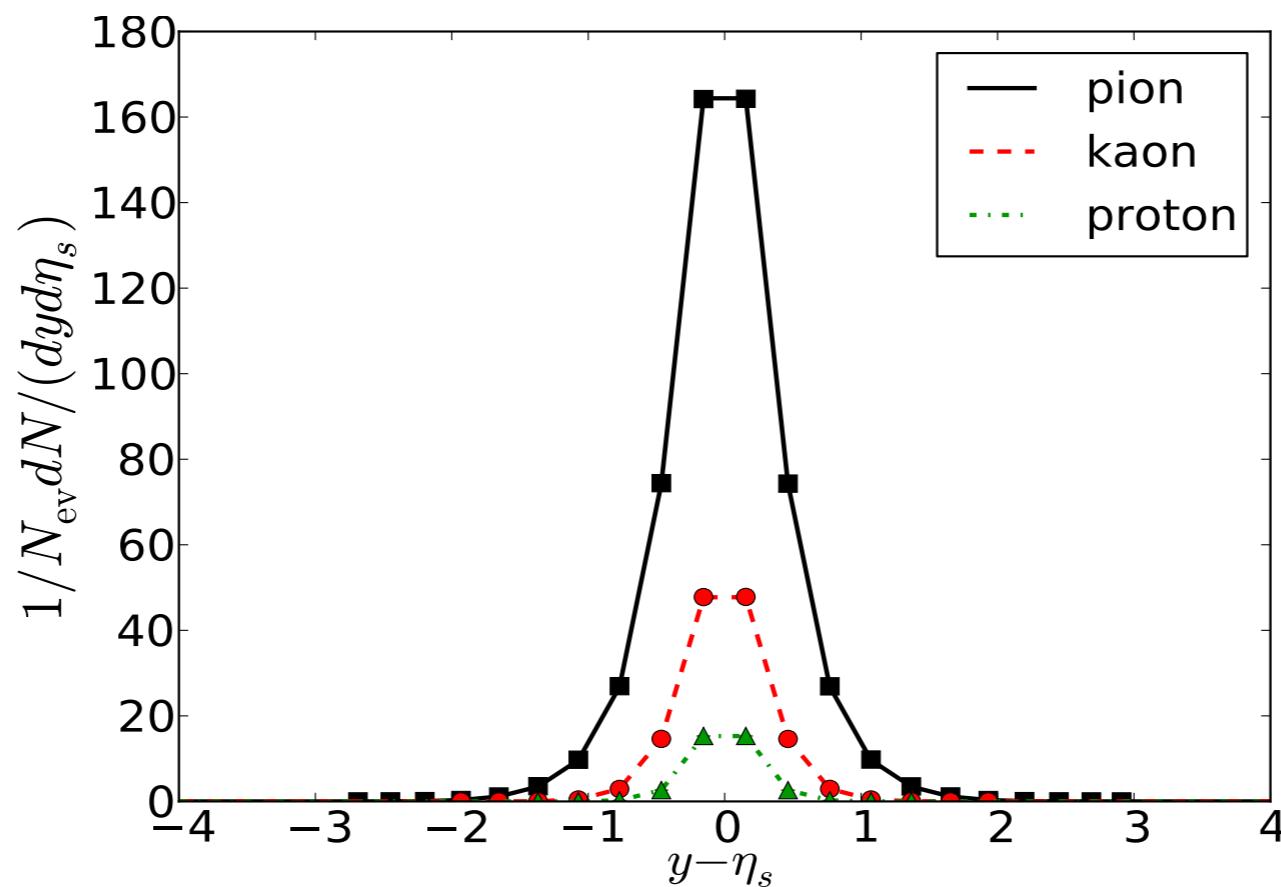
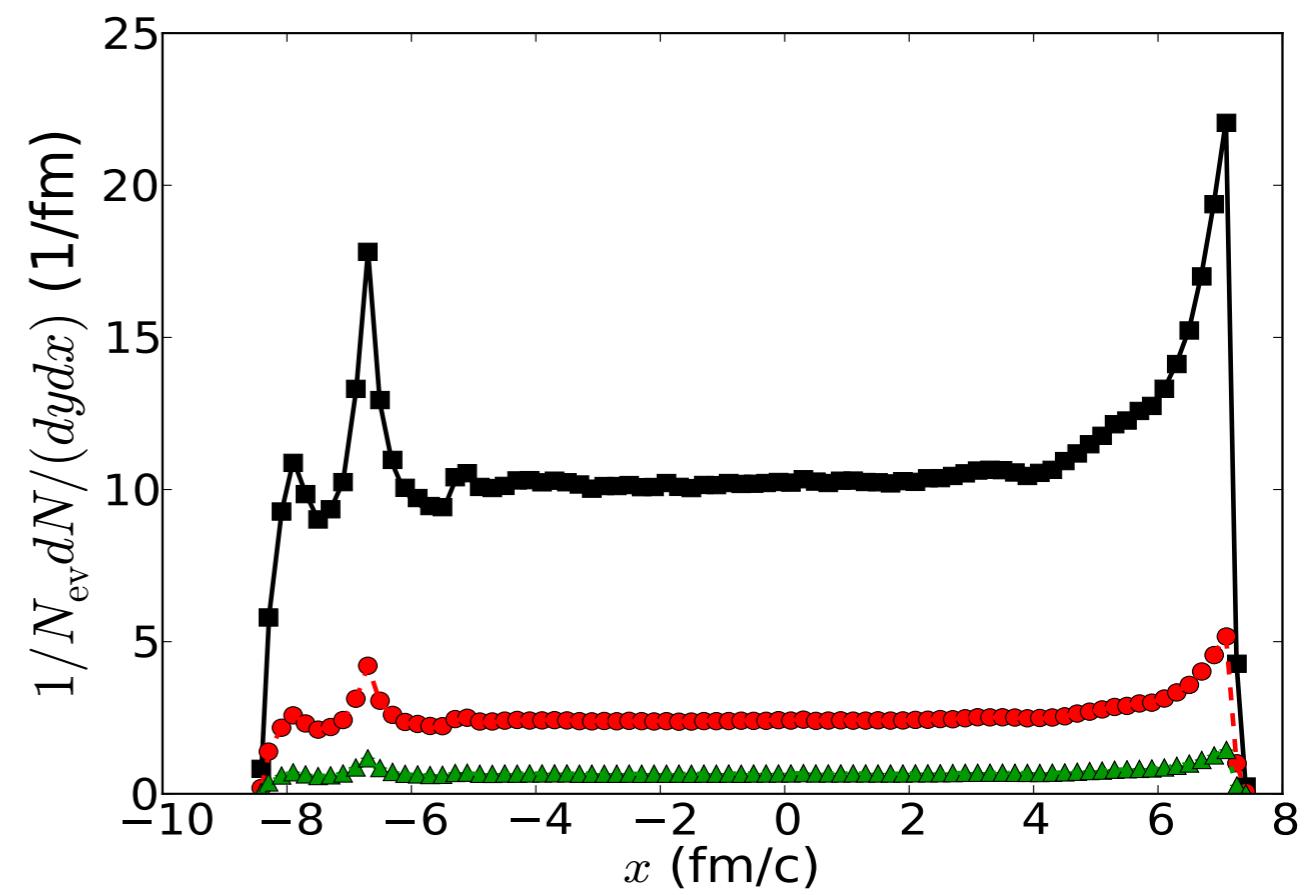
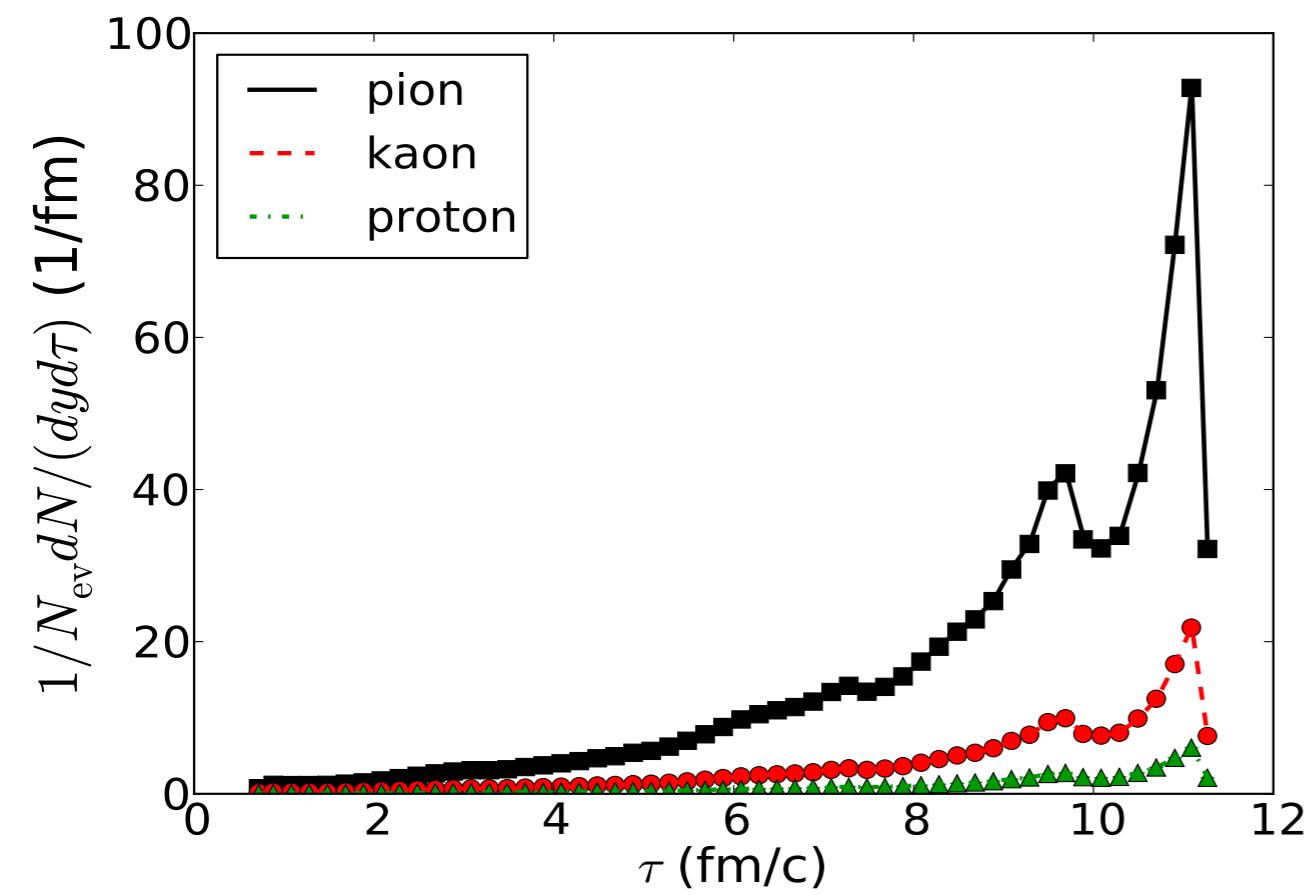
Code test iSS particle sampler



Code test iSS particle sampler



Code test iSS particle sampler



MCKLN 0-40%
 $\eta/s = 0.20$

iEBE-JET interface



iEBE-JET interface

OSU-McGill

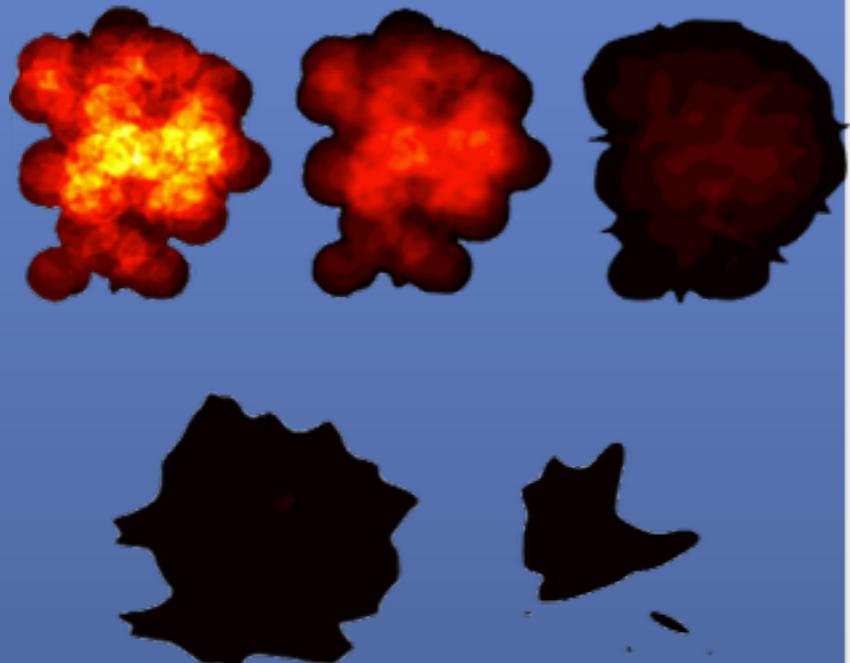
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Thermal Photon
Emission Rates

Hydrodynamic
Simulations
(VISH2+1)



HydroInfo
Package

$e, s, p, T,$
 $u^\mu, \pi^{\mu\nu}$

Thermal Photon
Interface

$$q \frac{dR}{d^3 q} = \Gamma_0 + \frac{\pi^{\mu\nu} q_\mu q_\nu}{2(e+p)} a_{\alpha\beta} \Gamma^{\alpha\beta}$$

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Hadrons spectra &
 V_n

Photon spectrum &
 V_n



iEBE-JET interface

OSU-McGill

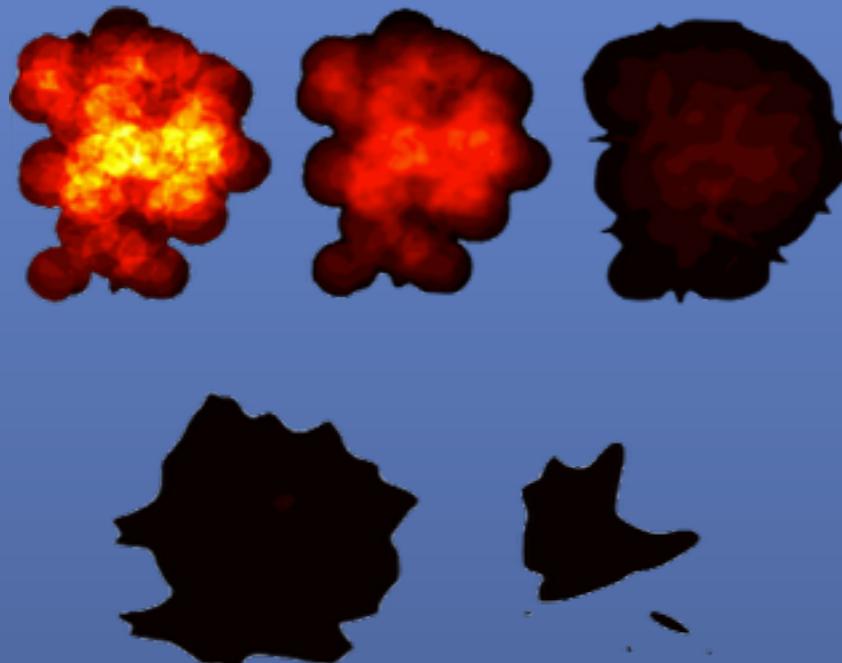
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Thermal Photon
Emission Rates

Hydrodynamic
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viscous
corrections

HydroInfo
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$e, s, p, T,$
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viscous
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Thermal Photon
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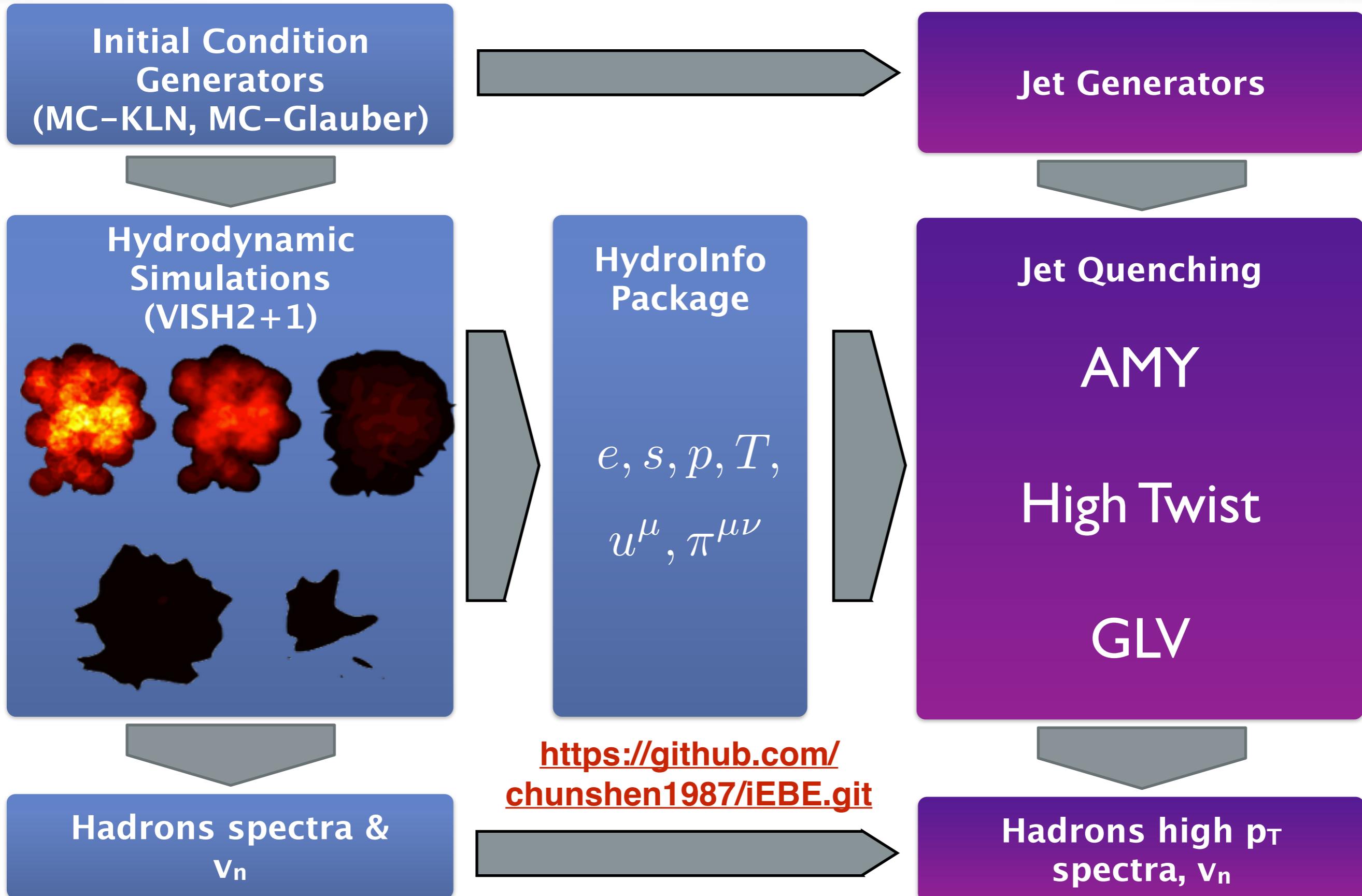
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Hadrons spectra &
 V_n

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iEBE-JET interface

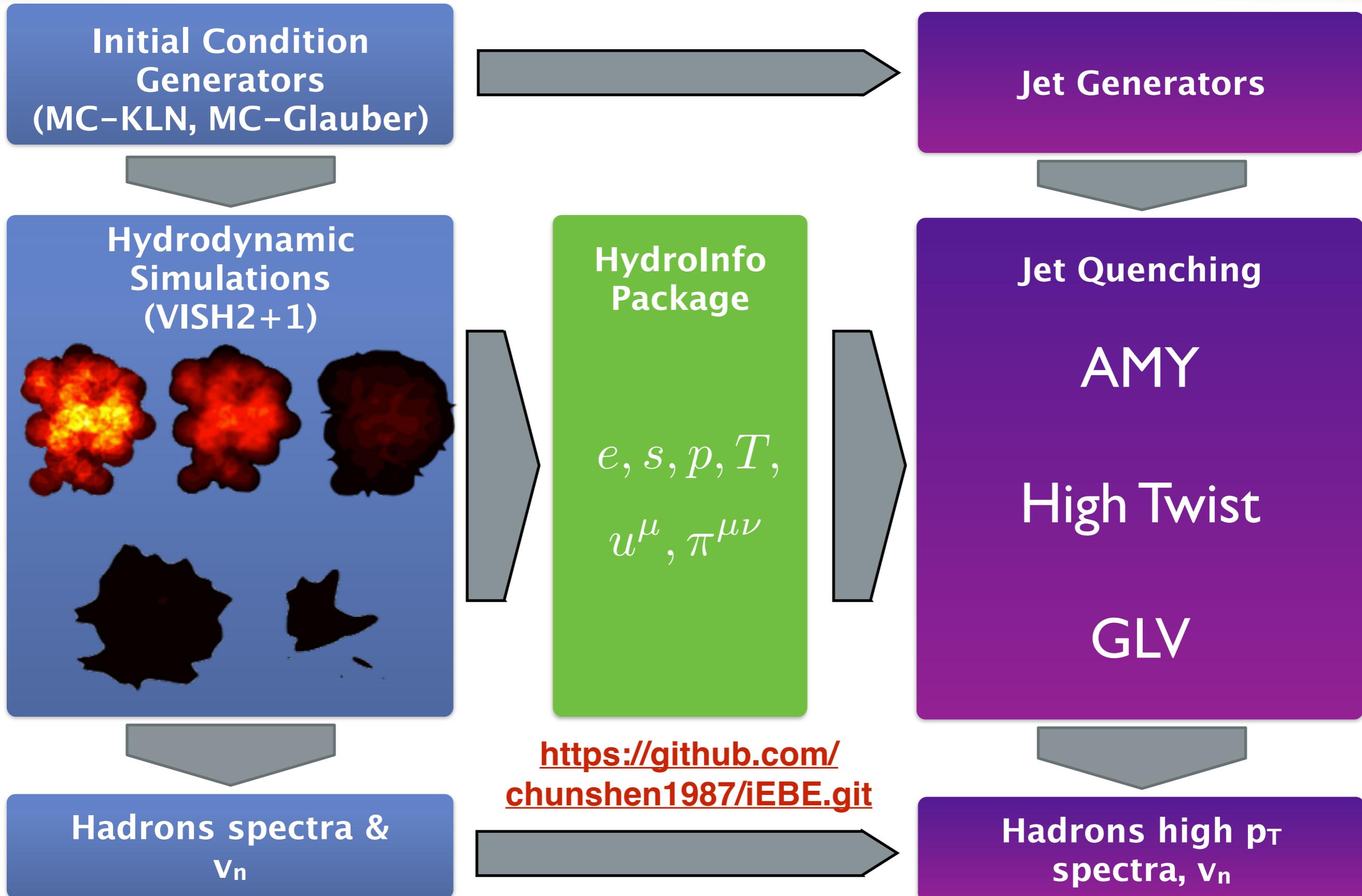


iEBE-JET interface

Our VIP customers:

- ◆ Abhijit (WSU): Jet (HT)
- ◆ Guangyou Qin (CCNU): Jet (AMY)
- ◆ Jiechen Xu (Columbia): Jet (CUJET)
- ◆ Shanshan Cao (Duke): heavy quark
- ◆ Will Horowitz (Cape Town): heavy quark
- ◆ Baoyi Chen (Tsinghua): heavy quark
- ◆ Jonah Bernhard (Duke): Ebe-VISHNU
- ◆ Damir Devetak (CMS): Ebe-VISHNU
- ◆ Min He (NUST), Zhou You (ALICE), Chiho (Nagoya), Jingfeng Liao (Indiana)

iEBE-JET interface



Hydroinfo package

Hydrodynamics evolves energy stress tensor,

$$T^{\mu\nu}$$



$$e(\text{GeV}/\text{fm}^3)$$

$$s(1/\text{fm}^3)$$

$$p(\text{GeV}/\text{fm}^3)$$

$$T(\text{GeV})$$

$$u^\mu$$

$$\pi^{\mu\nu}(\text{GeV}/\text{fm}^3)$$

$$\Pi(\text{GeV}/\text{fm}^3)$$

(optional)

HDF5 Format (Hierarchical Data Format)

- Binary format
 - typically **8 times smaller** than text file
- **Fast** random access
 - very handy for future MC jet quenching
- Platform independent (Mac, Linux, and Windows)
- Compatible with lots of languages and softwares
 - C++, Fortran, Matlab, Mathematica, ...
- Friendly GUI (easy to check data)

Interface Example

Initialization:

```
39 int bufferSize = paraRdr->getVal("HydroinfoBuffersize");
40 int hydroInfoVisflag = paraRdr->getVal("HydroinfoVisflag");
41 HydroinfoH5* hydroinfo_ptr = new HydroinfoH5("results/JetData.h5",
bufferSize, hydroInfoVisflag); //hydro data file pointer
42 int neta = paraRdr->getVal("neta");
```

Get hydro information:

```
int idx_Tb = 0;
hydroinfo_ptr->getHydroinfo(tau_local, x_local, y_local, fluidCellptr);
temp_local = fluidCellptr->temperature;
```

Hydrodynamic variables at
tau_local, x_local, y_local

```
11
12 struct fluidCell {
13     double ed, sd, vx, vy,
14                 temperature, pressure;
15     double pi[4][4];
16     double bulkPi;
17 };
```

iEBE-JET package

OSU-McGill

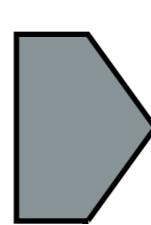
Initial Condition
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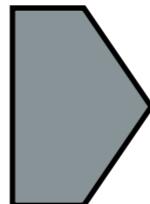
Hydrodynamic
Simulations
(ViSH2+1)



Hadrons spectra &
 v_n



HydroInfo
Package



Thermal Photon
Emission Rates



Thermal Photon
Interface



Photon spectrum &
 v_n



Collect results into sqlite database

Viscous Photon Emission Rates: General Formalism

Thermal photon emission rates can be calculated by

$$E_q \frac{dR}{d^3q} = \int \frac{d^3p_1}{2E_1(2\pi)^3} \frac{d^3p_2}{2E_2(2\pi)^3} \frac{d^3p_3}{2E_3(2\pi)^3} \frac{1}{2(2\pi)^3} |\mathcal{M}|^2$$
$$\times f_1(p_1^\mu) f_2(p_2^\mu) (1 \pm f_3(p_3^\mu)) (2\pi)^4 \delta^{(4)}(p_1 + p_2 - p_3 - q)$$

With

$$f(p^\mu) = f_0(E) + f_0(E)(1 \pm f_0(E)) \frac{\pi^{\mu\nu} \hat{p}_\mu \hat{p}_\nu}{2(e+p)} \chi\left(\frac{p}{T}\right)$$

We can expand photon emission rates around the thermal equilibrium:

$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\pi^{\mu\nu} \hat{q}_\mu \hat{q}_\nu}{2(e+p)} a_{\alpha\beta} \Gamma^{\alpha\beta},$$

OSU-McGill

$$a_{\mu\nu} = \frac{3}{2(u \cdot \hat{q})^4} \hat{q}_\mu \hat{q}_\nu + \frac{1}{(u \cdot \hat{q})^2} u_\mu u_\nu + \frac{1}{2(u \cdot \hat{q})^2} g_{\mu\nu} - \frac{3}{2(u \cdot \hat{q})^3} (\hat{q}_\mu u_\nu + \hat{q}_\nu u_\mu).$$

Viscous Photon Emission Rates: General Formalism

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$$\times f_1(p_1^\mu) f_2(p_2^\mu) (1 \pm f_3(p_3^\mu)) (2\pi)^4 \delta^{(4)}(p_1 + p_2 - p_3 - q)$$

With

$$f(p^\mu) = \frac{\pi^{\mu\nu} \hat{n}_\nu \hat{p}_\nu}{\Gamma_0(q, T) - a_{\alpha\beta} \Gamma^{\alpha\beta}(q, T)} \chi\left(\frac{p}{T}\right)$$

We can expand calculated in fluid local rest frame and the thermal equilibrium:

$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\pi^{\mu\nu} \hat{q}_\mu \hat{q}_\nu}{2(e + p)} - a_{\alpha\beta} \Gamma^{\alpha\beta},$$

OSU-McGill

$$a_{\mu\nu} = \frac{3}{2(u \cdot \hat{q})^4} \hat{q}_\mu \hat{q}_\nu + \frac{1}{(u \cdot \hat{q})^2} u_\mu u_\nu + \frac{1}{2(u \cdot \hat{q})^2} u_\mu u_\nu - \frac{1}{2(u \cdot \hat{q})^2} u_\mu u_\nu.$$

calculated in lab frame

Viscous Photon Emission Rates: General Formalism

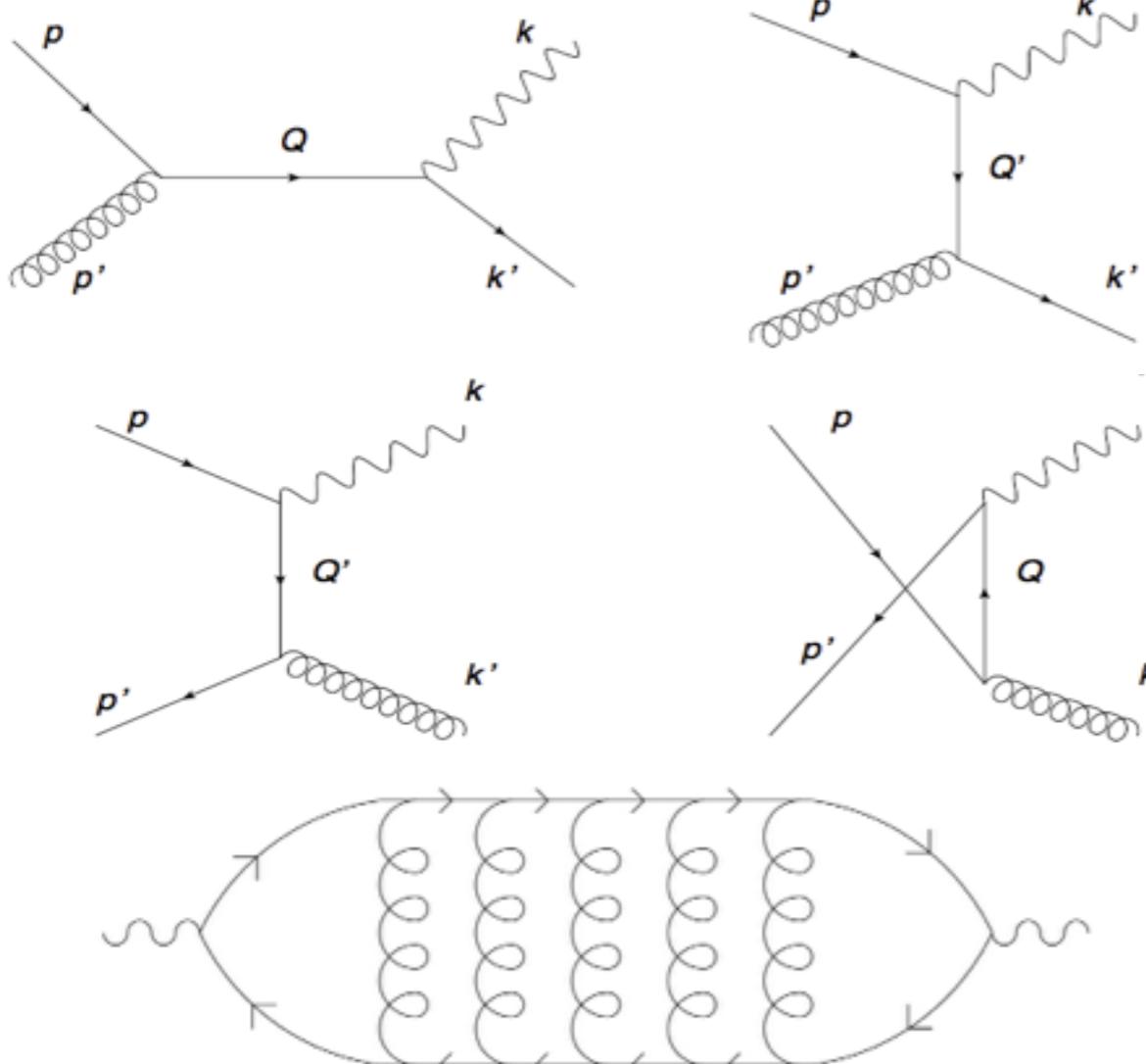
$$q \frac{dR}{d^3q} = \Gamma_0 + \frac{\pi^{\mu\nu} \hat{q}_\mu \hat{q}_\nu}{2(e+p)} a_{\alpha\beta} \Gamma^{\alpha\beta}$$

OSU-McGill

Equilibrium rates

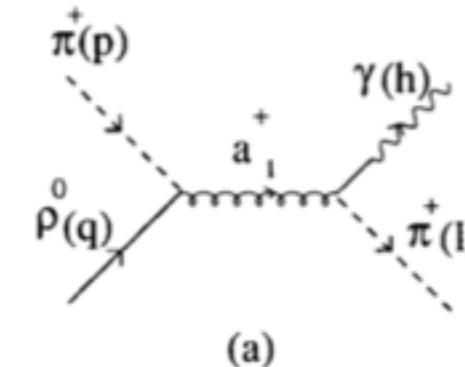
QGP

(AMY 2001)

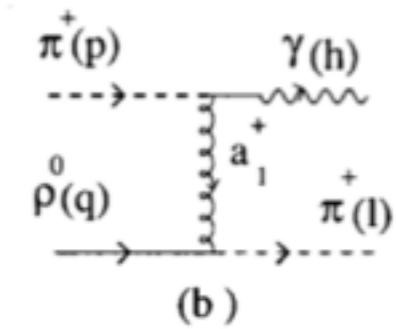


Hadron Gas

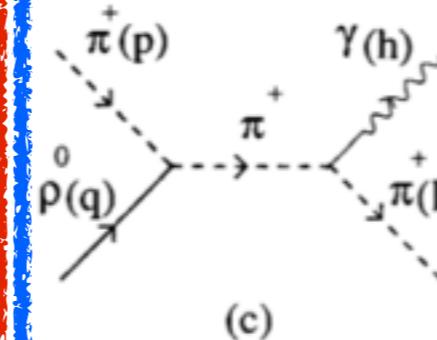
(TRG 2004)



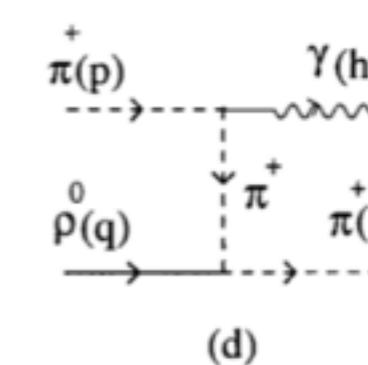
(a)



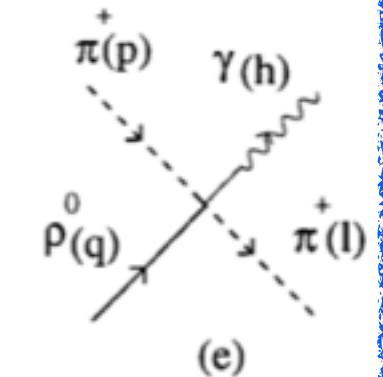
(b)



(c)



(d)



(e)

Viscous Photon Emission Rates: General Formalism

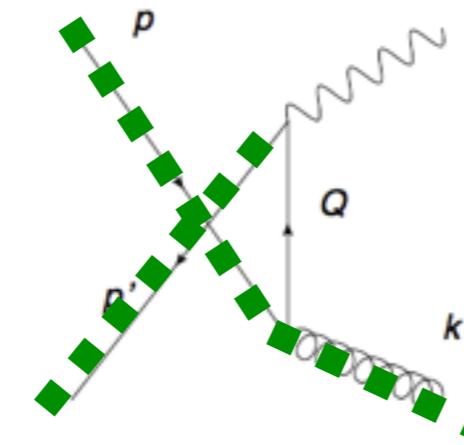
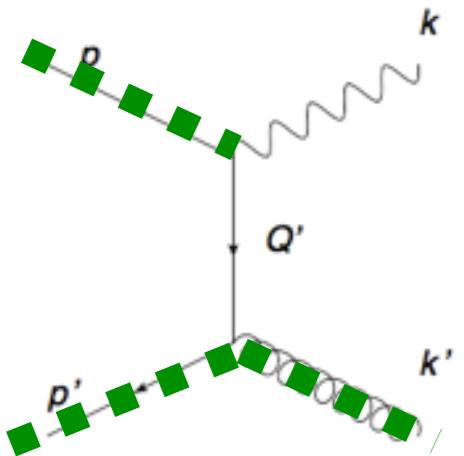
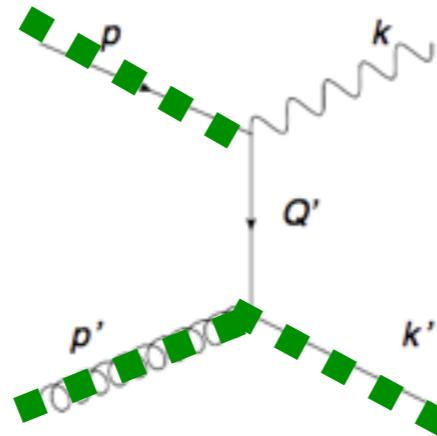
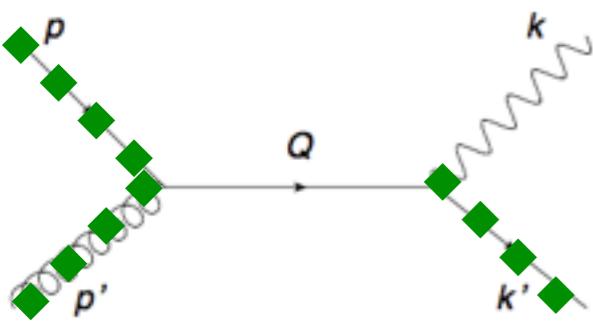
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OSU-McGill

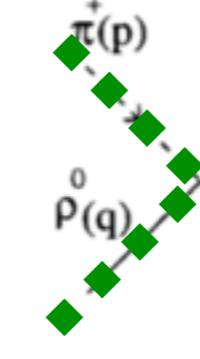
Equilibrium rates

off-equilibrium δf corrections

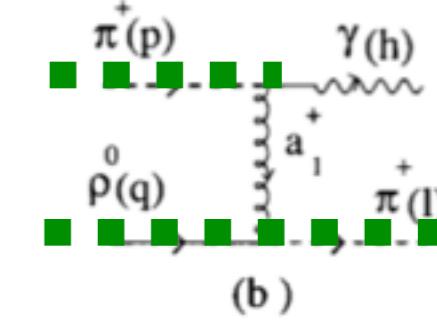
QGP



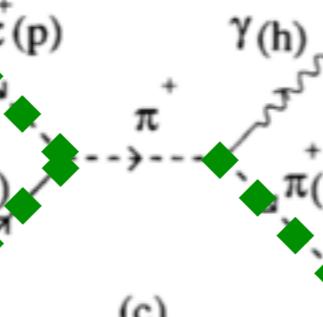
Hadron Gas



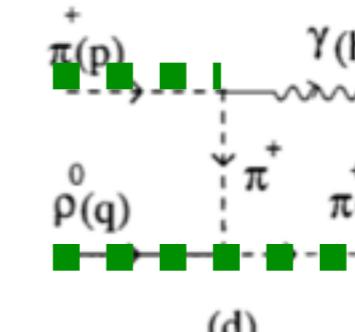
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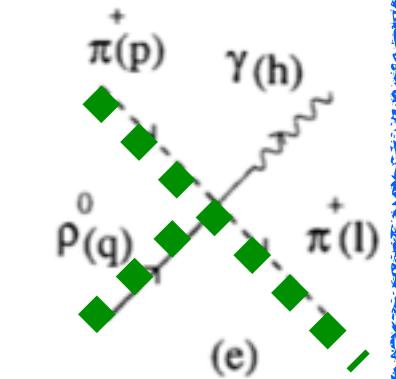
(b)



(c)



(d)



(e)

Viscous Photon Emission Rates: General Formalism

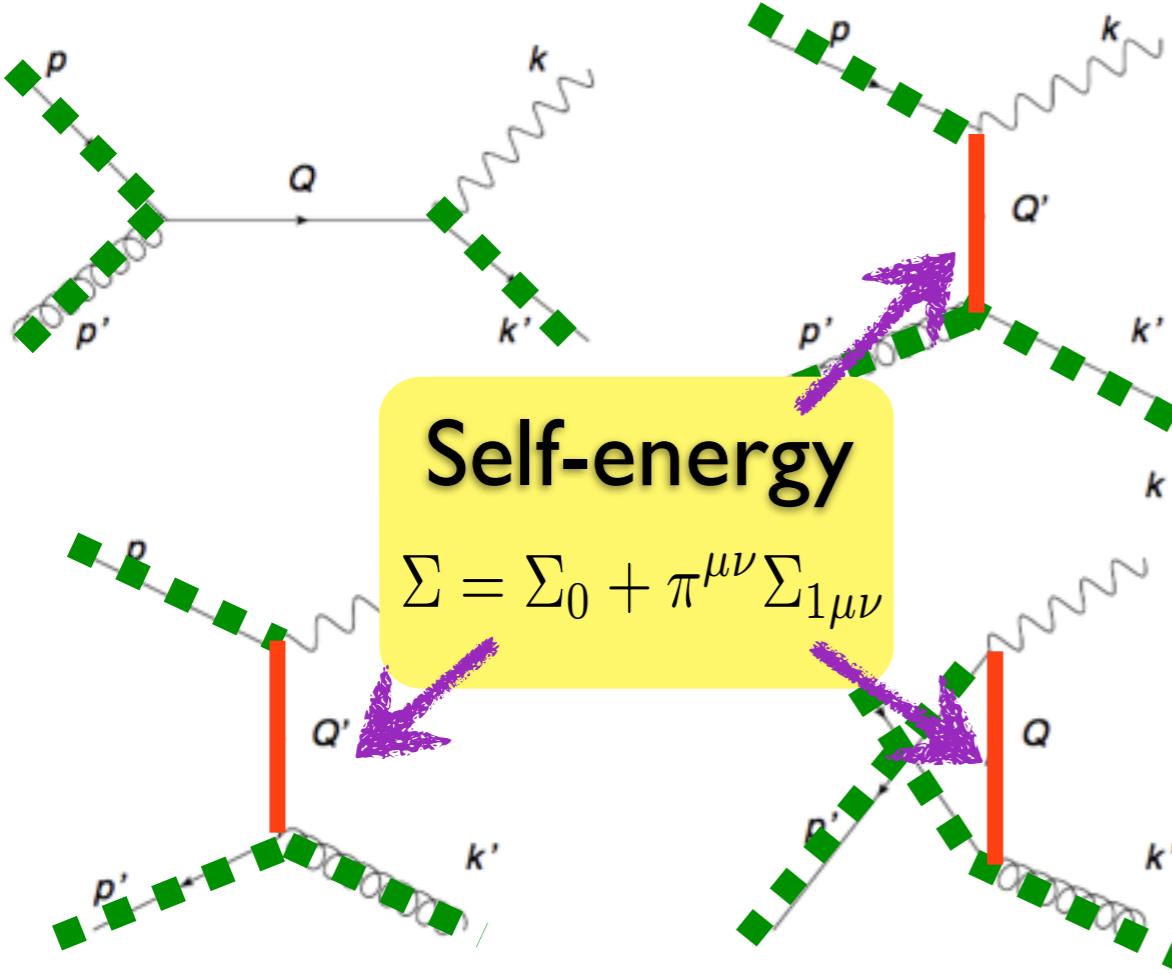
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OSU-McGill

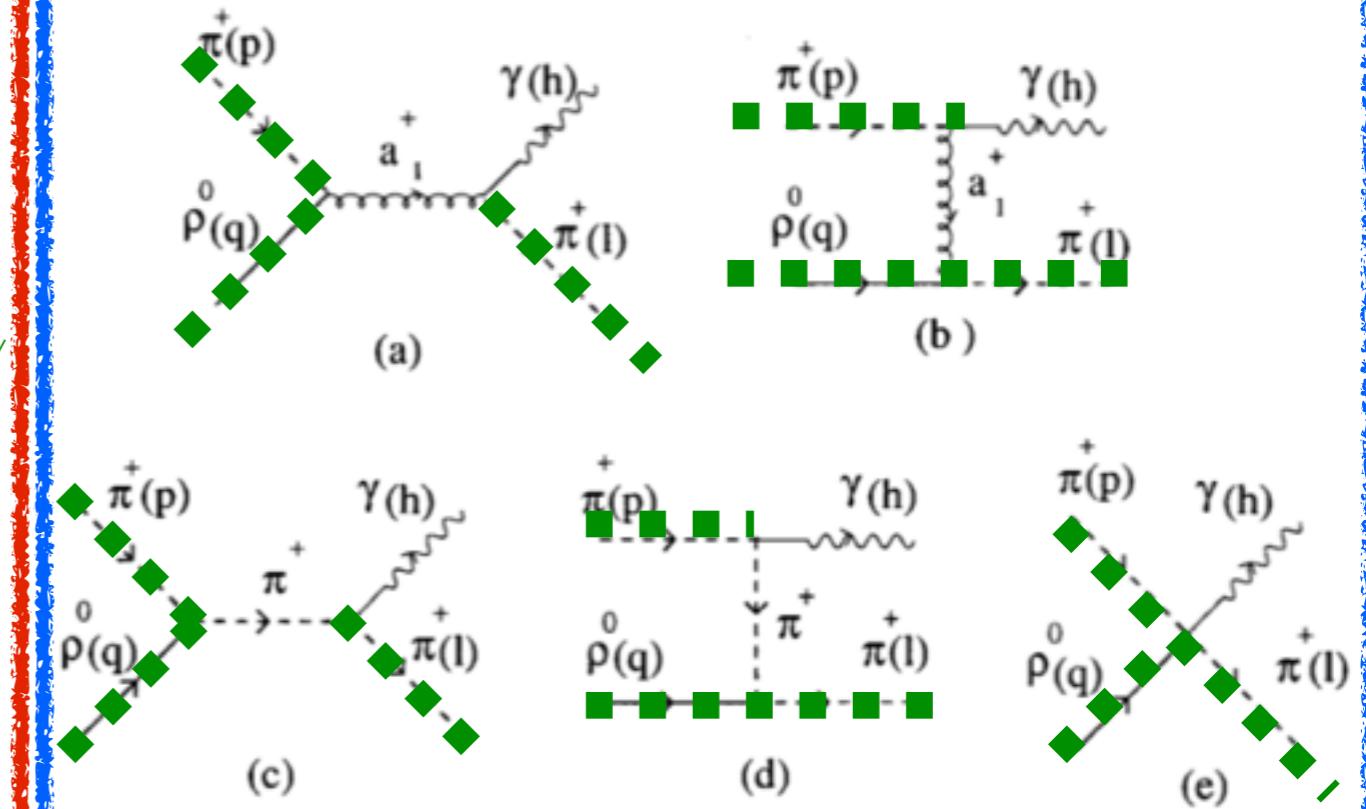
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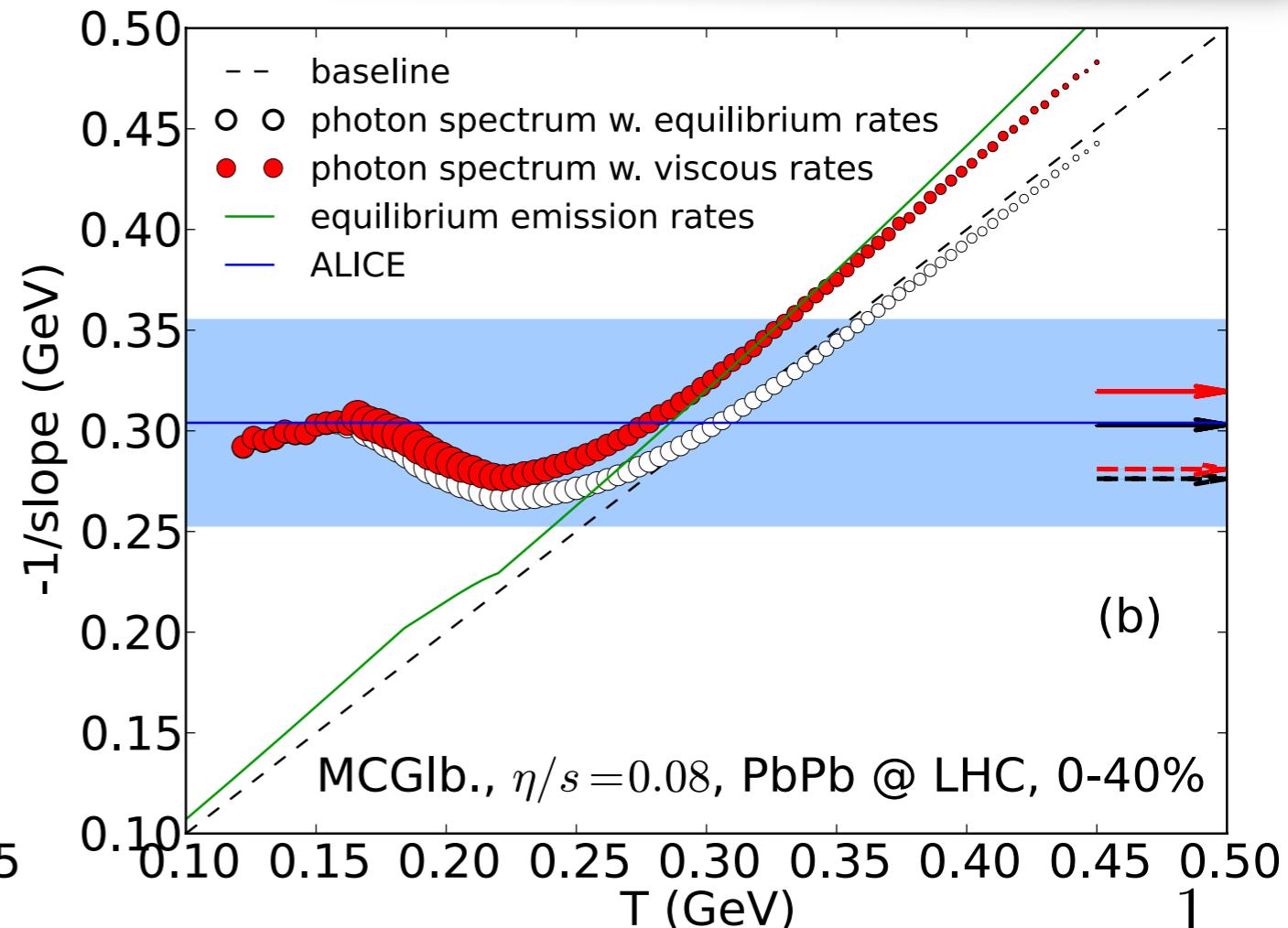
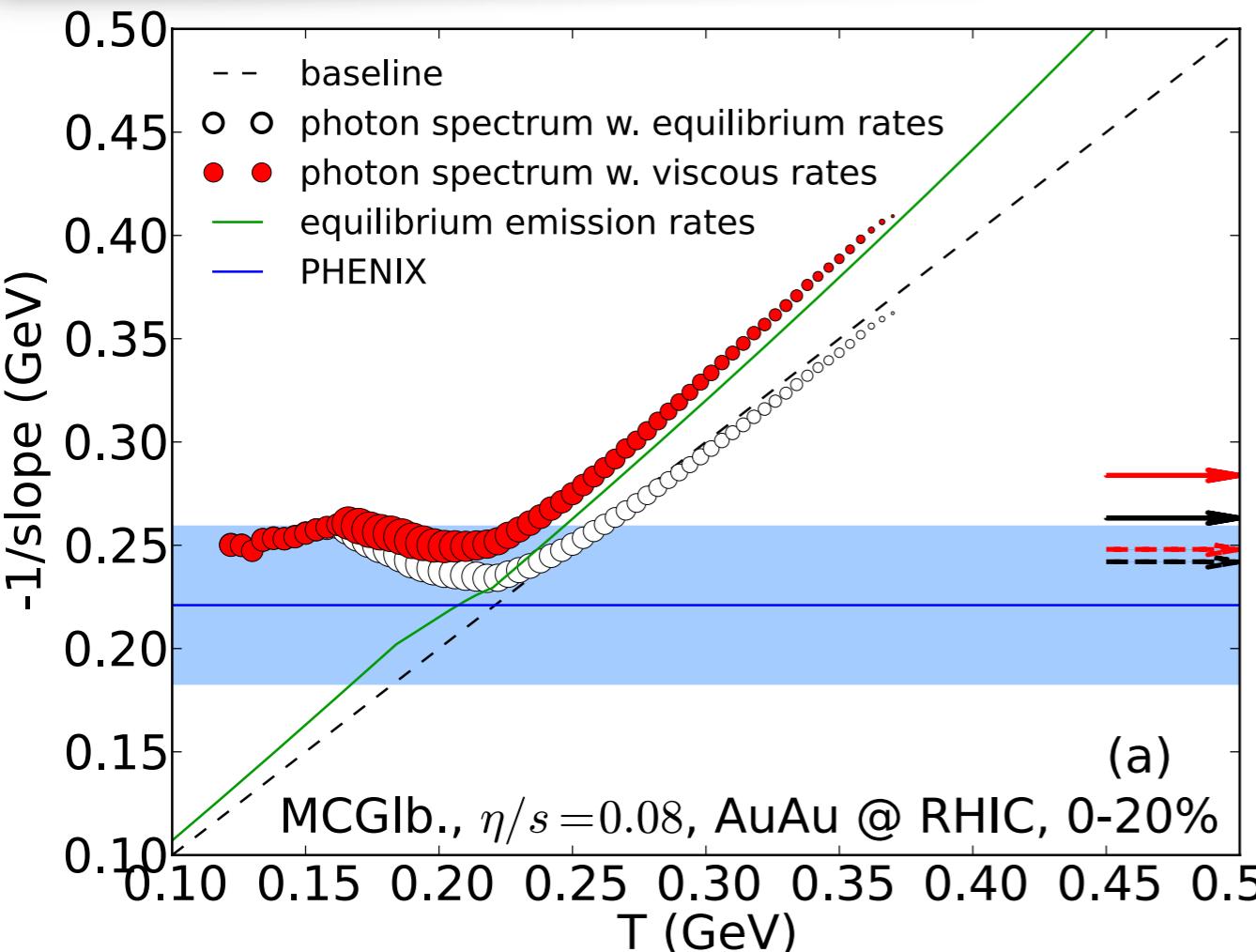
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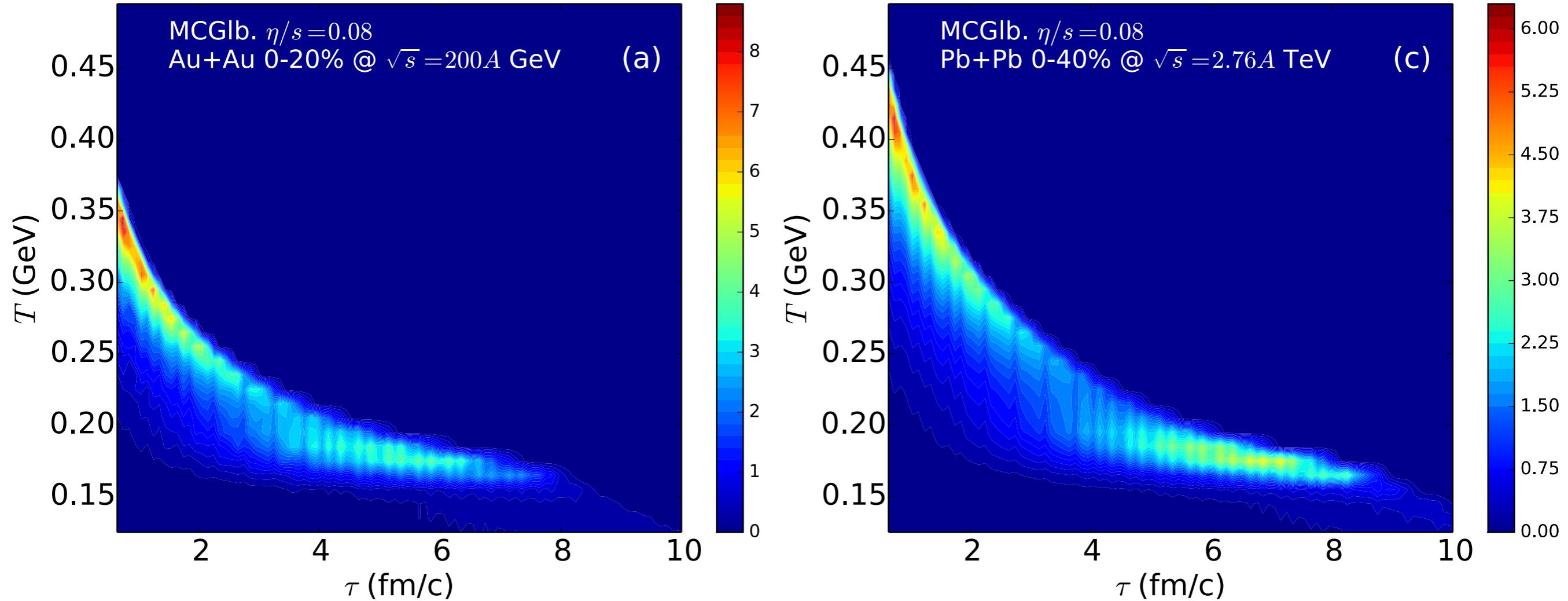
Fitted T_{eff} vs. True Temperature



- Photon emission rates $\propto \exp(-E/T) \log(E/T)$, $T_{\text{eff}} > T$
- All photons with $T < 250$ MeV at RHIC and < 300 MeV at LHC carries T_{eff} within the experimental fitted region
- About 50-60% of photons are emitted from $T = 165\text{--}250$ MeV, they are strongly blue shifted by radial flow

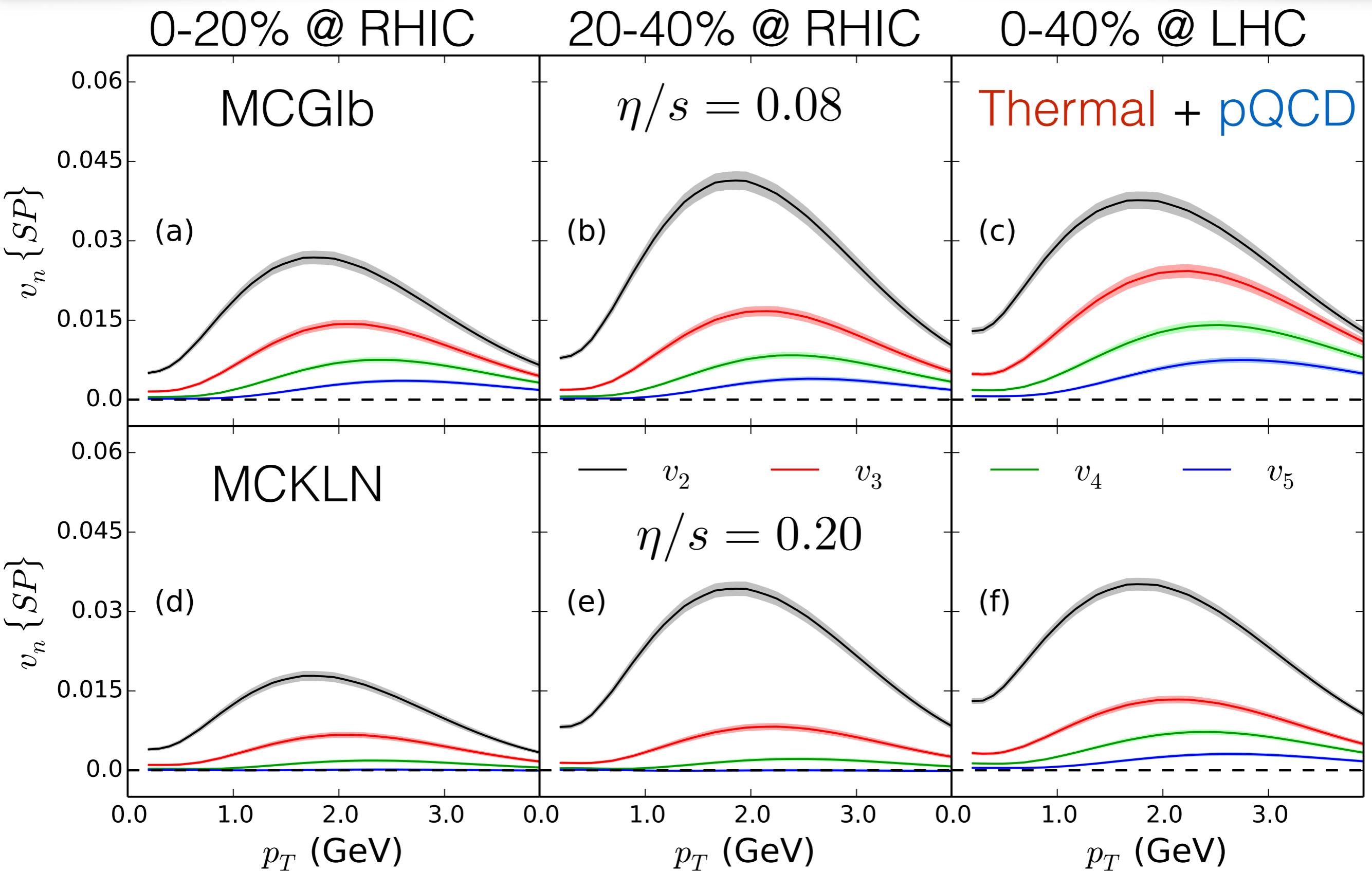
$$T_{\text{eff}} = T \sqrt{\frac{1+v}{1-v}}$$

Mapping thermal photon emission



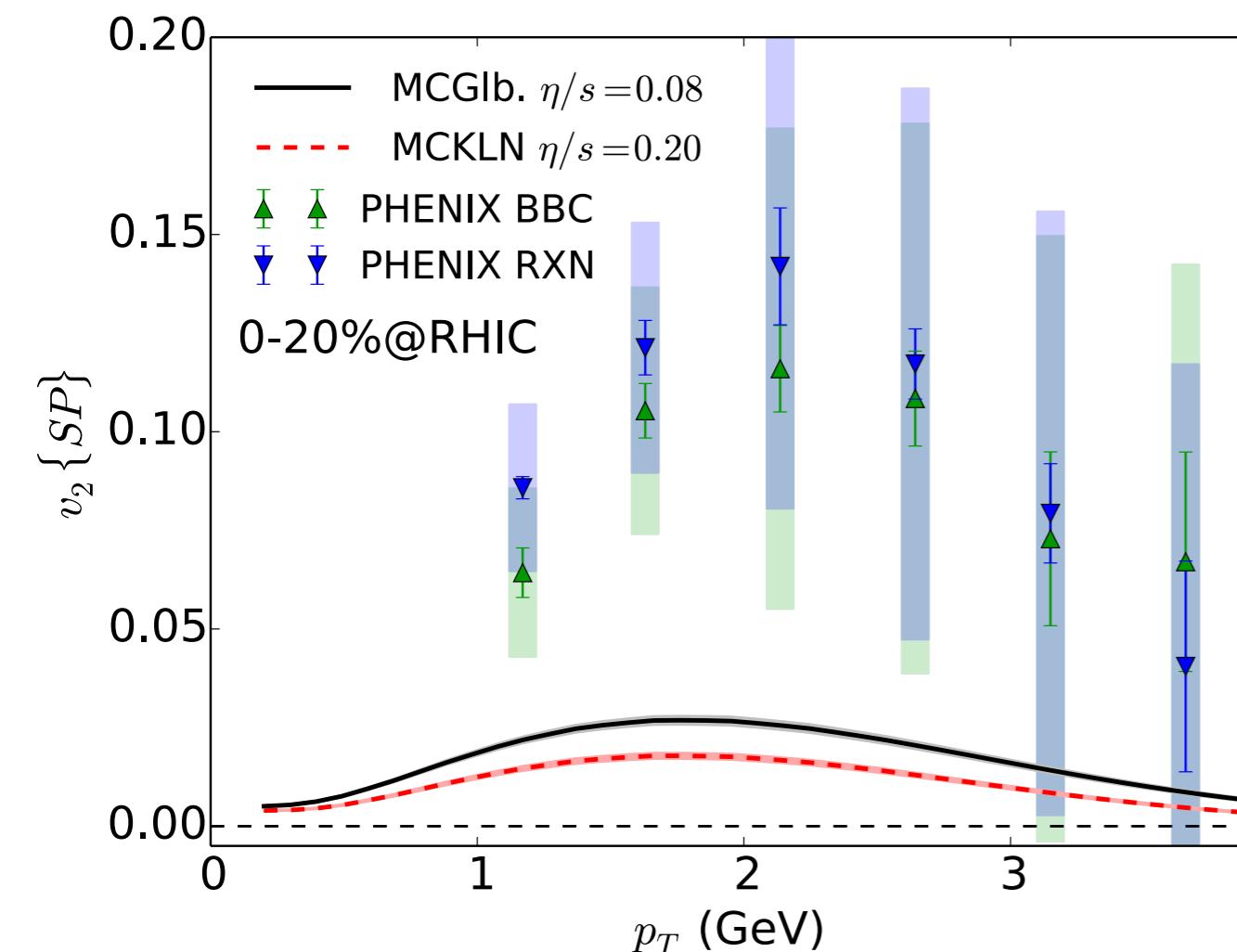
- By cutting hydro medium both in T and τ , we observe a **two-wave** thermal photon production
 - early time production — high rates at high temperatures
 - near transition region — growing of space-time volume

Event-by-Event Full Viscous Photon v_n

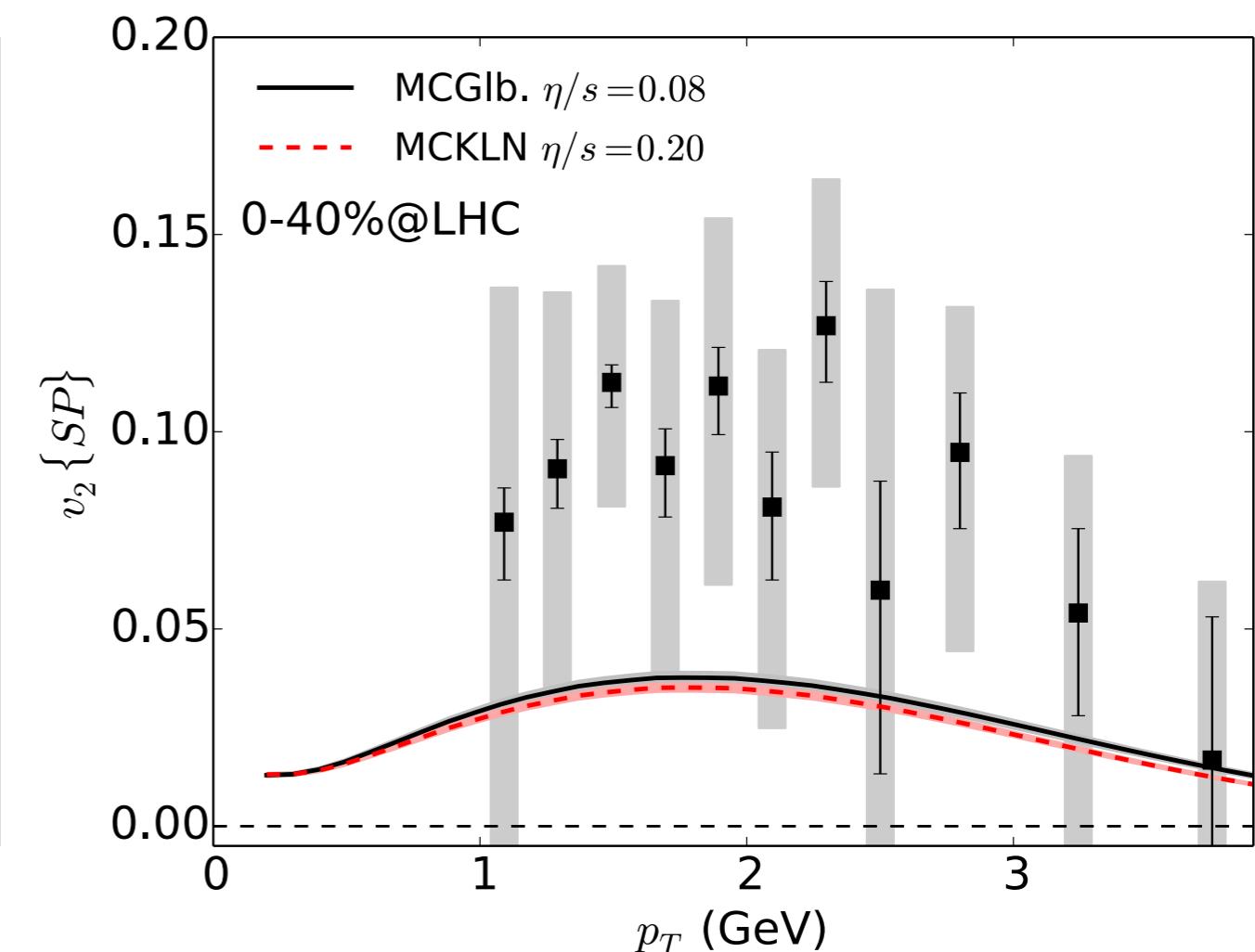


Comparisons with exp. data

RHIC 0-20%



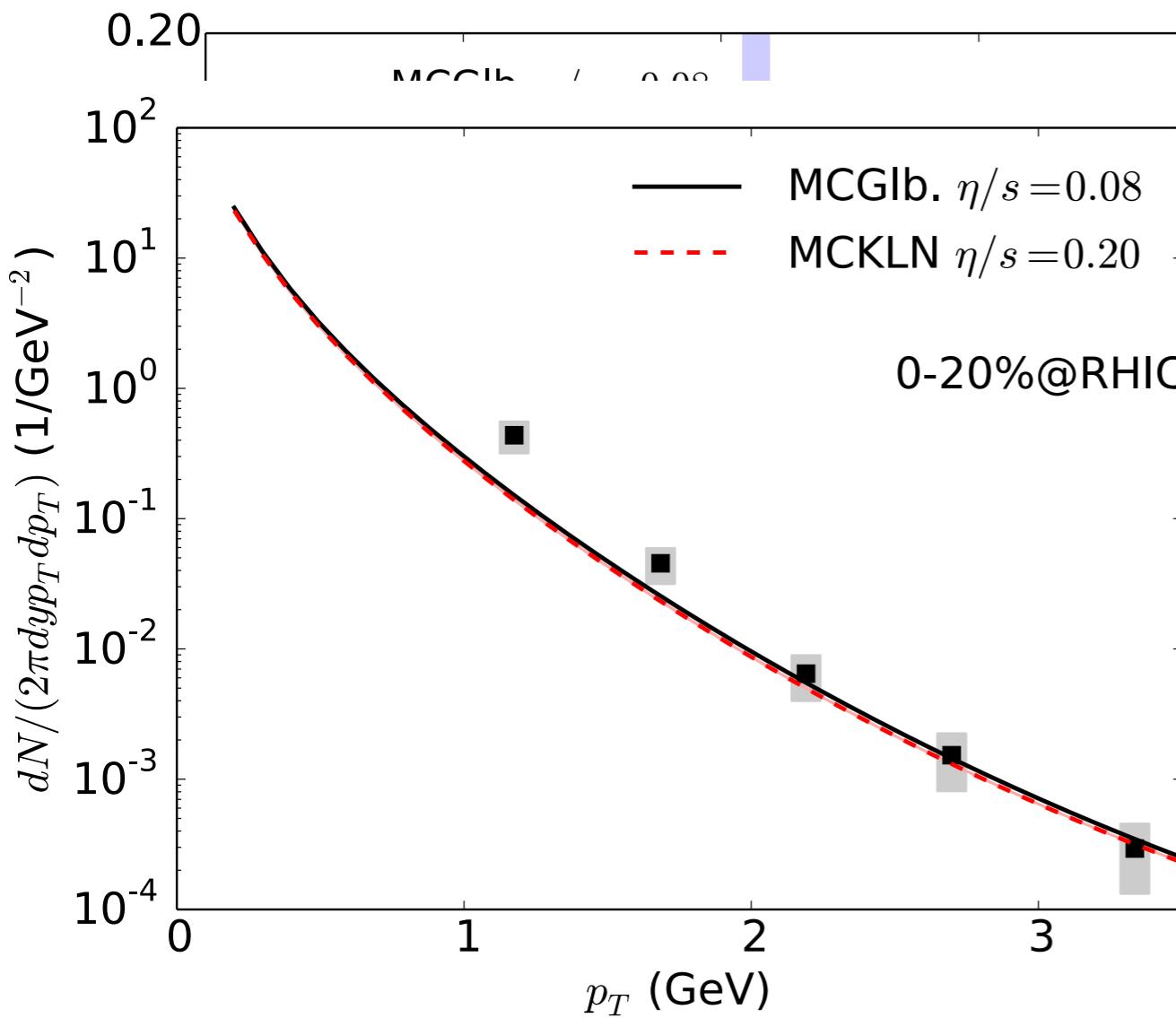
LHC 0-40%



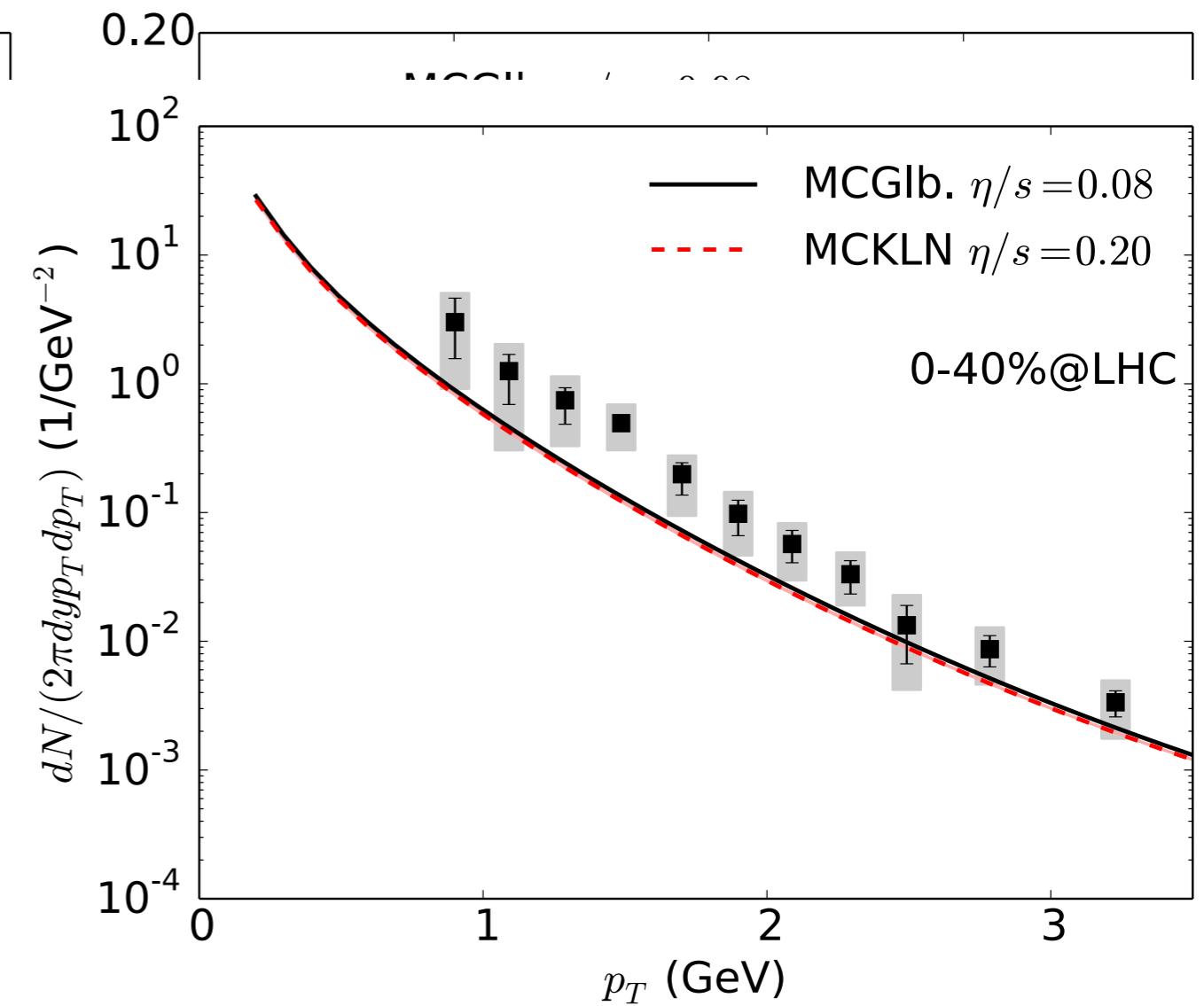
- Current calculations still underestimate the experimental data by a factor of 3

Comparisons with exp. data

RHIC 0-20%



LHC 0-40%



- Current calculations still underestimate the experimental data by a factor of 3
- Thermal yield is also missing in the azimuthally integrated photon spectra at low p_T

EM decays of short-lived resonances (I)

Thanks to Ralf Rapp and EMMI RRTF

Contributions from the short-lived resonances:

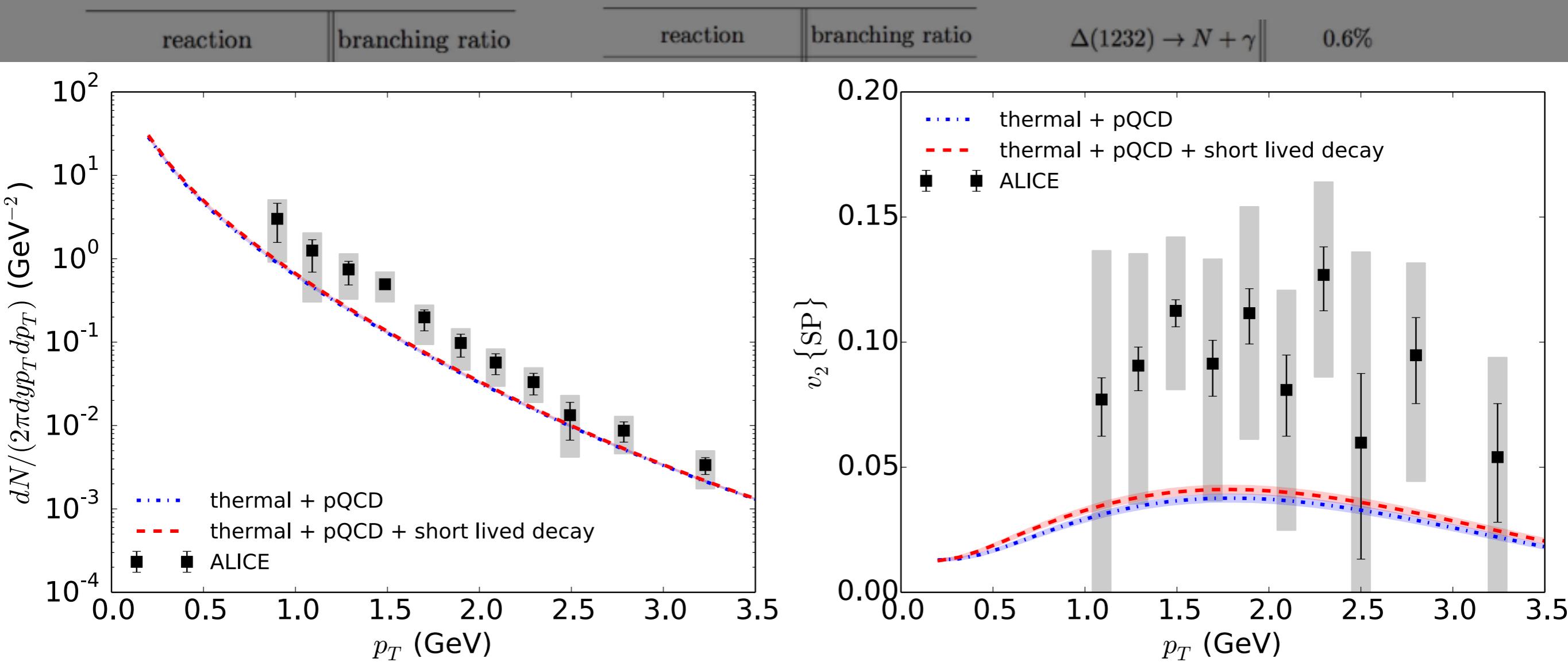
reaction	branching ratio
$\rho^0 \rightarrow \pi^+ + \pi^- + \gamma$	1%
$b_1(1235) \rightarrow \pi^\pm + \gamma$	$1.6 * 10^{-3}$
$h_1(1170) \rightarrow \pi^0 + \gamma$	$1.7 * 10^{-3}$
$a_1(1260) \rightarrow \pi^0 + \gamma$	$1.7 * 10^{-3}$
$f_1(1285) \rightarrow \rho_0 + \gamma$	5.5%
$a_2(1320) \rightarrow \pi^\pm + \gamma$	$2.68 * 10^{-3}$
$K^*(892) \rightarrow K^0 + \gamma$	$2.4 * 10^{-3}$
$K^*(892) \rightarrow K^\pm + \gamma$	$1 * 10^{-3}$
$K_1(1270) \rightarrow K^0 + \gamma$	$8.4 * 10^{-4}$
$K_1(1400) \rightarrow K^0 + \gamma$	$1.6 * 10^{-3}$
$K_2^*(1430) \rightarrow K^+ + \gamma$	$2.4 * 10^{-3}$
$K_2^*(1430) \rightarrow K^0 + \gamma$	$9 * 10^{-4}$

reaction	branching ratio	$\Delta(1232) \rightarrow N + \gamma$	0.6%
$N(1440) \rightarrow p + \gamma$	$4.15 * 10^{-4}$	$\Delta(1600) \rightarrow N + \gamma$	$1.8 * 10^{-4}$
$N(1440) \rightarrow n + \gamma$	$3 * 10^{-4}$	$\Delta(1620) \rightarrow N + \gamma$	$6.5 * 10^{-4}$
$N(1520) \rightarrow p + \gamma$	$4.15 * 10^{-3}$	$\Delta(1700) \rightarrow N + \gamma$	$4.1 * 10^{-3}$
$N(1520) \rightarrow n + \gamma$	$4.15 * 10^{-3}$	$\Delta(1905) \rightarrow N + \gamma$	$2.4 * 10^{-4}$
$N(1530) \rightarrow p + \gamma$	$2.25 * 10^{-3}$	$\Delta(1910) \rightarrow N + \gamma$	$1 * 10^{-4}$
$N(1530) \rightarrow n + \gamma$	$2.25 * 10^{-3}$	$\Delta(1920) \rightarrow N + \gamma$	$2 * 10^{-3}$
$N(1650) \rightarrow p + \gamma$	$1.2 * 10^{-3}$	$\Delta(1950) \rightarrow N + \gamma$	$1.05 * 10^{-3}$
reaction	branching ratio		
$\Lambda(1405) \rightarrow \Lambda + \gamma$		$5.4 * 10^{-4}$	
$\Lambda(1405) \rightarrow \Sigma^0 + \gamma$		$2 * 10^{-4}$	
$\Lambda(1520) \rightarrow \Lambda + \gamma$		$8.5 * 10^{-3}$	
$\Lambda(1520) \rightarrow \Sigma^0 + \gamma$		2%	
$\Sigma^0(1385) \rightarrow \Lambda + \gamma$		1.25%	
$\Xi(1530) \rightarrow \Xi + \gamma$		4%	

EM decays of short-lived resonances (II)

Thanks to Ralf Rapp and EMMI RRTF

Contributions from the short-lived resonances:

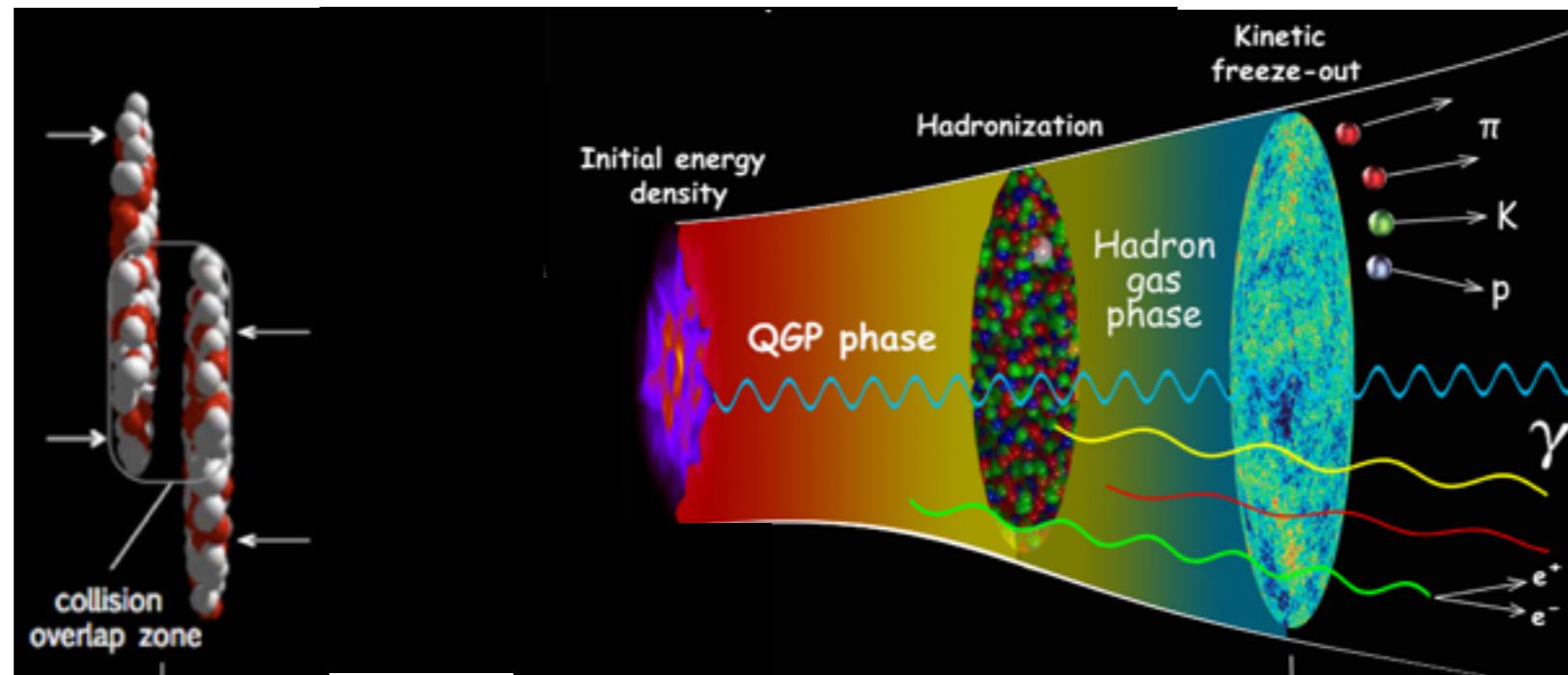


Small but significant effects in the right direction

$N(1710) \rightarrow n + \gamma$	$1 * 10^{-4}$
$N(1720) \rightarrow p + \gamma$	$1.5 * 10^{-3}$
$N(1720) \rightarrow n + \gamma$	$8 * 10^{-5}$
$\Xi(1530) \rightarrow \Xi + \gamma$	4%

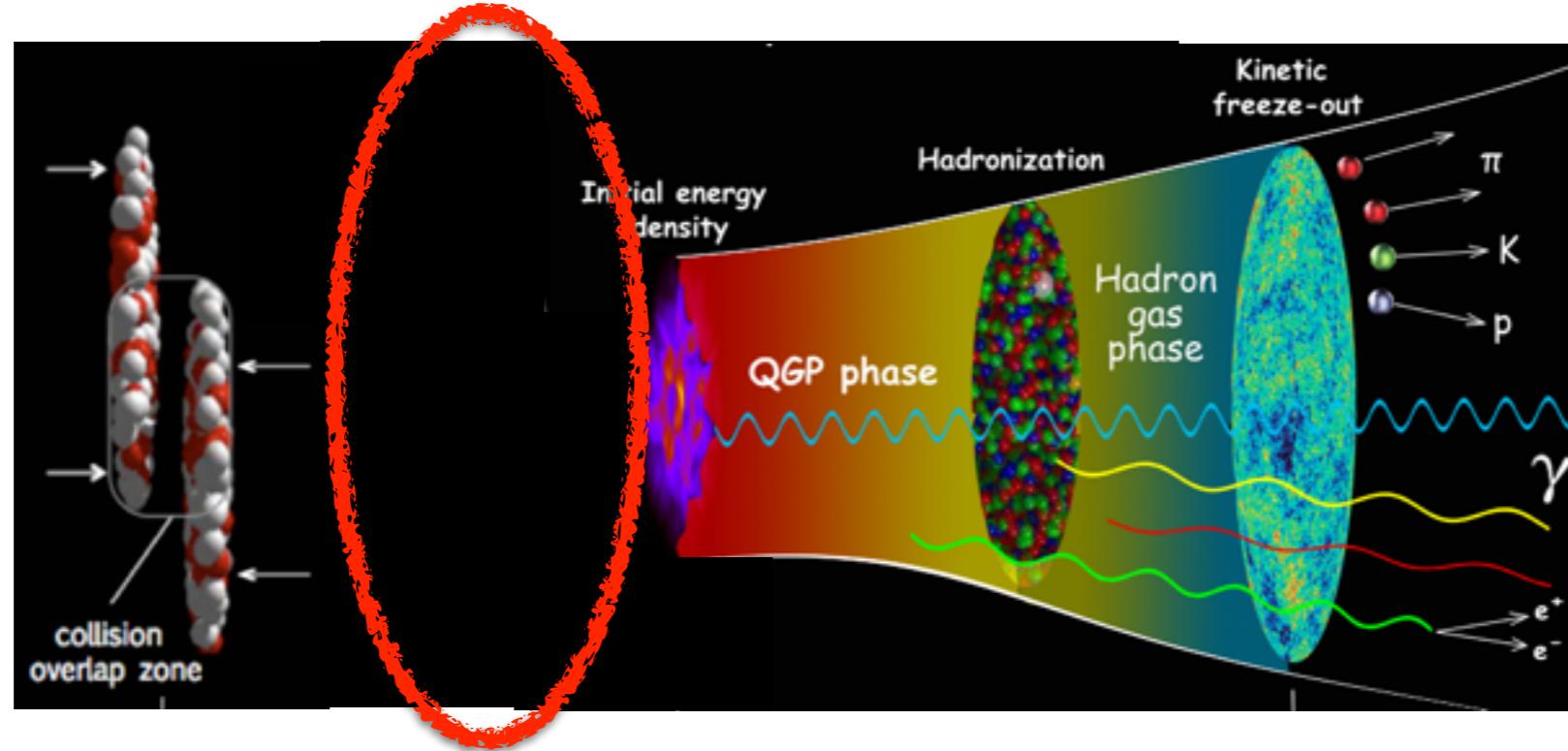
Pre-equilibrium flow (I)

Contributions from pre-equilibrium flow and $\pi^{\mu\nu}$:



Pre-equilibrium flow (II)

Contributions from pre-equilibrium flow and $\pi^{\mu\nu}$:



Free-streaming

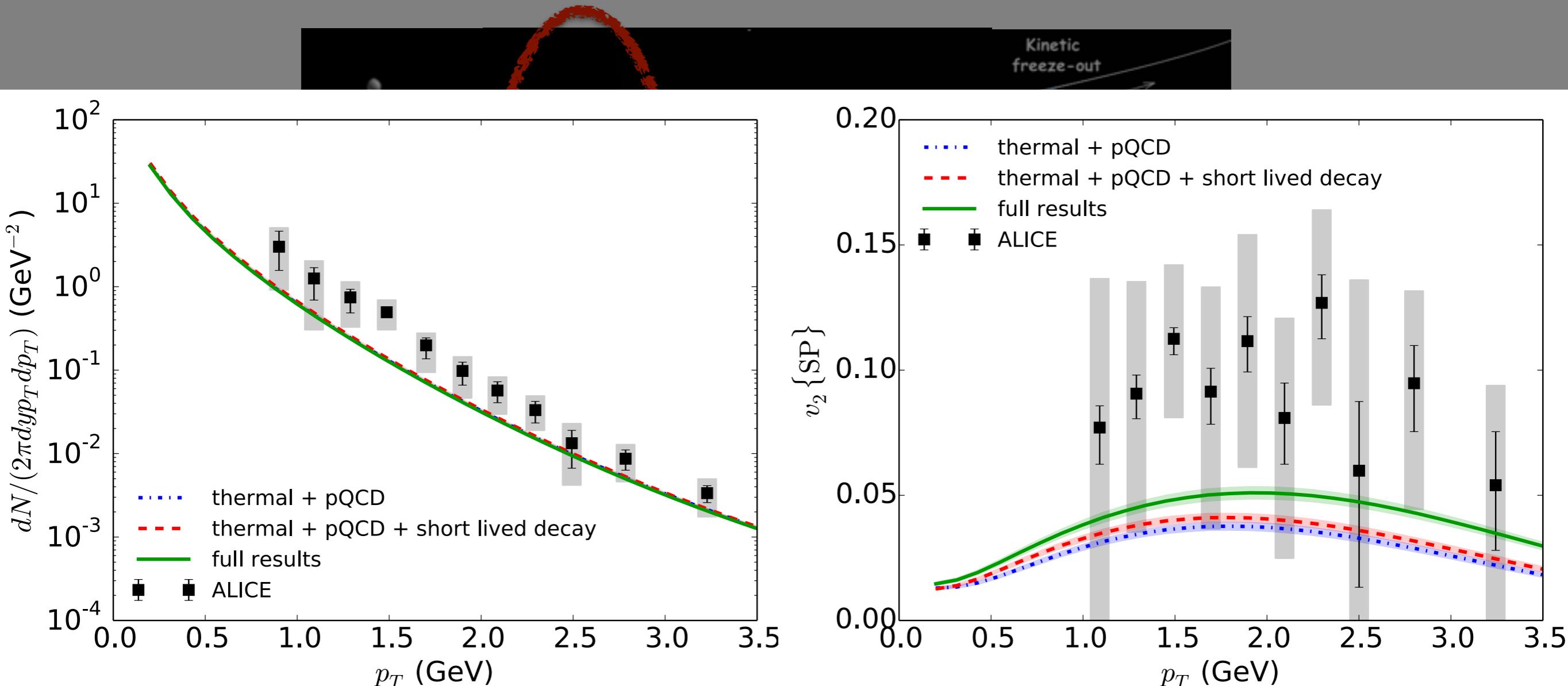
$$f(\tau_s, \vec{x}, \vec{p}) = f(\tau_0, \vec{x} - \hat{\vec{p}}(\tau_s - \tau_0), \vec{p})$$

$$T^{\mu\nu}(\tau_s, \vec{x}) = \int \frac{d^3 p}{E} p^\mu p^\nu f(\tau_s, \vec{x}, \vec{p})$$

$$T^{\mu\nu} u_\nu = e u^\mu \rightarrow = e u^\mu u^\nu - (P + \Pi) \Delta^{\mu\nu} + \pi^{\mu\nu}$$

Pre-equilibrium flow (III)

Contributions from pre-equilibrium flow and $\pi^{\mu\nu}$:



Small but significant effects in the right direction

Conclusion and outlook

- **iEBE** provides an advanced model framework to describe the bulk dynamics of relativistic heavy-ion collisions *event-by-event*
- **iEBE-JET** interface couples medium evolution with rare probes (**EM**, **jet**, **heavy-quark**) has been developed
- **iEBE-JET** has been applied to phenomenological studies to resolve direct photon flow puzzle

Coming soon

- Bulk viscosity, conserved current (net baryon density), pre-equilibrium dynamics

Thank you!

HDFView 2.9

File Window Tools Help

Recent Files /Users/Chun/Desktop/VISHJet/JetReader_h5/JetData.h5 Clear Text

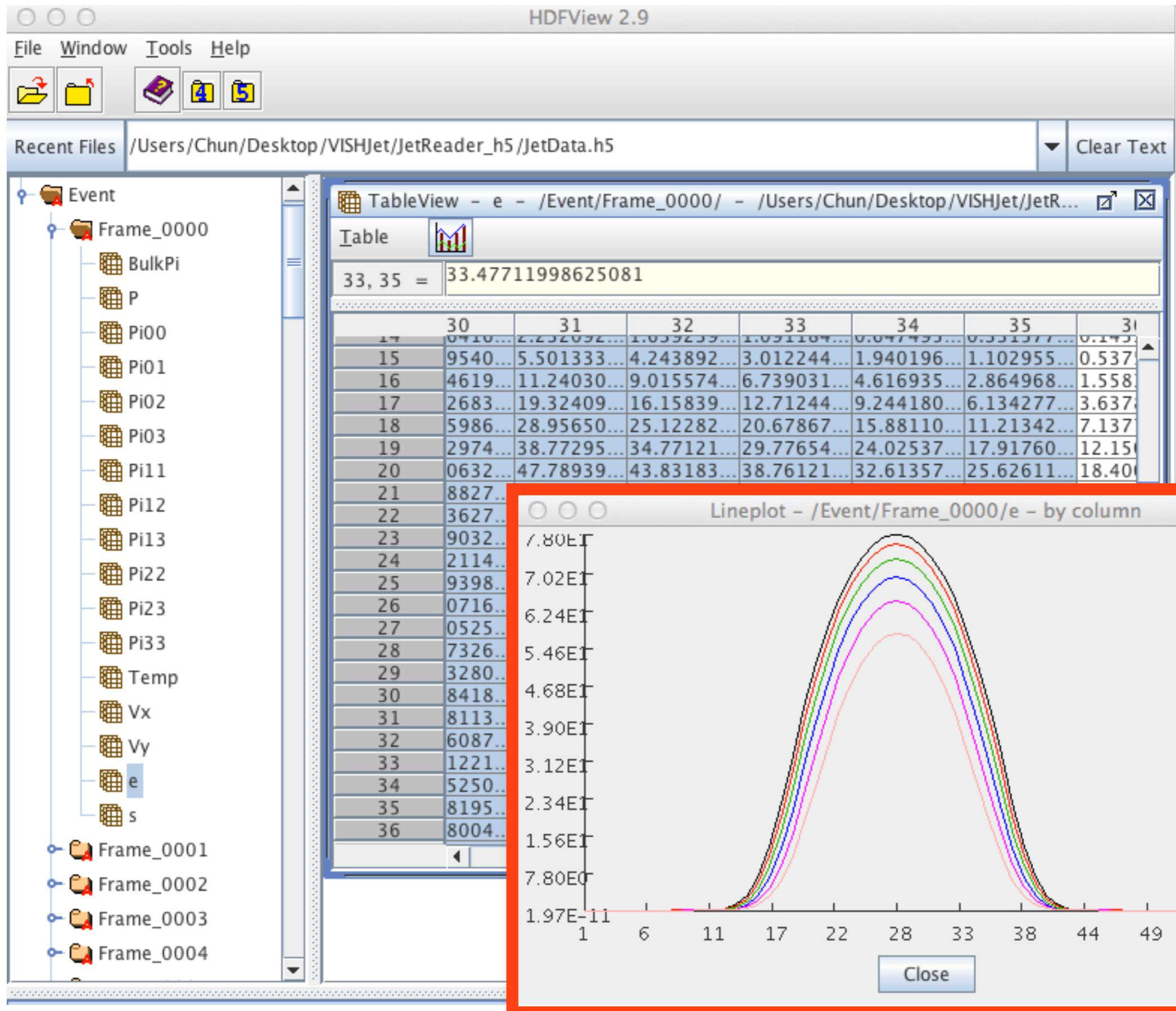
Event

- Frame_0000
 - BulkPi
 - P
 - Pi00
 - Pi01
 - Pi02
 - Pi03
 - Pi11
 - Pi12
 - Pi13
 - Pi22
 - Pi23
 - Pi33
 - Temp
 - Vx
 - Vy
 - e
 - s
- Frame_0001
- Frame_0002
- Frame_0003
- Frame_0004

TableView - e - /Event/Frame_0000/ - /Users/Chun/Desktop/VISHJet/JetR...

Table

	30	31	32	33	34	35	31
14	0.010...	2.232092...	1.059259...	1.051104...	0.047455...	0.331577...	0.145
15	9540...	5.501333...	4.243892...	3.012244...	1.940196...	1.102955...	0.537
16	4619...	11.24030...	9.015574...	6.739031...	4.616935...	2.864968...	1.558
17	2683...	19.32409...	16.15839...	12.71244...	9.244180...	6.134277...	3.637
18	5986...	28.95650...	25.12282...	20.67867...	15.88110...	11.21342...	7.137
19	2974...	38.77295...	34.77121...	29.77654...	24.02537...	17.91760...	12.150
20	0632...	47.78939...	43.83183...	38.76121...	32.61357...	25.62611...	18.400
21	8827...	55.36830...	51.75123...	46.88671...	40.80240...	33.44054...	25.230
22	3627...	61.68726...	58.27822...	53.72573...	47.87399...	40.53977...	31.920
23	9032...	66.79653...	63.59296...	59.28769...	53.63173...	46.51820...	37.830
24	2114...	70.56792...	67.50041...	63.49622...	58.07359...	51.17967...	42.590
25	9398...	73.22076...	70.27761...	66.36614...	61.25957...	54.54567...	46.050
26	0716...	74.85708...	71.91222...	68.06815...	63.04095...	56.49256...	48.170
27	0525...	75.44244...	72.48026...	68.64248...	63.64327...	57.11430...	48.880
28	7326...	74.84248...	71.92227...	68.09761...	63.05448...	56.57156...	48.190
29	3280...	73.19948...	70.28023...	66.36931...	61.29588...	54.65882...	46.210
30	8418...	70.52506...	67.45372...	63.43256...	58.20686...	51.37563...	42.770
31	8113...	66.62568...	63.47792...	59.24158...	53.74454...	46.65683...	37.960
32	6087...	61.60145...	58.21612...	53.73818...	47.89930...	40.62639...	32.050
33	1221...	55.28014...	51.65916...	46.82691...	40.76745...	33.47711...	25.310
34	5250...	47.65685...	43.74935...	38.73913...	32.62259...	25.65196...	18.410
35	8195...	38.74274...	34.67429...	29.70844...	24.00035...	17.93292...	12.150
36	8004...	28.93837...	25.12687...	20.67658...	15.89817...	11.22946...	7.146



HDFView 2.9

File Window Tools Help

Recent Files /Users/Chun/Desktop/VISHJet/JetReader_h5/JetData.h5 Clear Text

Event

- Frame_0000
 - BulkPi
 - P
 - Pi00
 - Pi01
 - Pi02
 - Pi03
 - Pi11
 - Pi12
 - Pi13
 - Pi22
 - Pi23
 - Pi33
 - Temp
 - Vx
 - Vy
 - e
 - s
- Frame_0001
- Frame_0002
- Frame_0003
- Frame_0004

TableView - e - /Event/Frame_0000/ - /Users/Chun/Desktop/VISHJet/JetR...

Table

33, 35 =	33.47711998625081					
30	31	32	33	34	35	31
15	9540...	5.501333...	4.243892...	3.012244...	1.940196...	1.102955...
16	4619...	11.24030...	9.015574...	6.739031...	4.616935...	2.864968...
17	2683...	19.32409...	16.15839...	12.71244...	9.244180...	6.134277...
18	5986...	28.95650...	25.12282...	20.67867...	15.88110...	11.21342...
19	7074...	38.77005...	35.77005...	31.00000...	21.00000...	17.00000...

Properties - /Event

General Attributes

Number of attributes = 9

Add Delete

Name	Value	Type	Array Size
DX	0.5	64-bit floating-point	1
DY	0.5	64-bit floating-point	1
OutputViscousFlag	1	32-bit integer	1
Tau0	0.6	64-bit floating-point	1
XH	27	32-bit integer	1
XL	-27	32-bit integer	1
YH	27	32-bit integer	1
YL	-27	32-bit integer	1
dTau	0.1	64-bit floating-point	1

Close